



GCSE (9-1) Mathematics

J560/06 Paper 6 (Higher Tier)

Monday 12 November 2018 – Morning

Time allowed: 1 hour 30 minutes

You may use:

- · a scientific or graphical calculator
- geometrical instruments
- tracing paper

Model Solutions



First name	
Last name	
Centre number	Candidate number

INSTRUCTIONS

- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number and candidate number.
- · Answer all the questions.
- Read each question carefully before you start to write your answer.
- Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided. If additional space is required, use the lined page(s) at the end of this booklet. The question number(s) must be clearly shown.
- Do **not** write in the barcodes.

INFORMATION

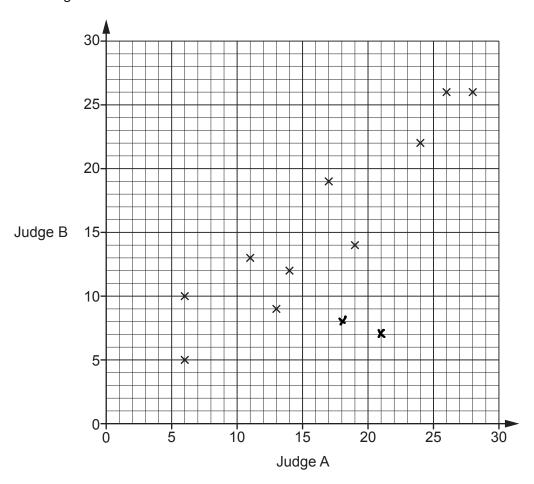
- The total mark for this paper is 100.
- The marks for each question are shown in brackets [].
- Use the π button on your calculator or take π to be 3.142 unless the question says otherwise.
- · This document consists of 24 pages.



2

Answer all the questions.

1 In a dance competition, two judges each award scores out of 30. The scatter diagram shows the scores awarded to the first 10 dancers.



(a) Here are the scores for the next two dancers.

Judge A	21	7
Judge B	18	8

Plot their scores on the scatter diagram.

[1]

(b) Dancers who are awarded a score of more than 20 by both judges receive a medal.

For the 12 dancers, express the ratio of medal winners to non-medal winners in its simplest form.

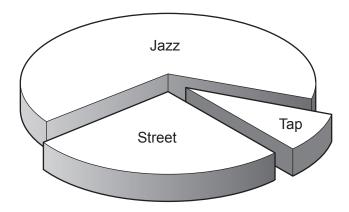
3 people score 20+ ,10m both judges

medal: no medal

(b)[3]

(c) This chart shows the types of dance performed by the 12 dancers.

3 performed a street dance, 8 performed a jazz dance and 1 performed a tap dance.



Why is this diagram misleading?

the wedges at the front look bigger than they actually are , due to the angle.

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2 The police record the speed of vehicles passing a speed checkpoint. The speeds are recorded in the table below.

Speed (s mph)	Number of vehicles(f)	midpoint of s	fz
0 < s ≤ 20	5	10(2)	50
20 < s ≤ 40	8	<i>30</i>	240
40 < s ≤ 50	37	45	1665
50 < s ≤ 60	47	<i>5</i> 5	2585
60 < s ≤ 80	3	70	20

(a) Calculate an estimate of the mean speed of the vehicles.

means sum of
$$\frac{50+240+1665+2585+210}{5+8+37+47+3}$$

$$= \frac{4750}{100} = 4.75$$

	4.75	
(a)	mph mph	[4

(b) Explain why it is not possible to use the information from this table to calculate the **exact** value of the mean speed.

the exact speed of each vehicle is not recorded, instead they are classified into groups

.. L .

3 A newborn baby has an approximate mass of 3.5 kilograms.

A human cell has an approximate mass of 2.7×10^{-11} grams.

