

GCSE Maths - Algebra

Nth term

Worksheet

WORKED SOLUTIONS

This worksheet will show you how to work out different types of nth term questions. Each section contains a worked example, a question with hints and then questions for you to work through on your own.

This work by PMT Education is licensed under CC BY-NC-ND 4.0











Section A

Worked Example

Find the nth term of the sequence 7, 10, 13, 16, 19, ...

Step 1: Find the term-by-term difference.

For the sequence 7, 10, 13, 16, 19, ... the term-by-term difference is 3.

Step 2: Use the term-by-term difference to make an estimate for the nth term.

If the nth term was 3n then the sequence would be 3, 6, 9, 12, 15, ...

Step 3: Compare the estimate and work out the difference between the sequences generated. Use the difference to find the formula for the nth term.

n	1	2	3	4	5
3n	3	6	9	12	15
3n+4	7	10	13	16	19

Comparing the original sequence with the sequence with nth term 3n, the difference between each term is +4. So, the nth term of the required sequence is 3n + 4.

Guided Example

Find the nth term of the sequence 2, 9, 16, 23, 30, ...

Step 1: Find the term-by-term difference.

Step 2: Use the term-by-term difference to make an estimate for the nth term.

Step 3: Compare the estimate and work out the difference between the sequences generated. Use the difference to find the formula for the nth term:

n	1	2	3	4	5
7n	7	14	24	28	35
7n-5	2	9	16	23	30

The original sequence with the sequence of the nth term has a difference of $-5 \cdot 50$, the nth term of the required sequence is 7n-5.











If you get stuck, look back at the worked and guided examples.

1. Find the nth term of the following sequences:

a) 0, 4, 8, 12, 16, ...

The term-by-term difference is 4.

If the nth term is 4n, the sequence would be 4,8,12,16,20

η	l l	2	3	¥	5
4n	4	8	12	16	20
4n-4	0	4	8	12	16

Since the difference between the 4n sequence and the original sequence is -4, the nth term of the required sequence is 4n-4.

b) -5, -3, -1, 1, 3, ...

The term-by-term difference is 2. If the 11th term is 2n, the sequence would be 2.4,6.8.10

η	ı	2	3	¥	5
2n	2	4	6	8	10
2n-7	-9	- 3	-1	ı.	3

Since the difference between the 2n sequence and the original sequence is -7, the nth term of the required sequence is 2n-7.

c) -1, -5, -9, -13, -17, ...

The term-by-term difference is -4 .

If the nth term is -4n, the sequence would be -4, -8, -12, -16, -20

d) 0, -13, -26, -39, -52, ...

The term-by-term difference is - 13

If the nth term is -13n, the sequena would be -13.-26.-39.-52.-65

e) 1.1, 2.6, 4.1, 5.6, 7.1, ...

The term-by-term difference is 1.5

If the nth term is 1.5n, the sequence would be 1.5, 3.0, 4.5, 6.0, 7.5

η	1	2	3	¥	5
-4n	-4	-8	-12	-16	-20
-41+3	-1	-5	-9	-13	-17

Since the difference between the -4n sequence and the original sequence is +3, the nth term of the required sequence is -4n+3

η	ı	2	3	¥	5
-13 n	-13	-26	-39	-52	-65
-13nt13	0	-13	-26	- 39	-52

Since the difference between the -13n sequence and the original sequence is +13, the nth term of the required sequence is -13n + 13

h	ı	2	3	¥	5
1.5n	1.5	3-0	4.5	6.0	7.5
1.5n-0.4	14	2.6	4.1	5.6	7-1

Sina the difference between the 2 sequences is -0.4, the nth term of the required sequence is 1.5n-0.4.











Section B

Worked Example

For the nth term 4n + 1, give the first 5 terms and the 90th term of the sequence

Step 1: Find the first five terms by substituting n = 1, 2, 3, 4, 5 into the nth term formula.

For
$$n = 1$$
: $4(1) + 1 = 5$

For
$$n = 2$$
: $4(2) + 1 = 9$

For
$$n = 3$$
: $4(3) + 1 = 13$

For
$$n = 4$$
: $4(4) + 1 = 17$

For
$$n = 5$$
: $4(5) + 1 = 21$

So, the first 5 terms are **5, 9, 13, 17, 21**.

