

# Internal Resistance MS

M1. (a) (i) (use of  $V = IR$ )

$$R_{\text{total}} = 1 \text{ (ohm)} \checkmark$$

$$V = 1 \times 1 = 1.0 \text{ V} \checkmark$$

2

(ii) (use of  $V = IR$ )

$$R = 9.0/1.0 = 9.0 \Omega \checkmark$$

$$r = 9.0 - 1.0 - 6.0 = 2.0 \Omega \checkmark$$

or use of ( $E = I(R + r)$ )

$$9.0 = 1(7 + r) \checkmark$$

$$r = 9.0 - 7.0 = 2.0 \Omega \checkmark$$

2

(iii) (use of  $W = VIt$ )

$$W = 9.0 \times 1.0 \times 5 \times 60 \checkmark$$

$$W = 2700 \text{ J} \checkmark$$

2

(iv) energy dissipated in internal resistance =  $I^2 \times 2.0 \times 5 \times 60 = 600 \text{ (J)}$   $\checkmark$

$$\text{percentage} = 100 \times 600/2700 = 22\% \checkmark \text{ CE from part aii}$$

2

(b) internal resistance limits current  $\checkmark$

hence can provide higher current  $\checkmark$

or energy wasted in internal resistance/battery  $\checkmark$

less energy wasted (with lower internal resistance)  $\checkmark$

or charges quicker  $\checkmark$

as current higher or less energy wasted  $\checkmark$

or (lower internal resistance) means higher terminal pd/voltage  $\checkmark$

as less pd across internal resistance or mention of lost volts  $\checkmark$

2

[10]

**M2.** (a) (i) energy changed to electrical energy per unit charge/coulomb passing through  
[or electrical energy produced per coulomb or unit charge]  
[or pd when no current passes through/or open circuit] **(1)**

(ii)  $I = \frac{6}{2.4} = 2.5 \text{ A}$  **(1)**

(iii) (use of  $\epsilon = I(R + r)$  gives)  $\epsilon = V + Ir$  and  $8 = 6 + Ir$  **(1)**

substitution gives  $8 - 6 = 2.5r$  **(1)** (and  $r = 0.8 \Omega$ )

4

(b) (i) (use of  $P = I^2R$  gives)  $P_R = 2.5^2 \times 2.4 = 15 \text{ W}$

[or  $P = VI$  gives  $P = 6 \times 2.5 = 15 \text{ W}$ ] **(1)**

(allow C.E. for value of  $I$  from (a))

(ii)  $P_T = 15 + (2.5^2 \times 0.8)$  **(1)**

$= 20 \text{ (W)}$  **(1)**

(allow C.E. for values of  $P_R$  and  $I$ )

(iii)  $E = 5 \times 2 \times 60 = 600 \text{ J}$  **(1)**

(allow C.E. for value of  $P$  from (i) and  $P_T$  from (ii))

4

**[8]**

**M3.** (i) ( $V = IR$  gives)  $12 = (30 + 30 + 2)I$  (1)

$$I = \left( \frac{12}{62} \right) = 0.19 \text{ A (1)} \quad (0.194 \text{ A})$$

(ii)  $V_{PQ} = 12 - (0.19 \times 2)$  (1)  
 $= 11.6 \text{ V (1)}$

(allow C.E. for incorrect  $I$  in (i))

[or  $V_{PQ} = 0.19 \times 60 = 11.6 \text{ V}$  ( $I = 0.194 \text{ A}$  gives  $11.6 \text{ V}$ )

[or  $V_{PQ} = 12 \times \frac{60}{62} = 11.6 \text{ V}$

(iii) ( $P_A = I^2 R$  gives)  $P_A = (0.19)^2 \times 30 = 1.08$  (1) W (1)

[or  $P_A = \frac{V^2}{R}$ ]

(allow C.E. for incorrect  $I$  in (i) or incorrect  $V$  in (ii))

(iv) ( $E = P_A t$  gives)  $E = 1.08 \times 20$  (1)

$= 21.6 \text{ J (1)}$

(allow C.E. for incorrect  $P_A$  in (iii))

[8]

**M4.** (a) (i) work (done)/energy (supplied) per unit charge (by battery) (1)

(or pd across terminals when no current passing through cell or open circuit)

1

(ii) when switch is closed a **current flows** (through the battery) (1)

hence a pd/lost volts develops across the internal resistance (1)

2

(b) (use of  $\epsilon = V + Ir$ )

$I = 5.8/10 = 0.58 \text{ (A) (1)}$

$6.0 = 5.8 + 0.58r$  (1)

$r = 0.2/0.58 = 0.34 \text{ (}\Omega\text{) (1)}$

3

- (c) need large current/power to start the car **(1)** (or current too low)

internal resistance limits the current/wastes power(or energy)/reduces terminal pd/increases lost volts **(1)**

2

[8]

- M5.** (a) (use of  $E = V + Ir$ )

$$12 = V + 420 \times 0.0095 \text{ (1)}$$

$$V = 8.0(1)\text{V (1)}$$

2

- (b)  $\rho = RA/I = 1.6 \times 10^{-3} \times 7.9 \times 10^{-5}/0.75 \text{ (1)}$

$$R = 1.7 \times 10^{-7} \text{ (1) } \Omega\text{m (1)}$$

3

[5]

