

Hooke's Law and Young's Modulus - Mark Scheme

Q1.

Question Number	Answer	Mark
(a)	<ul style="list-style-type: none"> • Use of Young modulus = gradient (of either initial linear region of graph) (1) <p>(MP1 accept ratios of co-ordinates up to strains of $(E_{28})0.0015$ or $(E_2)0.0014$)</p> <ul style="list-style-type: none"> • See 3.2 to 3.3×10^{10} (Pa) Or 4.2 to 4.4×10^{10} (Pa) (1) • Comparison of the two values obtained i.e. use of E_{28}/E_2 Or $(E_{28}-E_2)/E_2$ (1) • $E_{28}/E_2 = 1.30$ to 1.40 Or $(E_{28}-E_2)/E_2 = 0.30$ to 0.40 (1) <p>(MP4 is conditional on candidates using the linear sections for both graphs in MP1)</p> <p><u>Example of calculation</u></p> $E_{28} = \frac{140 \times 10^6 \text{ Pa}}{0.0032} = 4.38 \times 10^{10} \text{ Pa}$ $E_2 = \frac{104 \times 10^6 \text{ Pa}}{0.0032} = 3.25 \times 10^{10} \text{ Pa}$ $E_{28}/E_2 = \frac{4.38 \times 10^{10} \text{ Pa}}{3.25 \times 10^{10} \text{ Pa}} = 1.35$	4
(b)	<ul style="list-style-type: none"> • Use of counting squares or approximation of the area to a series of shapes from the 28-day graph (1) • $\frac{0.35 \times 10^6 - \text{area under 28-day graph}}{0.35 \times 10^6}$ (1) • Percentage reduction = 12.0 % to 15.0 % (1) <p><u>Example of calculation</u></p> $\Delta E_{28} = (\frac{1}{2} \times 80 \times 10^6 \text{ Pa} \times 0.0019) + [\frac{1}{2}(80 + 128) \text{ Pa} \times 10^6 \times (0.0038 - 0.0019)] + (64 \times 0.0001 \times 4 \times 10^6 \text{ Pa}) = 299\,200 \text{ J m}^{-3}$ $\text{Percentage reduction} = \frac{350\,000 \text{ J m}^{-3} - 299\,200 \text{ J m}^{-3}}{350\,000 \text{ J m}^{-3}} \times 100 = 14.5 \%$	3
(c)	<ul style="list-style-type: none"> • The breaking stress/force is greater (1) • The concrete is less flexible Or the concrete is stiffer (Do not accept a greater Young modulus) (1) • There is a smaller plastic region Or the elastic region is greater Or there's little change in the toughness Or a change in the properties of the concrete after you've used it could cause problems (1) 	3
Total for question		10

Q2.

Question Number	Answer	Mark
(a)	Compares ≈ 40 (MPa) (compression) with ≈ 10 (MPa) (tension) (1) Breaking/fracture/ultimate stress/force (much) greater under compression Or Breaking/fracture/ultimate stress is 40 MPa under compression, and 10 MPa under tension. Or Breaking/fracture/ultimate stress is 30 MPa greater under compression. (1)	(2)
(b)	Breaking stress = 5.00 to 5.10 ($\times 10^8$ Pa) (1) Use of $\sigma = F/A$ (1) $F = 8.0/8.1 \times 10^5$ N (1)	(3)
(c)(i)	<u>Example of calculation</u> $A = \pi \times (2.25 \times 10^{-2} \text{ m})^2 = 1.59 \times 10^{-3} \text{ m}^2$ $F = 1.59 \times 10^{-3} \text{ m}^2 \times 5.05 \times 10^8 \text{ Pa} = 8.03 \times 10^5 \text{ N}$	
(c)(i)	Concrete can withstand high(er) stress/force under compression (1) Or Concrete is strong(er) under compression The concrete remains under compression when tensile force applied. Or Applied/tensile force first has to overcome the compression Or When tensile force applied, concrete is still under compression (1) The steel/rods take (some of) the force/stress Or The force/stress causes deformation of the steel (1) Steel can withstand a large(r) tensile force/stress Or Steel is strong(er) under tension Or Ultimate tensile stress of steel is large(r) (1)	(4)
(c)(ii)	(When force removed) the rod will not return to its original length/shape (1) Or The rod will be permanently/plastically deformed the concrete will not compress (as much) Or The compression force will be less/zero (1)	(2)
Total for question		11

Q3.

Question Number	Answer	Mark
(a)	<ul style="list-style-type: none"> Ratio of stress to strain (for a material). Or stress per unit strain. Or σ / ϵ with symbols defined. Or $\frac{F x}{A \Delta x}$ with symbols defined. 	(1)
(b)(i)	<ul style="list-style-type: none"> Mean diameter = 0.234 mm (rounds to) Use of $A = \pi r^2$ $A = 4.3 \times 10^{-8} \text{ m}^2$ or 0.043 mm^2 <p><u>Example of calculation</u> Mean diameter = $\frac{1}{4} (0.230 + 0.235 + 0.230 + 0.240) = 0.234 \text{ mm}$ Area = $\pi \frac{(0.234 \times 10^{-3} \text{ m})^2}{4} = 4.30 \times 10^{-8} \text{ m}^2$</p>	(1) (1) (1)
(b)(ii)	<ul style="list-style-type: none"> Use of $W = m g$ Use of gradient = $m / \Delta x$ in Young Modulus formula i.e. $E = \text{gradient} \times g \times x / A$ $E = 1.6 \times 10^{11} \text{ Pa}$ e.c.f. from (b)(i) <p><u>Example of calculation</u> Young modulus = $195 \times 9.81 \text{ N kg}^{-1} \times \frac{3.50 \text{ m}}{4.30 \times 10^{-8} \text{ m}^2}$ = $1.56 \times 10^{11} \text{ Pa}$</p>	(1) (1) (1)
(b)(iii)	<p>Shorter wire gives greater gradient.</p> <p>Young modulus the same.</p>	(1) (1)
		(2)

Q4.