Step 2: Find the 90th term by substituting n = 90 into the nth term formula.

For
$$n = 90$$
: $4(90) + 1 = 361$.

So, the 90th term is 361.

Guided Example

For the nth term 3n - 8, give the first 5 terms and the 90th term of the sequence

Step 1: Find the first five terms by substituting n = 1, 2, 3, 4, 5 into the nth term formula.

$$n=1 \rightarrow 3(1)-8 = 3-8 = -5$$

 $n=2 \rightarrow 3(2)-8 = 6-8 = -2$
 $n=3 \rightarrow 3(3)-8 = 9-8 = 1$
 $n=4 \rightarrow 3(4)-8 = 12-8 = 4$
 $n=5 \rightarrow 3(5)-8 = 15-8 = 7$

Step 2: Find the 90th term by substituting n = 90 into the nth term formula.

$$n=90 \rightarrow 3(90)-8 = 270-8 = 262$$











If you get stuck, look back at the worked and guided examples.

- 2. For each of the following nth terms, give the first 5 terms and the 90th term of the sequence:
- a) -6n + 4

$$\begin{aligned}
 & n=1 \implies -6(1)+4 = -6+4 = -2 \\
 & n=2 \implies -6(2)+4 = -12+4 = -8 \\
 & n=3 \implies -6(3)+4 = -18+4 = -14 \\
 & n=4 \implies -6(4)+4 = -24+4 = -20 \\
 & n=5 \implies -6(5)+4 = -30+4 = -26
 \end{aligned}$$

The first 5 ferms are :

$$n = 90 \rightarrow -6(90) + 4 = -540 + 4 = -536$$

The 90th ferm of the sequence is -536.

b) 42n

The first 5 terms are:

$$42,84,126,168,210$$
 $n=90 \rightarrow 42(90) = 3780$

The 90 th term of the sequence is 3780.

c) 13n - 1.5

$$N=1 \rightarrow 13(1)-1.5 = 13-1.5 = 11.5$$

$$N=2 \rightarrow 13(2)-1.5 = 26-1.5 = 24.5$$

$$N=3 \rightarrow 13(3)-1.5 = 39-1.5 = 37.5$$

$$N=4 \rightarrow 13(4)-1.5 = 52-1.5 = 50.5$$

$$N=5 \rightarrow 13(5)-1.5 = 65-1.5 = 63.5$$

The first 5 terms one :

$$n = 90 \rightarrow 13(90) - 1.5 = 1170 - 1.5$$

= 1168.5

The 90th term of the sequence is 1168.5

d) -9n - 2

$$\begin{aligned}
 & N=1 \longrightarrow -9(1)^{-2} = -9^{-2} = -11 \\
 & n-2 \longrightarrow -9(2)^{-2} = -18^{-2} = -20 \\
 & N=3 \longrightarrow -9(3)^{-2} = -27^{-2} = -29 \times \frac{90}{2} \\
 & n=4 \longrightarrow -9(4)^{-2} = -36^{-2} = -38 \longrightarrow \frac{810}{2} \\
 & N=5 \longrightarrow -9(5)^{-2} = -45^{-2} = -47
 \end{aligned}$$

$$N = 90 \Rightarrow -9(90) - 2 = -810 - 2$$
$$= -812$$

The 90th ferm of the sequence is - 812.

The first 5 terms are -11, -20, -29, -38, -47



×90

1170



90

-810





Section C

Worked Example

Calculate the difference between the 13th term and the 25th term of the following sequence: 2, 6, 10, 14, 18, ...

Step 1: Find the nth term of the given sequence.

For the sequence 2, 6, 10, 14, 18, ... the term-by-term difference is +4. If the nth term was 4n then the sequence would be 4, 8, 12, 16, 20, ...

Comparing the original sequence with the sequence with nth term 4n, we see that the difference between each term is -2. So, the nth term of the required sequence is 4n - 2.

n	1	2	3	4	5
4n	4	8	12	16	20
4n-2	2	6	10	14	18

Step 2: Find the 13th and 25th terms.