Use these values to estimate the number of human cells in a newborn baby. Give your answer in standard form, correct to 2 significant figures.

$$3.5 \text{ kg} = 3500 \text{ g}$$

$$1 \quad \text{cell} = 2.7 \times 10^{-11} \text{ g}$$

$$1.296 \times 10^{14} = 3500 \text{ g}$$

$$1.296 \times 10^{14} = 3500 \text{ g}$$

$$1.3 \times 10^{14} \text{ (2sf)}$$

$$1.3 \times 10^{14} \text{ (2sf)}$$

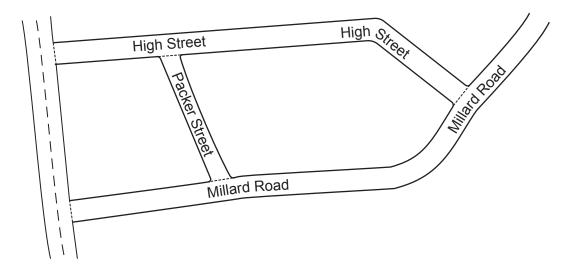
1-3 × 10 14 [5]

4 Use the symbols <, \le , =, >, or \ge to complete this statement.

If
$$x = 4.7$$
, truncated to 1 decimal place, then $4.7 \dots 4.8$ [2]

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5 This map shows part of a village.



Neil knows that Packer Street is 180 m long in real life.

(a) Neil measures the map.

He says

Packer Street is 3.5 cm long. High Street is 11.2 cm long.

Therefore, I calculate that High Street is 576 m long in real life.

Use Neil's figures to show that the answer to his calculation is correct.

[3]

$$x^{\frac{11\cdot2}{3\cdot5}=3\cdot2}$$
 3 · 5 cm = 180 m
 $11\cdot2$ cm = 576 m [3·2×180=576]

(b) Jodie measures the same map.

She says

I think Packer Street is longer than Neil's measurement of 3.5 cm. Therefore, High Street must be longer than 576 m in real life.

Is Jodie's reasoning correct? Show how you decide.

If Neil's measurement is too short, then 180m is in fact represented by a longer length on the map. This means the scale is changed, and the actual length of High St must be shorter. Hence, Jodie is incomect.

.....[2]

(c) On another map, Packer Street is 2.4 cm long.

Express the scale of this map in the form 1:n.

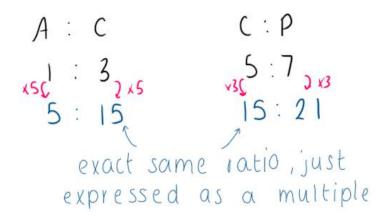
$$2.4 \text{ cm} = 180 \text{ m}$$
 convert to
 $2.4 \text{ cm} = 18000 \text{ cm}$ turn into ratio
 $2.4 : 18000$ $= 2.4$
 $1 : 7500$

(c) 1: 7500 [2]

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In a box of mixed nuts, the total number of almonds, cashews and peanuts is 1025. The ratio of almonds to cashews is 1 : 3. The ratio of cashews to peanuts is 5 : 7.

Calculate the number of cashews in the box.



number of cashews expressed as 15 parts, so can combine ratios.

$$A : C : P$$
 $5 : 15 : 21$
 $6+15+21 = 41$
 $1025 = 25$
 41
 $10. cashews = 15 \times 25$
 $= 375$

375

7 The probability that any postcard posted in Portugal on Monday is delivered to the UK within a week is 0.62.

The probability that any postcard posted in Portugal on Friday is delivered to the UK within a week is 0.41.

(a) Anna is on holiday in Portugal.

She posts 15 postcards to the UK on Monday.

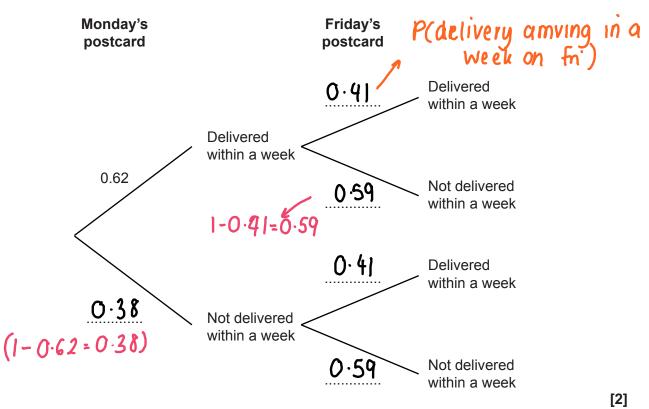
How many of her postcards can she expect to be delivered within a week?

(b) Sergio is in Portugal.

He posts one postcard to the UK on Monday. He posts another postcard to the UK on Friday.

The poole allower poolears to the off of the age.

(i) Complete the probability tree to show the possible outcomes for the postcards.

