## Work, Energy \& Power

1. Nov 01-Q/4

A sphere has volume $V$ and is made of metal of density $\rho$.
(a) Write down an expression for the mass $m$ of the sphere in terms of $V$ and $\rho$. [1]
(b) The sphere is immersed in a liquid. Explain the apparent loss in the weight of the sphere. [3]
(c) The sphere in (b) has mass $2.0 \times 10^{-3} \mathrm{~kg}$. When the sphere is released, it eventually falls in the liquid with a constant speed of $6.0 \mathrm{cms}^{-1}$.
(i) For this sphere travelling at constant speed, calculate

1. its kinetic energy, kinetic energy = . $\qquad$ . J
2. its rate of loss of gravitational potential energy.
rate $=$ $\qquad$ $\mathrm{J} \mathrm{s}^{-1}[5]$
(ii) Suggest why it is possible for the sphere to have constant kinetic energy whilst losing potential energy at a steady rate.[2]
3. May 02-Q/4

A steel ball of mass 73 g is held 1.6 m above a horizontal steel plate, as illustrated in Fig. 4.1.


Fig. 4.1
The ball is dropped from rest and it bounces on the plate, reaching a height $h$.
(a) Calculate the speed of the ball as it reaches the plate. speed = $\qquad$ ms-1 [2]
(b) As the ball loses contact with the plate after bouncing, the kinetic energy of the ball is $90 \%$ of that just before bouncing. Calculate
(i) the height $h$ to which the ball bounces, $\quad h=$ $\qquad$ m
(ii) the speed of the ball as it leaves the plate after bouncing. speed $=$ ms -1
[4]
(c) Using your answers to (a) and (b), determine the change in momentum of the ball during the bounce.
change $=$. $\qquad$
(d) With reference to the law of conservation of momentum, comment on your answer to (c). [3]
3. May 02-Q/5

Some gas is contained in a cylinder by means of a moveable piston, as illustrated in Fig. 5.1.


Fig. 5.1
State how, for this mass of gas, the following changes may be achieved.
(a) increase its gravitational potential energy [1]
(b) decrease its internal energy [1]
(c) increase its elastic potential energy [1]
4. May 03-Q/2
(a) (i) Define displacement.
(ii) Use your definition to explain how it is possible for a car to travel a certain distance and yet have zero displacement. [3]
(b) A car starts from rest and travels upwards along a straight road inclined at an angle of $5.0^{\circ}$ to the horizontal, as illustrated in Fig. 2.1.


Fig. 2.1
The length of the road is 450 m and the car has mass 800 kg . The speed of the car increases at a constant rate and is $28 \mathrm{~m} \mathrm{~s}^{-1}$ at the top of the slope.
(i) Determine, for this car travelling up the slope, 1. its
acceleration, acceleration = ................................... $\mathrm{ms}^{-1}$ [2]
2. the time taken to travel the length of the slope,
time taken =
3. the gain in kinetic energy, gain in kinetic energy =
4. the gain in gravitational potential energy. gain in potential energy =
(ii) Use your answers in (i) to determine the useful output power of the car.
power=
[3]
(iii) Suggest one reason why the actual power output of the car engine is greater than that calculated in (ii).
5. May 04-Q/4

A ball has mass $m$. It is dropped onto a horizontal plate as shown in Fig. 4.1.


Fig. 4.1
Just as the ball makes contact with the plate, it has velocity $v$, momentum $p$ and kinetic energy $E_{\mathrm{k}}$.
(a) (i) Write down an expression for momentum $p$ in terms of $m$ and $v$.
(ii) Hence show that the kinetic energy is given by the expression

$$
E_{\mathrm{k}}=\frac{p^{2}}{2 m}
$$

6. May 05-Q/3

A bullet of mass 2.0 g is fired horizontally into a block of wood of mass 600 g . The block is suspended from strings so that it is free to move in a vertical plane.
The bullet buries itself in the block. The block and bullet rise together through a vertical distance of 8.6 cm , as shown in Fig. 3.1.


Fig. 3.1
(a) (i) Calculate the change in gravitational potential energy of the block and bullet.
change $=$
J [2]
(ii) Show that the initial speed of the block and the bullet, after they began to move off together, was $1.3 \mathrm{~ms}^{-1}$. [1]
(b) Using the information in (a)(ii) and the principle of conservation of momentum, determine the speed of the bullet before the impact with the block.
speed = .
(c) (i) Calculate the kinetic energy of the bullet just before impact.
kinetic energy = $\qquad$ J [2]
(ii) State and explain what can be deduced from your answers to (c)(i) and (a)(i) about the type of collision between the bullet and the block.[2]
7.Nov 05-Q/8
(a) Explain the concept of work. [2]
(b) A table tennis ball falls vertically through air. Fig. 8.1 shows the variation of the kinetic energy $E_{K}$ of the ball with distance $h$ fallen. The ball reaches the ground after falling through a distance $h_{0}$.