- M6.** (a) (i) work done (by the battery) per unit charge **(1)**  
or (electrical) energy per unit charge  
or pd/voltage when open circuit/no current

- (ii) the resistance of the materials within the battery **(1)**  
or hindrance to flow of charge **in** battery  
or loss of pd/voltage per unit current

2

- (b) (i) (use of  $E = V + Ir$ )

$$12 = V + 800 \times 0.005 \text{ (1) (working/equation needs to be shown)}$$

$$V = 12 - 4 = 8.0\text{V (1)}$$

- (ii) (use of  $P = I^2r$ )

$$P = 800^2 \times 0.005 \text{ (1) (working/equation needs to be shown)}$$

$$P = 3200 \text{ (1) W (1) or } \text{J s}^{-1}$$

5

(c) car will probably **not** start (1)

battery will not be able to provide enough current (1)  
or less current  
or lower terminal pd/voltage

2

[9]

**M7.** (a) mention of pd across internal resistance or energy loss  
in internal resistance or  $\text{emf} > V$  ✓

pd across internal resistance/lost volts increases with  
current or correct use of equation to demonstrate ✓

2

(b) (i)  $y$  – intercept 1.52 V ( $\pm 0.01$  V) ✓

1

(ii) identifies gradient as  $r$  or use of equation ✓

substitution to find gradient or substitution in equation ✓

$$r = 0.45 \pm 0.02 \Omega \checkmark$$

3

(c) (i) same intercept ✓

double gradient (must go through 1.25,  $0.40 \pm 1.5$  squares) ✓

2

(ii) same intercept horizontal line ✓

1

(d) (i) (use of  $Q = It$ )

$$Q = 0.89 \times 15 = 13 \checkmark \text{ C } \checkmark$$

2

(ii) use of  $P = I^2 r$  ✓

$$P = 0.89^2 \times 0.45$$

$$P = 0.36 \text{ W } \checkmark$$

2

[13]

**M8.** (a) **battery** has internal resistance (1)  
**current** passes through (this resistance) (1)  
work done/voltage lost, which reduces the value of the emf (1)

3

QWC 1

- (b) (i) circuit diagram to show:  
two **cells** in series **(1)**  
two resistors, each labelled  $r$  **(1)**
- (ii) (use of  $P = IV$  gives)  $1.6 = 2.5 I$  **(1)** ( $I = 0.64$  (A))  
(use of  $\epsilon = V + Ir$  gives)  $3.0 = 2.5 + 0.64 \times 2r$  **(1)** **(1)**  
 $0.5 = 1.28r$  and  $r = 0.39 \Omega$  **(1)**  
[or  $R_{\text{bulb}} = 2.5^2/1.6 = 3.9$  ( $\Omega$ ) and  $2.5 = 3.9 \times I$  gives  $I = 0.64$  (A)  
'lost volts' =  $(3 - 2.5) = 0.5$  (V) i.e. 0.25 (V) per cell  
 $0.25 = 0.64r$  and  $r = 0.39 \Omega$ ]

5

- (c)  $\epsilon = V + Ir$  gives  $V = -Ir + \epsilon$  (equation of straight line) **(1)**  
intercept on  $y$ -axis gives  $\epsilon$  **(1)**  
gradient gives  $(-r)$  **(1)**

3

[11]

**M9.** (a)  $V = -Ir + \epsilon$  **(1)**

1

- (b) straight line (within 1st quadrant) **(1)**  
negative gradient **(1)**

2

- (c)  $\epsilon$  : intercept on voltage axis **(1)**  
 $r$ : gradient **(1)**

2

[5]

**M10.** (a) (i)  $6.0$  ( $\Omega$ ) **(1)**

1

(ii)  $4.5$  (V) **(1)**

1

- (iii) (use of  $I = V/R$ )

$I = 4.5/6.0 = 0.75$  (A) **(1)**

current through cell A =  $0.75/2 = 0.375$  (A) **(1)**

2

(iv) charge =  $0.375 \times 300 = 112$  **(1)** C **(1)**

2

- (b) cells C and D will go flat first or A and B last longer **(1)**

current/charge passing through cells C and D (per second) is double/more than that passing through A or B **(1)**

energy given to charge passing through cells **per second** is double or more than in cells C and D **(1)** or in terms of power

3

[9]

- M11.** (a) (i) electrical energy produced (in the battery) per unit charge **(1)**

[or potential/voltage across terminals when there is no current]

- (ii) there is a current (through the battery) **(1)**

voltage 'lost' across the internal resistance **(1)**

Max 2

- (b) (i)  $\epsilon = V + Ir$  **(1)**

- (ii) labelled scales **(1)**

correct plotting **(1)**

best straight line **(1)**

$\epsilon$ : intercept on y axis **(1)** = 9.2 ( $\pm$  0.1) V **(1)**

$$r: (-) \text{ gradient} = \frac{9.2}{0.65} = 14.2 \Omega \text{ (1) (range 14.0 to 14.3)}$$

8

[10]