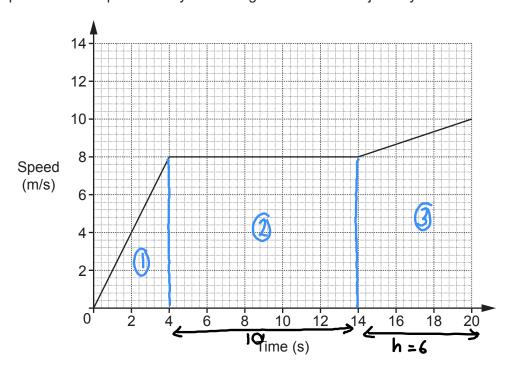


(ii) Calculate the probability that only one of Sergio's postcards is delivered within a week.

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8 The graph shows the speed of a cyclist during 20 seconds of a journey.



- (a) Find the acceleration of the cyclist
 - (i) for the first 4 seconds \bigwedge means change in

$$a = \underbrace{\Delta V}_{t}$$

$$= \underbrace{A}_{t} = 2$$

(a)(i) _____m/s² [2]

(ii) between 4 seconds and 14 seconds.

(ii)m/s² [1]

(b) Work out the distance travelled by the cyclist during the 20 seconds.

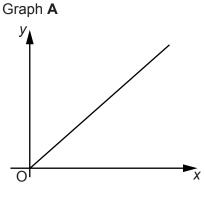
area under graph

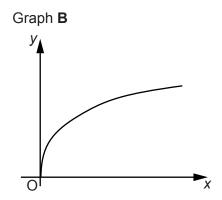
area 2 A=bxh = 8x10 = 80m

area 3
$$A = \frac{1}{2}h(a+b)$$

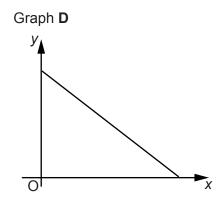
= $\frac{1}{2}x6x(8+10)$
= 54m

9 These graphs show different relationships between the variables *x* and *y*.





Graph **C**



Identify the graph which shows the following.

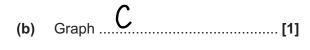
(a) y is directly proportional to x.

Straigh line through origin

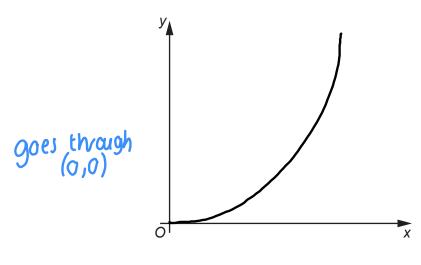
(a) Graph[1]

(b) y is inversely proportional to x.

$$y = \frac{k}{x}$$
reciprocal grouph



10 Sketch a graph which shows that y is directly proportional to x^2 .



[2]

11 A regular polygon has *n* sides.

The polygon's interior angle is 5 times the size of its exterior angle.

Find *n*.

let extenor angle =
$$x$$
... interior angle = $5x$

• Sum of exterior angles is
$$360^\circ \rightarrow n \propto = 360^\circ$$

• each exterior angle is equal $\rightarrow n \propto = 360^\circ$
and there a 'n' number

• sum of interior angles =
$$180(n-2)$$
 $\rightarrow \frac{180(n-2)}{n} = 5x$

Equation 0
$$nx = 360$$

 $x = \frac{360}{n}$

$$so, 5x = \frac{1800}{n}$$

$$180(n-2) = 1800$$

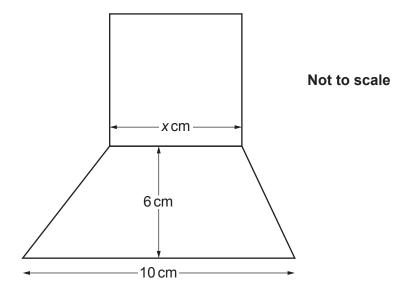
$$n-2 = 10$$

$$+2(n-2) = 1800$$

$$+2(n-2) = 1800$$

$$n = 12$$
 [5]

12 In the diagram, the square and the trapezium share a common side of length x cm.



The area of the square is equal to the area of the trapezium.