For
$$n = 13$$
: $4(13) - 2 = 50$
For $n = 25$: $4(25) - 2 = 98$

Step 3: Find the difference between the two.

The difference between the 13th and 25th term is 98 - 50 = 48.

Guided Example

Calculate the difference between the 19th term and the 61st term of the following sequence: -4, -7, -10, -13, -16, ...

Step 1: Find the nth term of the given sequence.

The term by term difference is -3. If the nth term is -3n, then the sequence would be -3, -6, -9, -12, -15. The difference between this sequence with the original sequence is -1. Hence, the nth term is -3n-1.

n	1	2	3	4	5
- 3h	- 3	-6	-9	-12	- 15
-311-1	-4	-7	-10	- 13	-16

Step 2: Find the 19th and 61st terms.

$$n = 19 \rightarrow -3(19) - 1 = -57 - 1 = -58$$

$$n = 61 \rightarrow -3(61) - 1 = -183 - 1 = -184$$

$$-183$$

Step 3: Find the difference between the two terms.

$$-184 - (-58) = -126 + \frac{58}{-126}$$











If you get stuck, look back at the worked and guided examples.

3. Calculate the difference between the 82nd term and the 131st term of the following sequence: 2, -3, -8, -13, -18, ...

Identify the nth term: Term by term difference: - 5 sequence for -5n = -5, -10, -15, -20, -25 The nfh term = -5n+7

ŋ	l l	2	3	¥	5
-5n	-5	-10	-15	-20	-25
-Sn+7	2	- 3	-8	-13	-18

Find the 82nd and 1315t ferm:

$$n=82 \rightarrow -5(82)+7 = -410+7 = -403$$

 $n=131 \rightarrow -5(131)+7 = -655+7 = -648$

Find the difference:
$$-648 - (-403) = -648 + 403 = -245$$

4. Calculate the difference between the 49th term and the 89th term of the following sequence: -3, 6, 15, 24, 33, ...

Identify the nth term:

Term by term difference: 9 Sequence for 9n = 9,18,27,36,45

n	ı	2	3	¥	5
9n	9	18	27	36	45
9n-12	-3	6	15	24	33

The nth term = 9n - 12

8 49 Find the 49th term and the 89th ferm: $n = 49 \rightarrow 9(49) - 12 = 441 - 12 = 429$ $n = 89 \rightarrow 9(89) - 12 = 801 - 12 = 789$ Calculate the difference 801 789-429 = 360 <

5. Calculate the difference between the 23rd term and the 91st term of the following sequence: 5.5, 8, 10.5, 13, 15.5, ...

Identify the nth term: Term by term difference: 2.5

η	- I	2	3	Ч	5
2.5n	2.5	5.0	7.5	10.0	12.5
2.5n+3	5.5	8.0	10-5	13.0	15.5

Sequence for 2.5n: 2.5,5,7.5,10,12.5 The nth term = 2.5 nt 3

Find the 23rd term and the 91st term:	23 X 2.5	91 * 25
$n = 23 \rightarrow 2.5(23) + 3 = 57.5 + 3 = 60.5$	115	455
$n = 91 \rightarrow 2.5(91) + 3 = 227.5 + 3 = 230.5$	46	182
Calculate the difference	<u>575</u>	217.5
230.5 - 60.6 = 170		











Section D

Worked Example

Is 194 a term in the sequence 7, 13, 19, 25, 31, ... ?

Step 1: Find the nth term of the given sequence.

For the sequence 7, 13, 19, 25, 31, ... the term-by-term difference is +6. If the nth term was 6n then the sequence would be 6, 12, 18, 24, 30, ...

Comparing the original sequence with the sequence with nth term 6n, we see that the difference between each term is +1. So, the nth term of the required sequence is 6n + 1.

n	1	2	3	4	5
6n	6	12	18	24	30
6n+1	7	13	19	25	31

Step 2: Determine if the given term belongs to the sequence with the above nth term.

