

1. The table shows some values of x and y that satisfy the equation $y = a \cos x^\circ + b$

x	0	30	60	90	120	150	180
y	3	$1 + \sqrt{3}$	2	1	0	$1 - \sqrt{3}$	-1

Find the value of y when $x = 45$

$$y = a \cos x^\circ + b$$

When $x = 0$
 $y = 3$

$$3 = a \times \cos 0^\circ + b \quad \cos 0^\circ = 1$$

$$3 = a \times 1 + b$$

$$3 = a + b$$

$$3 = a + 1$$

$$-1 \quad -1$$

$$2 = a$$

When $x = 90$
 $y = 1$

$$1 = a \times \cos 90^\circ + b$$

$$1 = a \times 0 + b$$

$$1 = b$$

When $x = 45$

$$y = 2 \times \cos 45^\circ + 1$$

$$y = 2 \times \frac{\sqrt{2}}{2} + 1$$

$$y = \sqrt{2} + 1$$

$\sqrt{2} + 1$ ✓

(Total for Question 1 is 4 marks)

$$\frac{6 - \sqrt{8}}{\sqrt{2} - 1} \times \frac{\sqrt{2} + 1}{\sqrt{2} + 1}$$

$$= \frac{(6 - \sqrt{8})(\sqrt{2} + 1)}{(\sqrt{2} - 1)(\sqrt{2} + 1)}$$

$$= \frac{6\sqrt{2} + 6 - \sqrt{8} \times 2 - \sqrt{8}}{2 + \sqrt{2} - \sqrt{2} - 1}$$

$$= \frac{3\sqrt{2} + 2}{1}$$

$$= 2 + 3\sqrt{2}$$

Numerator

$$6\sqrt{2} + 6 - \sqrt{8} \times 2 - \sqrt{8}$$

$$6\sqrt{2} + 6 - \sqrt{16} - \sqrt{8}$$

$$6\sqrt{2} + 6 - 4 - \sqrt{8}$$

$$6\sqrt{2} + 2 - \sqrt{8}$$

$$6\sqrt{2} + 2 - \sqrt{2} \times 2 \times 2$$

$$6\sqrt{2} + 2 - \sqrt{2} \times \sqrt{2} \times \sqrt{2}$$

$$6\sqrt{2} + 2 - 3\sqrt{2}$$

$$3\sqrt{2} + 2$$

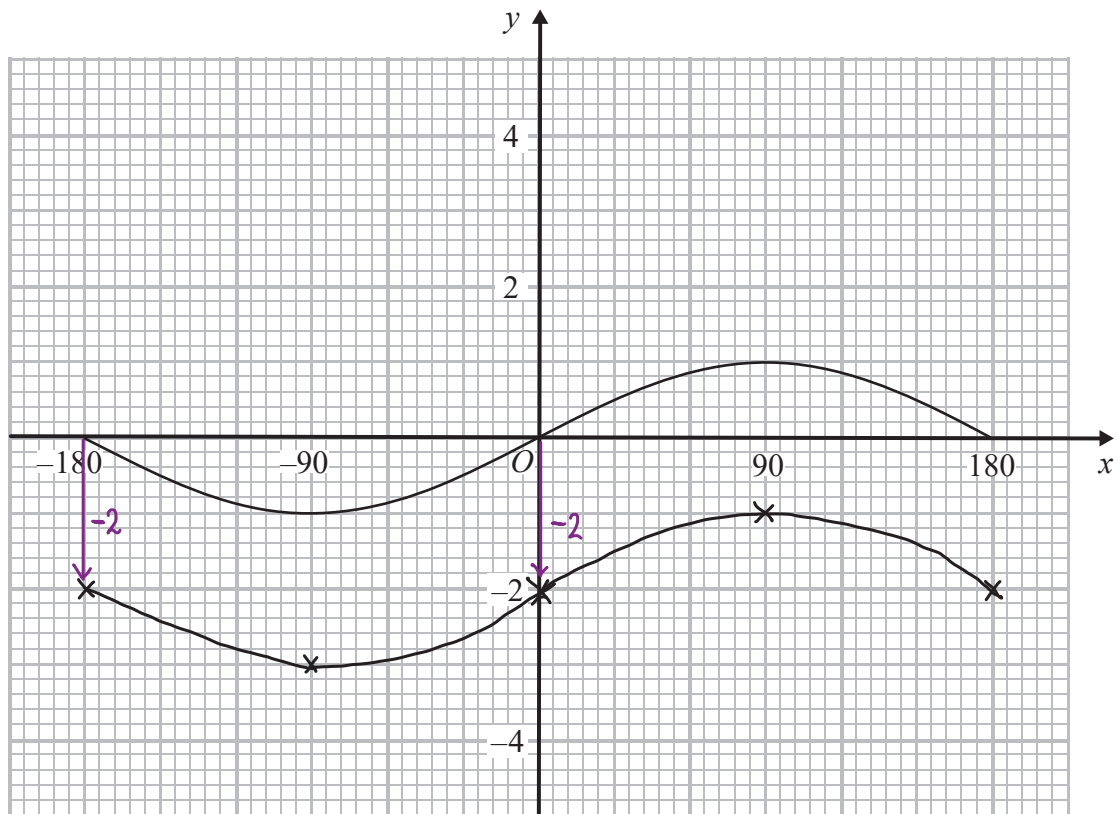
Denominator

$$2 + \sqrt{2} - \sqrt{2} - 1$$

$$2 - 1$$

$$= 1$$

2. Here is the graph of $y = \sin x^\circ$ for $-180 \leq x \leq 180$



On the grid, sketch the graph of $y = \sin x^\circ - 2$ for $-180 \leq x \leq 180$

$$y = (\sin x) - 2$$

← Shifts in y are as expected

∴ a shift of -2 in the y direction

- move the curve down by 2

(Total for Question is 2 marks)