Work out the value of x.

area of square =
$$\chi^2$$

area of trapezium: $\frac{1}{2} h(a+b)$

area of $\frac{1}{2} = \frac{1}{2} \times 6 \times (10+x)$

= $\frac{3(10+x)}{30+x}$

area $\frac{1}{2} = area$
 $\chi^2 = 30+x$

faltonial

 $\chi^2 - \chi - 30 = 0$
 $\chi + 5 = 0$

Jet each bracket

 $\chi + 5 = 0$ to 0

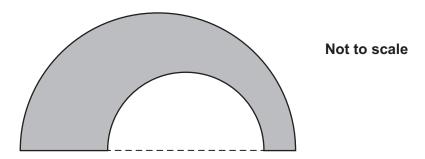
 $\chi - 6 = 0$
 $\chi = 6$

Tength

x = 6

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13 The shape below is formed from two semicircles and a straight line.



The radius of the large semicircle is 8 cm.

The radius of the small semicircle is *t*cm.

Find an expression, in terms of *t*, for the **exact perimeter** of the shaded shape.

14 (a) Without using a calculator, show that $0.\dot{1}\dot{9}$ can be written as $\frac{19}{99}$. [3]

let
$$x = 0.19191919...$$
) subtract x from 100 x .19.19191919...) subtract x from 100x to cancel our decimal places
$$\frac{99x \cdot 19}{x = \frac{19}{99}} = 99$$

(b) Explain how $\frac{19}{99} = 0.\dot{1}\dot{9}$ can be used to find $\frac{19}{990}$ as a decimal and write down its value.

$$\frac{19}{990} = \frac{19}{99} \times \frac{1}{10}$$

$$= 0.19 \div 10$$

$$= 0.09 \div 10$$

$$= 0.019 \times \frac{19}{990} = 0.01$$

PhysicsAndMathsTutor.com

15

15 Use the formula $x_{n+1} = \frac{(x_n)^3}{30} + 2$ with $x_1 = 2$ to calculate x_2 and x_3 . Round your answers correct to 4 decimal places.

$$\chi_{n+1} = \frac{(\chi_n)^3}{30} + 2$$

$$\chi_1 = 2 + 2 = 2 \cdot 2 \cdot (7 \cdot (4dp))$$

$$\chi_2 = 2 \cdot 2 \cdot (67 \cdot (4dp))$$

$$\chi_3 = \frac{(2 \cdot 266 \cdot ...)^3}{30} + 2 = 2 \cdot 3882 \cdot (4dp)$$

$$\chi_3 = 2 \cdot 3882$$

$$x_2 = 1.2667$$
 and $x_3 = 2.3882$ [3]

16 A £1 coin weighs 8.75 g, correct to the nearest 0.01 g. Mitul weighs the contents of a large bag of £1 coins. The coins weigh 2.63 kg, correct to the nearest 10 g.

Mitul says

I am sure that the bag contains exactly £300 because, using bounds, $2625 \div 8.755 = 299.8$ to 1 decimal place.

Show that Mitul may not be correct.

Mitul has used the Lower bound of 8.75g and the upper bound of 2.63kg.

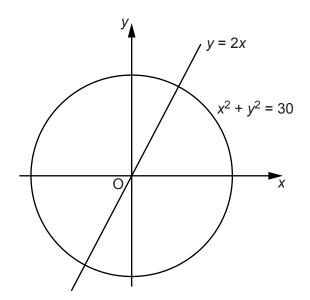
If you change which bounds are used:

UB total weight
$$= \frac{2635}{8.745} = 301.32$$

hence there could be £301.

[3]

17 Find the exact coordinates of the two intersections of the line y = 2x and the circle $x^2 + y^2 = 30$.



Not to scale

to find intersections, you have to

$$y = 2x$$
 0 \Rightarrow $y' = (2x)^{2}$
 $x' + y' = 30$ 0 Sub 0 into 0:

 $x' + 4x' = 30$
 $x' = 6$
 $x = 6$

360°

18 (a) Sketch the graph of $y = \cos x + 1$ for $0^{\circ} \le x \le 720^{\circ}$.

180°

3

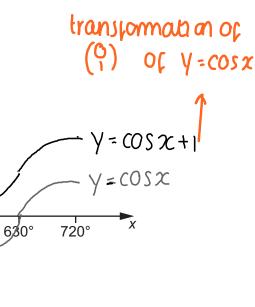
2

1.

0.

-1

90



[3]

(b) Explain why the equation $\cos x + 1 = 2.7$ has no solutions.

Solutions to cosx+1 are bound by 0 and 2, and 2.7 exceeds this.