194 is a term in the above sequence if there exists a positive integer n where 6n + 1 = 194. So, we need to solve this equation:

$$6n + 1 = 194$$

$$6n = 193$$

$$n = \frac{193}{6} = 32.1666 \dots$$

Since n is not an integer, 194 is **not** a term in the given sequence.

Guided Example

Is -2361 a term in the sequence -1, -3, -5, -7, -9, ... ?

Step 1: Find the nth term of the given sequence.

Term by term difference:
$$-2$$

Sequence for $-2n : -2, -4, -6, -8, -10$

nth term : $-2n+1$

n	1	2	3	4	5
- 2n	- 2	- 4	- 6	- 8	-10
-2n+1	-1	-3	- 5	- 7	-9

Step 2: Determine if the given term belongs to the sequence with the above nth term.

$$-1 \left(-2n+1 = -2361 \right)$$

$$-2n = -2362$$

$$-2361 belongs to$$

$$+-2 \left(+ n = 1181 \right)$$
The given sequence.











If you get stuck, look back at the worked and guided examples.

6. Is 925 a term in the sequence -5, -1, 3, 7, 11, ...?

Find the nth term:
Term by term difference: 4

Sequence for 4n = 4,8,12,16,20

The nth term = 4n-9

η	l l	2	3	¥	5
4n	4	8	12	16	20
41-9	-5	-1	3	7	U

Determine of the ferm belongs to the sequence:

$$49 \left(\frac{4n-9}{4n} = 925\right)$$

 $49 \left(\frac{4n-9}{4n} = 934\right)$
 $40 \left(\frac{4n-9}{4n} = 233.5\right)$

The term 925 does not belong in the given sequence.

7. Is 1389 a term in the sequence 13, 29, 45, 61, 77, ...?

Term by term difference: 16 Sequence for 16n = 16, 32, 48,64,80 The nth term: 16n-3

n	L	2	3	ч	5
16 n	16	32	48	64	80
l6n - 3	13	29	45	61	77

Determine of the ferm belongs to the sequence:

$$+3 \left(\begin{array}{c} 16 \text{ n} - 3 = 1389 \\ 16 \text{ n} = 1392 \\ \Rightarrow 16 \end{array} \right) = 87$$

$$\frac{128}{112}$$

$$\frac{128}{112}$$

The term 1389 belongs in the given sequence.

8. Is -313 a term in the sequence 10, 8, 6, 4, 2, ...?

Term by term difference: -2Sequence for -2n = -2, -4, -6, -8, -10The nth term : -2n+12

η	ı	2	3	¥	5
-2n	- 2	- 4	-6	-8	-10
-2n+12	10	8	6	Ч	2

Determine of the ferm belongs to the sequence:

$$-12 \left(-2n + 12 = -313 \right)$$

$$-2n = -325$$

$$\div -2 \left(-2n + 12 = -313 \right)$$

$$162.5$$

$$\frac{162.5}{12}$$

$$\frac{162.5}{12}$$

The term - 313 does not belong in the given sequence.





Section E - Higher only

Worked Example 1

Find the nth term of the following quadratic sequence 3, 9, 19, 33, 51,

Step 1: Work out the differences between the terms. Write the differences so that they form a new linear sequence.

Sequence of differences: 6, 10, 14, 18, ...

Step 2: Use the term-by-term rule of the sequence of differences to find the coefficient of n^2 .

In the sequence of differences 6, 10, 14, 18, ..., the term-by-term rule is +4.

Since the original sequence is a quadratic sequence, it will have an n^2 term in the formula. The coefficient of n^2 is always half of the term-by-term rule of the sequence of differences. In this case, the term-by-term rule is +4 so the coefficient of n^2 will be 2.

Coefficient of n^2 : 2

Step 3: Compare the given sequence with the quadratic sequence $\underline{}$ using the coefficient of n^2 found in **Step 2.**

2n²	2	8	18	32	50
Sequence	3	9	19	33	51
Difference	+1	+1	+1	+1	+1

Step 4: Find the linear part of the quadratic nth term by finding the linear nth term of the new sequence of differences.

