

GCSE Maths – Geometry and Measures

Rotation, Reflection, Translation, and Enlargement

Worksheet

NOTES



SOLUTIONS



This worksheet will show you how to work through rotations, reflections, translations, and enlargements. Each section contains a worked example, a question with hints and then questions for you to work through on your own.

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Section A - Reflection



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If you get stuck, look back at the worked and guided examples.

- 1. Each square in the grid is of length 1.
- a) Reflect the following shape in the line x = 7



b) Reflect the following shape in the line y = x





c) Reflect the following shape in the line x = -3.



d) Reflect the following shape in the line y = x - 1







Section B - Translation



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If you get stuck, look back at the worked and guided examples.

Each square in the grid is of length 1.

- 2. The following graph shows two shapes labelled A and B.
 - a) Work out the vector that translates shape A to shape B.
 - b) Work out the vector that translates shape B to shape A.



3. Translate the following shape by the vector $\begin{pmatrix} 4 \\ -4 \end{pmatrix}$.







- 4. The following grid shows two shapes labelled A and B.
 - a) What vector transforms shape A to shape B?
 - b) Translate shape B by the vector $\begin{pmatrix} -1 \\ -2 \end{pmatrix}$.



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Section C - Enlargement



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If you get stuck, look back at the worked and guided examples.

Each square in the grid is of length 1.

5. Consider the following graph with shape A and shape B.

Mark the centre of enlargement if shape B is enlarged to shape A. What is the scale factor for this enlargement?



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- 6. Consider shape A in the following grid.
 - a) Enlarge shape A by a scale factor of 3, and name the new shape 'shape C'.
 - b) Enlarge shape A by a scale factor of $\frac{1}{2}$, and name the new shape 'shape D'.

Centre of enlargement for both the enlargements is (0,1).







- 7. Enlarge the following shape by the scale factor 2 with centre of enlargement:
 - a) the origin
 - b) (5,4)
 - c) (−1,−1)

Label the new shapes as A, B and C, respectively.



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Section D - Enlargement (Higher Only)



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If you get stuck, look back at the worked and guided examples.

Each square in the grid is of length 1.

8. Describe fully the transformation that transforms shape A to shape B.



9. Enlarge the following shape by scale factor -2 with centre of enlargement (1,1).







Section E - Rotations

Worked Example

Rotate the following shape 90° anti-clockwise with the origin as the centre of rotation.



▶ Image: Second Second

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Step 1: Place tracing paper on the graph, trace the original shape and mark the centre of rotation.

Step 2: Hold down the writing pen on the centre of rotation and rotate the tracing paper according to the rotation described in the question.

▶ Image: Contraction PMTEducation

Step 3: Remove the tracing paper and draw the final image on the graph.

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If you get stuck, look back at the worked and guided examples.

Each square in the grid is of length 1.

10. Rotate the following shape by 90° clockwise with centre of rotation (2,2).



11. Rotate the following shape 90° anticlockwise with centre of rotation at the origin.





- 12. Consider the shape on the following grid.
 - a) Rotate the following shape 270° anti-clockwise with centre of rotation (1, -2). Label this shape B.
 - b) Rotate shape B 90° clockwise around the same centre of rotation. Name this shape C.
 - c) Describe the rotation which will map the initial shape to shape C.







Section F – Combined Transformations (Higher Only)



Perform the following transformations to the shape below:

- Reflect the following shape in the line x = 1. Label the shape B.
- Reflect shape B in the line *y* = 3. Label this shape C.
- Rotate shape C about the origin clockwise 180°.

Explain if there are any invariant points between the transformations.



Step 1: Transformations need to be done in the order described.

Reflection in the line x = 1:



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Guided Example

Perform the following transformations to the shape below:

- Rotate the following shape 180° clockwise with centre of rotation (0, 2). Label the shape B.
- Rotate B anti-clockwise 180° with centre of rotation (0, 3). Label this shape C.

Find a transformation, that can transform the initial shape to shape C.



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If you get stuck, look back at the worked and guided examples.

Each square in the grid is of length 1.

- 13. Translate the following shape by the series of translations described:
 - Reflect the following shape in the line x = 1. Label the shape B.
 - Translate shape B by the vector $\binom{3}{1}$. Label the new shape C.
 - Rotate shape C 270° anticlockwise about the point (4, −2). Label the new shape D.

Find and reason the presence of any invariant vertices from the initial shape to the final shape.







14. Shape A is reflected in the line y = 3, which is then reflected in the line x = 3. The final shape is labelled B.

Describe the single transformation that maps A to B.



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15. Describe transformations for the following shape, that would lead to 1 or more than 1 invariant vertices of the triangle. These are **not** combined transformations. One of each, rotation, enlargement, translation, and reflection.



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16. The following shape is rotated around the origin 270° clockwise and then reflected in the line x = y.

Describe the transformation that maps the initial image to the final image. Label any invariant points if present.





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