Fig. 8.1
(i) Describe the motion of the ball. [3]
(ii) On Fig. 8.1, draw a line to show the variation with $h$ of the gravitational potential energy $E_{\mathrm{P}}$ of the ball. At $h=h_{0}$, the potential energy is zero. [3]
8. Nov 06-Q/1
(a) Define what is meant by
(i) work done, [2]
(ii) power. [1]
(b) A force $F$ is acting on a body that is moving with velocity $v$ in the direction of the force. Derive an expression relating the power $P$ dissipated by the force to $F$ and $v$.
(c) A car of mass 1900 kg accelerates from rest to a speed of $27 \mathrm{~ms}^{-1}$ in 8.1 s .
(i) Calculate the average rate at which kinetic energy is supplied to the car during the acceleration. rate $=$ $\qquad$ W [2]
(ii) The car engine provides power at a constant rate. Suggest and explain why the acceleration of the car is not constant. [2]
8. Nov 06-Q/3

Francium-208 is radioactive and emits $\alpha$-particles with a kinetic energy of $1.07 \times 10^{-12} \mathrm{~J}$ to form nuclei of astatine, as illustrated in Fig. 3.1.


Fig. 3.1
(a) State the nature of an $\alpha$-particle. [1]
(b) Show that the initial speed of an $\alpha$-particle after the decay of a francium nucleus is approximately $1.8 \times 10^{7} \mathrm{~ms}^{-1}$. [2]
(c) (i) State the principle of conservation of linear momentum. [2]
(ii) The Francium-208 nucleus is stationary before the decay.

Estimate the speed of the astatine nucleus immediately after the decay.
speed = $\qquad$ $\mathrm{ms}^{-1}[3]$
(d) Close examination of the decay of the francium nucleus indicates that the astatine nucleus and the $\alpha$-particle are not ejected exactly in opposite directions. Suggest an explanation for this observation. [2]
9. May 07-Q/4
(a) A stone of mass 56 g is thrown horizontally from the top of a cliff with a speed of $18 \mathrm{~m} \mathrm{~s}^{-1}$, as illustrated in Fig. 4.1.


Fig. 4.1
The initial height of the stone above the level of the sea is 16 m . Air resistance may be neglected.
(i) Calculate the change in gravitational potential energy of the stone as a result of falling through 16 m .
change $=$ $\qquad$ J [2]
(ii) Calculate the total kinetic energy of the stone as it reaches the
sea. kinetic energy = $\qquad$
$\qquad$ J [3]
(b) Use your answer in (a)(ii) to show that the speed of the stone as it hits the water is approximately $25 \mathrm{~m} \mathrm{~s}^{-1}$. [1]
(c) State the horizontal velocity of the stone as it hits the water.
horizontal velocity $=$ $\qquad$ $\mathrm{m} \mathrm{s}^{-1}$ [1]
(d) (i) On the grid of Fig. 4.2, draw a vector diagram to represent the horizontal velocity and the resultant velocity of the stone as it hits the water. [1]


Fig. 4.2
(ii) Use your vector diagram to determine the angle with the horizontal at which the stone hits the water.
angle $=$ ${ }^{\circ}$ [2]
10.Nov 07-Q/3
(a) (i) Define potential energy. [1]
(ii) Distinguish between gravitational potential energy and elastic potential energy [2]
(b) A small sphere of mass 51 g is suspended by a light inextensible string from a fixed point $P$.
The centre of the sphere is 61 cm vertically below point $P$, as shown in Fig. 3.1.


Fig. 3.1
The sphere is moved to one side, keeping the string taut, so that the string makes an angle of $18^{\circ}$ with the vertical. Calculate (i) the gain in gravitational potential energy of the sphere, gain $=$
(ii) the moment of the weight of the sphere about point $P$. moment $=$ Nm [2]
11. May 08-Q/3

A shopping trolley and its contents have a total mass of 42 kg .
The trolley is being pushed along a horizontal surface at a speed of $1.2 \mathrm{~m} \mathrm{~s}^{-1}$. When the trolley is released, it travels a distance of 1.9 m before coming to rest.
(a) Assuming that the total force opposing the motion of the trolley is constant,
(i) calculate the deceleration of the trolley, deceleration = $\qquad$ $\mathrm{m} \mathrm{s}^{-2}[2]$
(ii) show that the total force opposing the motion of the trolley is 16 N. [1]
(b) Using the answer in (a)(ii), calculate the power required to overcome the total force opposing the motion of the trolley at a speed of $1.2 \mathrm{~m} \mathrm{~s}^{-1}$. power $=$ W [2]