The new sequence of differences is 1, 1, 1, 1, 1, ... So, the linear nth term for the sequence of differences is simply +1 as each term in the sequence is the same.

Step 5: Find the nth term of the quadratic sequence by combining the linear nth term of the sequence of differences found in **Step 4** and the coefficient of n^2 found in **Step 2**.

The linear nth term for the sequence of differences was +1 and the coefficient of n^2 was found to be 2. So, the nth term for the quadratic sequence is

$$2n^2 + 1$$
.











Worked Example 2

Find the nth term of the following quadratic sequence -17, -30, -49, -74, -105

Step 1: Work out the differences between the terms. Write the differences so that they form a new linear sequence.

Sequence of differences: -13, -19, -25, -31, ...

Step 2: Use the term-by-term rule of the sequence of differences to find the coefficient of n^2 .

In the sequence of differences, the term-by-term rule is -6.

Since it is a quadratic sequence, it will have an n^2 term in the formula. The coefficient of n^2 is always half of the term-by-term rule of the sequence of differences. In this case, the term-by-term rule is -6 so the coefficient of n^2 will be -3.

Coefficient of n^2 : -3

Step 3: Compare the given sequence with the quadratic sequence $\underline{}$ using the coefficient of n^2 found in **Step 2**.

-3n ²	-3	-12	-27	-48	-75
Sequence	-17	-30	-49	-74	-105
Difference	-14	-18	-22	-26	-30

Step 4: Find the linear part of the quadratic nth term by finding the linear nth term of the new sequence of differences.

For the new sequence of differences -14, -18, -22, -26, -30, ... the term-by-term rule is -4. Comparing the sequence of differences with the sequence generated by the nth term -4n, there is a difference of -10 for each term. So, the nth term for the sequence of differences is -4n-10.

n	1	2	3	4	5
-4n	-4	-8	-12	-16	-20
-4n-10	-14	-18	-22	-26	-30

Step 5: Find the nth term of the quadratic sequence by combining the linear nth term of the sequence of differences found in **Step 4** and the coefficient of n^2 found in **Step 2**.

The linear nth term for the sequence of differences was -4n - 10 and the coefficient of n^2 was found to be -3. So, the nth term for the quadratic sequence is

$$-3n^2-4n-10$$
.











Guided Example

Find the nth term of the following quadratic sequence 5, 16, 33, 56, 85,

Step 1: Work out the differences between the terms. Write the differences so that they form a new linear sequence.

Sequence of difference: 11, 17,23,29

Step 2: Use the term-by-term rule of the sequence of differences to find the coefficient of n^2 .

The term by term rule of the sequence of differences
$$136$$
.
The wefficient of $n^2 = 6 \div 2 = 3$ (always half of the term by term rule)

Step 3: Compare the given sequence with the quadratic sequence $3n^2$ using the coefficient of n^2 found in Step 2.

<u>3</u> n ²	3	12	27	48	75
Sequence	5	16	33	56	85
Difference	2	4	6	8	10

Step 4: Find the linear part of the quadratic nth term by finding the linear nth term of the new sequence of differences.

η	ı	2	3	Ч	5
2n	2	4	6	8	lo
2n	2	4	6	8	10

The nth term for the sequence of differences: 2n

Step 5: Find the nth term of the quadratic sequence by combining linear nth term of the sequence of differences found in **Step 4** and the coefficient of n^2 found in **Step 2**.

$$3n^{2} + 2n$$











If you get stuck, look back at the worked and guided examples.

- 9. Find the nth term of the following quadratic sequences
- a) -10, -21, -40, -67, -102,

$$-10$$
 -21 -40 -67 -102 -11 -19 -27 -35

sequence of difference = -11, -19, -27, -35

The term-by-term rule = -8

The wefficient of $n^2 = -8 \div 2 = -4$ wefficient of n^2 is always half the term-by-term

rule

-4n2	-4	-16	-36	-64	-100
Sequence	-10	-21	-40	-67	-102
Diff	-6	-5	-4	-3	-2

The linear difference sequence: -6, -5, -4, -3, -2

The term -by-term rule is: 1

The Inth term sequence: 1, 2, 3, 4, 5

η	l	2	3	ч	5
ln	1	2	3	Ч	5
n-7	-6	-5	-4	- 3	-2

The 11th term for the sequence of differences: n-7

Combine linear nH term with wefficient of n2



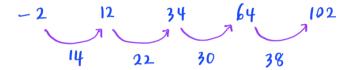








b) -2, 12, 34, 64, 102, ...



