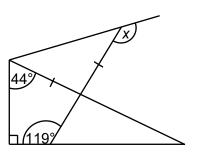
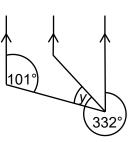
### Higher Check In – 8.03 Angles

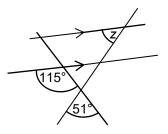
- 1. A regular polygon has an interior angle of 156°. How many sides does the polygon have?
- 2. Find angle x.



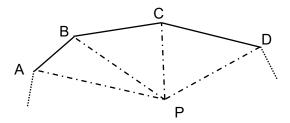
3. Find angle y.



4. Find angle z.



- 5. The interior angles of a polygon sum to 1620°. How many sides does the polygon have?
- 6. Point P is inside an *n*-sided polygon ABCD....



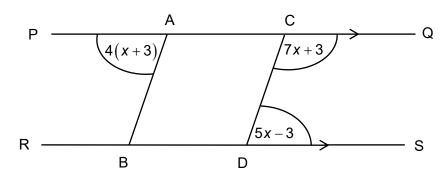
Use the diagram to show that the sum of the interior angles of a polygon can be given by this formula:

Sum of the interior angles = 180n - 360

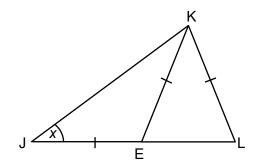




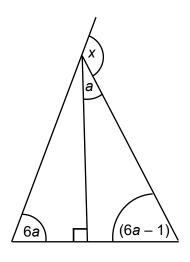
7. Prove that AB is parallel to CD.



8. Prove that angle JLK = 2x.



9. Find angle *x*.



10. The size of an exterior angle of a regular polygon is  $5x^{\circ}$  and the number of sides of this polygon is 8x. Find the size of the interior angle.

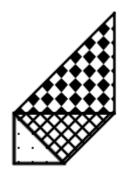






#### Extension

A spiral pattern is made using right-angled isosceles triangles as shown in the diagram below. The lengths of the sides of the first triangle are 1, 1,  $\sqrt{2}$ .



How many triangles are needed to complete a full rotation, and what are the sizes of each triangle in the pattern?





### Answers

- 1. 15 sides
- 2.  $x = 126.5^{\circ}$
- 3.  $y = 51^{\circ}$
- 4.  $z = 64^{\circ}$
- 5. 11 sides
- 6. *n* triangles each with sum of interior angles  $180^{\circ} = 180n$ Sum of angles at point P =  $360^{\circ}$ Therefore sum of interior angles is 180n - 360
- 7.  $(7x+3)+(5x-3) = 180^{\circ}$  (interior angles add to  $180^{\circ}$ ) which gives  $x = 15^{\circ}$ . Angle PAB =  $4(15+3) = 72^{\circ}$  and angle ACD =  $180 - 7 \times 15 + 3 = 72^{\circ}$ . AB is parallel to CD because corresponding angles are equal oe.
- 8. Angle JKE = x (base angles of an isosceles triangle are equal). Angle JEK = 180 - 2x (angle sum of a triangle is  $180^{\circ}$ ). Angle LEK = 2x (angles on a straight line). Angle JLK = LEK = 2x (base angles of an isosceles triangle are equal).
- 9.  $x = 155^{\circ}$
- 10. 165°

#### Extension

Since the angles are 45° there will be  $\frac{360}{45} = 8$  triangles to complete the spiral.

Triangle	Side Lengths
1	1, 1, √2
2	$\sqrt{2}, \sqrt{2}, 2$
3	2, 2, 2√2
4	$2\sqrt{2}, 2\sqrt{2}, 4$
5	4, 4, 4\sqrt{2}
6	$4\sqrt{2}, 4\sqrt{2}, 8$
7	8, 8, 8√2
8	8√2, 8√2, 16





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Assessment Objective	Qu.	Торіс	R	Α	G
AO1	1	Use the sum of the exterior angles of a polygon is $360^\circ$			
AO1	2	Apply angle properties to find angles in a rectilinear figure			
AO1	3	Apply angle properties about parallel lines			
AO1	4	Apply angle properties to find angles in a rectilinear figure			
AO1	5	Use the sum of the interior angles of a polygon, $180(n-2)$			
AO2	6	Use angle properties to justify the sum of the interior angles of a polygon			
AO2	7	Apply angle properties in a more formal proof of geometrical results			
AO2	8	Apply angle properties in a more formal proof of geometrical results			
AO3	9	Use angle properties to solve a triangle problem			
AO3	10	Use angle properties to solve a polygon problem			

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