Question Number	Answer	Mark
(a)(i)	<p>Use of fall factor = $\frac{\text{height fallen before the rope begins to stretch}}{\text{total unstretched length of rope}}$ (1)</p> <p>Use of $\epsilon = \frac{\Delta x}{x}$ with $x = 15.0$ m (1)</p> <p>Use of $E_{\text{grav}} = mg\Delta h$ (1)</p> <p>Use of $E_{\text{grav}} = E_{\text{el}}$ with their Δx (1)</p> <p>$F_{\text{max}} = 14\,000$ (N) (1)</p> <p><u>Example of calculation</u> Height fallen = $15.0 \text{ m} \times 0.8 = 12 \text{ m}$ $\Delta x = 0.09 \times 15.0 \text{ m} = 1.35 \text{ m}$ $E_{\text{grav}} = 71 \text{ kg} \times 9.81 \text{ N kg}^{-1} \times 12 \text{ m} = 8358 \text{ J}$ (from fall) $E_{\text{grav}} = 71 \text{ kg} \times 9.81 \text{ N kg}^{-1} \times 1.35 \text{ m} = 940.3 \text{ J}$ (from extension) $8358 \text{ J} + 940.3 \text{ J} = \frac{1}{2} \times F_{\text{max}} \times 1.35 \text{ m}$ $F_{\text{max}} = 13\,775 \text{ N}$</p>	5
(a)(ii)	<ul style="list-style-type: none"> This would not be a good idea, as the climber would reach a higher velocity (just before the rope stretches) (1) (Hence) the climber's deceleration/force (as the rope stretches) would be greater (1) 	2
(b)	<p>Max 6</p> <ul style="list-style-type: none"> Use of area under the graph to determine the stored energy (1) Energy = 800 J (new) (1) Energy = 700 J (old) (1) The old rope would absorb/store less energy (1) Use of $F = k\Delta x$ to determine k (accept gradient of a tangent) (1) Calculation of k for both ropes at same applied force (1) The old rope is not as stiff as the new rope (1) Or The old rope extends more (1) The old rope would break at a smaller applied force/stress (1) 	6
Total for question		13

Q5.

Question Number	Answer	Mark
	<p>A is the correct answer as strain = $\frac{\text{extension}}{\text{original length}} = \frac{0.2}{50}$ (1)</p> <p>B is not the correct answer as the extension in mm was not converted to cm before being used in the equation for strain</p> <p>C is not the correct answer as the extension in mm was not converted to cm and the incorrect formula of original length/extension was used</p> <p>D is not the correct answer as the incorrect formula of original length/extension was used</p>	

Q6.

Question Number	Answer	Mark
	<p>C is the correct answer</p> <p>A is not the correct answer as every column is wrong. B is not the correct answer as the P and Q columns are the wrong way round. D is not the correct answer as the Q and R columns are the wrong way round.</p>	(1)

Q7.

Question Number	Answer	Mark
(a)(i)	<ul style="list-style-type: none"> $E_{el} = \frac{1}{2} k \Delta x^2$ Or Use of $E_{el} = \frac{1}{2} F \Delta x$ and use of $F = k \Delta x$. Elastic PE is transferred into kinetic energy Or $E_{el} = E_k$ $\frac{1}{2} m v^2 = \frac{1}{2} k \Delta x^2$ States that m and k are constant so $v \propto \Delta x$. Or States that $v = \sqrt{\frac{k}{m}} \Delta x$. 	(1) (1) (1) (1)
(a)(ii)	<ul style="list-style-type: none"> Gradient calculated. Or Use of a point on the line in a relevant equation. Use of $\frac{1}{2} k \Delta x^2 = \frac{1}{2} m v^2$ or gradient = $\sqrt{(k/m)}$ i.e. $k = m \times \text{gradient}^2$ k in range 22 – 26 N m⁻¹ <p><u>Example of calculation</u> Gradient $\frac{4.8 \text{ m s}^{-1} - 2.2 \text{ m s}^{-1}}{0.30 \text{ m}} = 8.67 \text{ (s}^{-1}\text{)}$ $k = \text{mass} \times \text{gradient}^2$ $k = 3.0 \times 10^{-1} \text{ kg} \times (8.67 \text{ s}^{-1})^2$ $k = 22.6 \text{ N m}^{-1}$</p>	(1) (1) (1)
(b)	<ul style="list-style-type: none"> Limit of proportionality exceeded. Or Extension no longer proportional to force. Range of Hooke's Law exceeded. Or Hooke's Law no longer applies. 	(1) (1)
		(4) (3) (2)