sequence of difference = 14, 22, 30, 38The term-by-term rule = 8 The wefficient of $n^2 = 8 \div 2 = 4$

4n2	4	16	36	64	100
Sequence	-2	12	34	64	102
Diff	- 6	-4	-2	0	2

The linear difference sequence: -6,-4,-2,0,2

The term -by-term rule is: 2

The 2n term sequence: 2,4,6,8,10

η	l	2	3	ų	5
2n	2	4	6	8	10
2n-8	-6	-4	- よ	Ø	2

The 11th term for the sequence of differences: 2n-8

Combine linear nH term with wefficient of n2







Section F - Higher only

Worked Example

For the nth term $4n^2 + 1$, give the first 5 terms and the 83rd term of the sequence.

Step 1: Find the first five terms by substituting n = 1, 2, 3, 4, 5 into the nth term formula.

For
$$n = 1$$
: $4(1)^2 + 1 = 5$

For
$$n = 2$$
: $4(2)^2 + 1 = 17$

For
$$n = 3$$
: $4(3)^2 + 1 = 37$

For
$$n = 4$$
: $4(4)^2 + 1 = 65$

For
$$n = 5$$
: $4(5)^2 + 1 = 101$

So, the first 5 terms are 5, 17, 37, 65, 101.

Step 2: Find the 83rd term by substituting n = 83 into the nth term formula.

For
$$n = 83$$
: $4(83)^2 + 1 = 27557$.

The 83rd term is 27557.

Guided Example

For the nth term $n^2 - 7$, give the first 5 terms and the 96th term of the sequence.

Step 1: Find the first five terms by substituting n = 1, 2, 3, 4, 5 into the nth term formula.

$$h=1 \longrightarrow (1)^2 - 7 = 1 - 7 = -6$$

$$n=2 \implies (2)^2-7 = 4-7 = -3$$

$$n=3 \rightarrow (3)^2-7 = 9-7=2$$

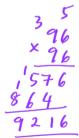
$$n=4 \rightarrow (4)^2-7 = 46-7 = 9$$

$$n=5 \rightarrow (5)^2 - 7 = 25 - 7 = 18$$

Step 2: Find the 96th term by substituting n = 96into the nth term formula.

$$n=96 \rightarrow (96)^2 - 7 = 9216 - 7$$

= 9209







If you get stuck, look back at the worked and guided examples.

- 10. For each of the following nth terms, give the first 5 terms and the 123rd term of the sequence:
- a) $-9n^2$ $h=1 \rightarrow -9(1)^2 = -9$ $n=2 \rightarrow -9(2)^2 = -9 \times 4 = -36$ $n = 3 \rightarrow -9 (3)^2 = -9 \times 9 = -81$ $n=4 \rightarrow -9(4)^2 = -9 \times 16 = -144$ 425 $n=5 \rightarrow -9(5)^2 = -9 \times 25 = -225 \leftarrow -\frac{1}{225}$

The first 5 terms are : -9, -36, -81, -144, -225 -136161 $n = 123 \rightarrow -9(123)^2 = -136161 \leftarrow$

The 123 rd term is - 136/61

b)
$$n^2 - 3n + 5$$

$$h=1 \longrightarrow (1)^{2}-3(1)+5 = 1-3+5 = 3$$

$$n=2 \longrightarrow (2)^{2}-3(2)+5 = 4-6+5 = 3$$

$$n=3 \longrightarrow (3)^{2}-3(3)+5 = 9-9+5 = 5$$

$$n=4 \longrightarrow (4)^{2}-3(4)+5 = 16-12+5 = 9$$

$$n=5 \longrightarrow (5)^{2}-3(5)+5 = 25-15+5 = 15$$

 $n = 123 \rightarrow (123)^2 - 3(123) + 5$ - 15129 - 369 + 5 = 14765

X 123

1369

2 46

15129

123

415129

x (-9)

