

1	$\begin{aligned} &(4n^2+2n+2n+1) \\ &- (2n+1)= \\ &4n^2+4n+1-2n-1 \\ &= 4n^2 + 2n \\ &= 2n(2n + 1) \end{aligned}$	proof (supported)	<p>M1 for 3 out of 4 terms correct in the expansion of <math>(2n + 1)^2</math> or <math>(2n + 1)(2n + 1) - 1</math></p> <p>P1 for <math>4n^2 + 2n</math> or equivalent expression in factorised form</p> <p>C1 for convincing statement using <math>2n(2n + 1)</math> or <math>2(2n^2 + n)</math> or <math>4n^2 + 2n</math> to prove the result</p>
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2		$2(2n-3)$  even	<p>C1 correct expansion of brackets to give at least 3 terms from <math>n^2-2n-2n+4</math></p> <p>C1 arrives at <math>n^2-2n^2+4n-4</math> oe</p> <p>C1 reduces to <math>2(2n-3)</math> or <math>4n - 6</math></p> <p>C1 for conclusion e.g. <math>2(2n-3)</math> always even, <math>4n - 6</math> is always even since both are even numbers, they are multiples of 2.</p>
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3			<p>M1 for the start of a method to convert 0.22... to a fraction, eg <math>10y = 2.22..</math> or <math>(y=) \frac{2}{9}</math></p> <p>M1 for the start of a method to convert 0.13636... to a fraction,  <math>10x = 1.3636..</math> or <math>100x = 13.6363... </math> or <math>1000x = 136.3636..</math> or <math>(x=) \frac{13.5}{99}</math> or <math>(x=) \frac{135}{990}</math></p> <p>C1 for correct arithmetic and concluding the proof</p> <p>OR</p> <p>M1 for <math>0.1\dot{3}\dot{6} \times 0.2 = 0.0\dot{3}</math> (<math>= z</math>)</p> <p>M1 for complete method to find two appropriate recurring decimals the difference of which is a rational number, eg. <math>100z = 3.0303... (z =) 0.0303... </math> or <math>\frac{3}{99}</math></p> <p>C1 for correct arithmetic and concluding the proof</p>
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4		Proof to reach $\frac{24}{55}$	<p>M1 for <math>100x = 43.636... (43.\dot{6}\dot{3})</math>  or <math>10x = 4.3636... (4.3\dot{6})</math> and <math>1000x = 436.36... (436.\dot{3}\dot{6})</math></p> <p>M1 (dep) for finding difference that would lead to a terminating decimal</p> <p>A1 for completing algebra to reach <math>\frac{24}{55}</math></p>
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5		Completes proof	<p>M1 Expands both expressions  eg <math>\frac{1}{2}(n^2 + n + n^2 + n + 2n + 2)</math> or <math>n^2 + n</math> and <math>n^2 + n + 2n + 2</math>  or factorises <math>\frac{1}{2}(n+1)(n+n+2)</math></p> <p>C1 Completes proof with explanation and reference to <math>(n+1)^2</math></p>
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6	Statement supported by algebra	<p>B1 writing a general expression for an odd number eg <math>2n+1</math></p> <p>M1 (dep) for expanding ("odd number")<sup>2</sup> with at least 3 out of 4 correct terms</p> <p>A1 for correct simplified expansion, eg <math>4n^2 + 4n + 1</math></p> <p>C1 (dep A1) for a concluding statement eg <math>4(n^2 + n) + 1</math> (is one more than a multiple of 4)</p>	<p>Could be <math>2n - 1, 2n + 3</math>, etc</p> <p>Note that <math>4n^2 + 4n + 2</math> or <math>2n^2 + 4n + 1</math> in expansion of <math>(2n + 1)^2</math> is to be regarded as 3 correct terms</p>
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7	Proof shown	C2            C1	<p>for complete argument, eg <math>n(n - 1)</math> is the product of two consecutive integers and must be even as either <math>n</math> or <math>n - 1</math> must be even</p> <p><b>or</b> gives correct reasoning for <math>n</math> odd <b>and</b> <math>n</math> even  <math>n</math> odd: odd <math>\times</math> odd = odd and odd <math>-</math> odd = even  <math>n</math> even: even <math>\times</math> even = even and even <math>-</math> even = even</p> <p><b>or</b> <math>n</math> odd: <math>(2n + 1)^2 - (2n + 1) = 4n^2 + 2n = 2(2n^2 + n)</math>  <math>n</math> even: <math>(2n)^2 - (2n) = 4n^2 - 2n = 2(2n^2 - n)</math></p> <p>for factorising, eg <math>n(n - 1)</math></p> <p><b>OR</b> gives correct reasoning for <math>n</math> odd <b>or</b> <math>n</math> even</p> <p><b>OR</b> gives a partial explanation using <math>n</math> odd <b>and</b> <math>n</math> even, eg odd<sup>2</sup> - odd = even and even<sup>2</sup> - even = even)</p>	
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8	Proof	M1   M1  A1	<p>for correct expressions for two consecutive even numbers eg <math>2n</math> and <math>2n + 2</math></p> <p>(dep M1) for expanding both expressions with at least one expansion fully correct eg <math>4n^2</math> and <math>4n^2 + 4n + 4n + 4</math>  <b>or</b> for factorising both terms and intention to square correctly eg <math>(2n)^2</math> and <math>2^2(n + 1)^2</math></p> <p>complete proof</p>	<p><math>(2n)^2 + (2n + 2)^2</math>  <math>= 4n^2 + 4n^2 + 8n + 4</math>  <math>= 8n^2 + 8n + 4 = 4(2n^2 + 2n + 1)</math></p> <p><b>Or</b>  <math>(2n)^2 + (2n + 2)^2</math>  <math>= 4n^2 + 4n^2 + 8n + 4</math>  <math>= 8n^2 + 8n + 4 = 4(2n^2 + 2n + 1)</math></p> <p><b>Or</b>  <math>(2n)^2 + (2n + 2)^2</math>  <math>= 4(n)^2 + 4(n + 1)^2</math>  <math>= 4(n^2 + (n + 1)^2)</math></p>
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