

GCSE Maths – Algebra

Forming and Solving Equations

Worksheet

NOTES



SOLUTIONS



This worksheet will show you how to work out different types of questions involving forming and solving equations. Each section contains a **worked example**, a **question with hints** and then **questions for you to work through** on your own.

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Section A

Worked Example

Clara, Marty and Karen each win a share of a raffle prize. Clara wins twice as much as Marty, and Karen wins £50 less than Clara.

If the total prize money was £400, how much money did Marty win?

Step 1: Identify the unknown value which we are trying to find.

We are looking for the amount of money won by Marty.

Let x = the amount of money won by Marty

Step 2: Use the information in the question to express Clara and Karen's winning in an expression involving x .

Clara wins twice as much as Marty. So, Clara wins £ $2x$.

Karen wins £50 less than Clara, so Karen wins £ $(2x - 50)$.

Step 3: Create an equation using the amount won by each winner and other information we are given.

The total prize money is £400, so the sum of Marty, Clara and Karen's winnings must be £400.

$$x + 2x + (2x - 50) = 400$$

Step 4: Solve the linear equation to find x .

$$x + 2x + (2x - 50) = 400$$

$$5x - 50 = 400$$

$$5x = 450$$

$$x = \frac{450}{5}$$

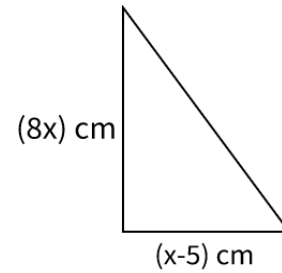
$$x = 90$$

Marty won £90.



Guided Example

Consider the triangle shown on the right.
The area of the right-angled triangle is 56 cm^2 .
Find the exact length of the hypotenuse.



Step 1: Create an equation for the area of the triangle in terms of x .

We know the formula for area of triangle:

$$\text{Area} = \text{Base} \times \text{Height} \times \frac{1}{2}$$

Step 2: Solve the quadratic equation you have created to find x .

Step 3: Substitute the value for x into the base and height lengths.

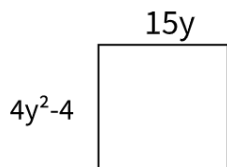
Step 4: Use Pythagoras' Theorem to find the length of the hypotenuse.



Now it's your turn!

If you get stuck, look back at the worked and guided examples.

1. Consider the square below. Calculate the length of the side.



2. Rose, David and Rani work for an advertising company, and are tasked with selling festival tickets. Rose sells 100 more than David and Rani sells three times as much as David. All together they sell 800 tickets. How many tickets did David sell?
3. I am thinking of a number. I add four to the number, and then multiply the result by 8. I then divide the result by 3. The final result is 48. Form an equation to show the process the starting number has gone through and use it to calculate what number I started with.
4. Michelle is saving up for a handbag costing £108. She works for one week at £6.50 per hour, and at the end of the week, her grandmother gives her £17. If by this time she has the exact amount to purchase the handbag, how many hours did she work that week?



Section B

Worked Example

Marge thinks of two positive integers. One number is four times the other, and the product of the two numbers is 64.

Step 1: Identify the unknown values we are trying to find as letters.

Let the smaller integer = a

Let the bigger integer = b

Step 2: Express the relationships between a and b as equations.

EQUATION 1

We know one number is four times the other:

$$4a = b$$

EQUATION 2

We know the product of the numbers is 64:

$$ab = 64$$

Step 3: Solve the simultaneous equations.

Substitute Equation 1 into Equation 2 to find a :

$$ab = 64$$

$$a(4a) = 64$$

$$4a^2 = 64$$

$$a^2 = 16$$

$$a = \pm 4$$

We know the values are positive integers, so $a = 4$.

Substitute $a = 4$ into Equation 1:

$$4a = b$$

$$4(4) = b$$

$$\mathbf{b = 16}$$

Marge thought of the numbers 4 and 16.



Guided Example

A lawn is a rectangular shape and has a length twice as long as its width. The area of the lawn is 98 m^2 . What is the perimeter of the lawn?

Step 1: Label the unknown length and width as letters.

Step 2: Create an equation using the information in the question about the size and area of the lawn.

Step 3: Solve the equation and find the value of x . Substitute x into the equations in Step 1 to find the length and width. Then, find the perimeter of the lawn.



7. Polly thinks of a number. She doubles the number and adds six.

Queenie thinks of a different number. She multiplies the number by eight and subtracts six.

Polly and Queenie both end on the same number. The number Polly starts with is twice Queenie's.

Use the information to find what number Polly and Queenie started with.

8. Kelly and Sam take their 2 children to play crazy golf. The total cost is £33. Billy takes his 3 children to play crazy golf and the total cost is £27.50. Calculate the price of a child's ticket and an adult's ticket.