The 123rd term is 14765

The first 5 terms are : 3, 3, 5, 9, 15

c)
$$-3.2n^2 + 9n + 5.1$$

$$h=1 \longrightarrow -3.2(1)^{2} + 9(1) + 5 \cdot 1 = 10.9$$

$$n=2 \longrightarrow -3.2(2)^{2} + 9(2) + 5 \cdot 1 = 10.3$$

$$n=3 \longrightarrow -3.2(3)^{2} + 9(3) + 5 \cdot 1 = 3.3$$

$$n=4 \longrightarrow -3.2(4)^{2} + 9(4) + 5 \cdot 1 = -10.1$$

$$n=5 \longrightarrow -3.2(5)^{2} + 9(5) + 5 \cdot 1 = -29.9$$

$$n = |23 \rightarrow -3.2(|23)^{2} + 9(|23)$$

$$+ 5 \cdot |$$

$$= -47300 \cdot 7$$

The 123rd term is -47300.7

The first 5 terms are : 10.9, 10.3, 3.3, -10.1, -29.9









Section G - Higher only

Worked Example

A sequence has an nth term of $2n^2 + 4n - 10$.

Work out which term in the sequence has a value of 116.

Step 1: To find the value of n for which the given term corresponds to, set the nth term equal to the given term in the sequence.

$$2n^2 + 4n - 10 = 116$$

Step 2: Solve the quadratic equation.

$$2n^{2} + 4n - 10 = 116$$

$$2n^{2} + 4n - 126 = 0$$

$$n^{2} + 2n - 63 = 0$$

$$(n - 7)(n + 9) = 0$$

$$n = 7 \text{ or } n = -9$$

Step 3: Select the value of n which is the non-negative integer. This n tells you which term in the sequence has the given value.

Since n must be a non-negative integer, 116 is the term in the sequence corresponding to n = 7 and so 116 is the **7th term** in the sequence.

Guided Example

A sequence has an nth term of $-4n^2 + 3$.

Work out which term in the sequence has a value of -61.

Step 1: To find the value of n for which the given term corresponds to, set the nth term equal to the given term in the sequence.

$$-4n^2+3=-61$$

Step 2: Solve the quadratic equation.

$$-3 \left(-4n^{2}+3=-61\right) + |64|$$

$$-3 \left(-4n^{2}+3=-64\right) + |64|$$

$$-4n^{2}=-64$$

$$-4n^{2}=-64$$

$$-9 \left(-4n^{2}+3=-64\right)$$

$$-$$

Step 3: Select the value of n which is the non-negative integer. This n tells you which term in the sequence has the given value.







If you get stuck, look back at the worked and guided examples.

11. A sequence has an nth term of $-5n^2 + 37n + 918$. Work out which term in the sequence has a value of 932.

$$-932 \begin{cases} -5n^{2} + 37n + 918 = 932 \\ -5n^{2} + 37n + 918 - 932 = 0 \end{cases}$$

$$-5n^{2} + 37n - 14 = 0$$

$$-5n^{2} + 37n - 14 = 0$$

$$5n^{2} - 37n + 14 = 0$$

$$5n - 3 = 0 \qquad or \qquad n - 7 = 0$$

$$n = \frac{2}{5}$$

$$n = 7$$

Choose n which is an integer

932 belongs to the 7th term in the sequence

12. A sequence has an nth term of $6n^2 - 64n - 150$. Work out which term in the sequence has a value of -128.

+128
$$(6n^2 - 64n - 150 = -128)$$

 $6n^2 - 64n - 150 + 128 = 0$
 $26n^2 - 64n - 22 = 0$
 $3n^2 - 32n - 11 = 0$
factorise $(3n+1)(n-11) = 0$
 $3n+1 = 0$ or $n-11 = 0$
 $n = -\frac{1}{3}$
choose n which is not a negative integer

-128 is the 11th term in the sequence