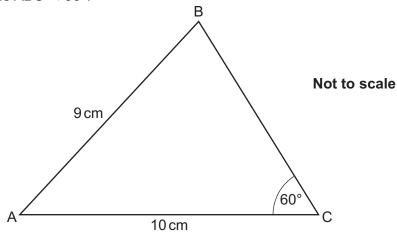
45\d°

540°

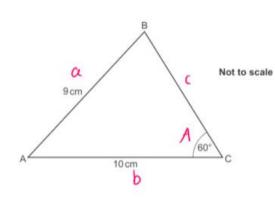
.....

19 In this triangle:

- AB = 9 cm
- $AC = 10 \, cm$
- BC > 5 cm
- angle BCA = 60°
- angle ABC < 90°.



Calculate the area of triangle ABC.



cosine rule:

$$a^{1} = b^{1} + c^{1} - 2bc \cos A$$
 $9^{2} = 10^{1} + (Bc)^{1} - (2 \times 10 \times Bc \times cos 60)$
 $81 = 100 + Bc^{1} - 10(Bc)$
 $0 = (Bc)^{1} - 10(Bc) + 19$
 $0 = x^{2} - 10x + 19$

$$\chi = 10 \pm \sqrt{(10)^2 - (4 \times 1 \times 19)}$$

told in the question that BC>5, so (annot be 5-56

Area of triangle = 1/2 ab sinc 2 sides and angle between hem

= 32.3cm(1dp)

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20 (a) b is a vector.

Given that $\mathbf{b} + \begin{pmatrix} 5 \\ 2 \end{pmatrix}$ is parallel to $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$, find two possible answers for \mathbf{b} .

let
$$b = \begin{pmatrix} x \\ y \end{pmatrix}$$

 $b + \begin{pmatrix} 5 \\ 2 \end{pmatrix} = \begin{pmatrix} x \\ y \end{pmatrix} + \begin{pmatrix} 5 \\ 2 \end{pmatrix} = \begin{pmatrix} x+5 \\ y+2 \end{pmatrix}$

We have to find possibilities for $\binom{x}{y}$ which makes $\binom{x+5}{y+2}$ multiples of $\binom{2}{1}$, as they are parallel

for example
$$\binom{1}{1}$$
 or $\binom{3}{2}$

$$b+\binom{5}{2}=\binom{6}{3}$$

$$b+\binom{5}{2}=\binom{8}{4}$$

(a) $b = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \text{ or } \begin{bmatrix} 3 \\ 2 \end{bmatrix}$ [3]

(b) Given that

$$m \binom{4}{1} + n \binom{5}{2} = \binom{12}{6}$$

find the value of m and the value of n.

$$m\binom{4}{1} + n\binom{5}{2} = \binom{12}{6}$$

$$\binom{4m}{m} + \binom{5n}{2n} = \binom{12}{6}$$

$$0 : 4m + 5n = 12$$

$$0 \times 4 : -\frac{4m + 8n = 24}{-3n = -12}$$

$$m + 2(4) = 6$$

$$m + 8 = 6$$

$$m = 7$$

(b)
$$m = \frac{-2}{n}$$
 $n = \frac{4}{n}$ [5]

21 Show that
$$\frac{5x}{x+5} + \frac{25}{x-7} - \frac{300}{(x+5)(x-7)}$$
 simplifies to an integer. [6]
$$\frac{5x}{x+5} + \frac{25}{x-7} - \frac{300}{(x+5)(x-7)}$$

$$= \frac{5x}{(x+5)} \frac{(x-7)}{(x+5)(x-7)} + \frac{25(x+5)}{(x-7)(x+5)} - \frac{300}{(x+5)(x-7)}$$

$$= \frac{5x(x-7) + 25(x+5) - 300}{(x+5)(x-7)}$$

$$= \frac{5x^3 - 35x + 25x + 125 - 300}{(x+5)(x-7)}$$

$$= \frac{5x^3 - 10x - 175}{(x+5)(x-7)} = \frac{5(x^3 - 10x - 175)}{(x+5)(x-7)} = \frac{5(x+5)(x-7)}{(x+5)(x-7)} = \frac{5}{(x+5)(x-7)} = \frac{5}{(x+5)(x-$$

22 ADDITIONAL ANSWER SPACE

If additiona must be cle	I space is required, you should use early shown in the margin(s).	the following lined	page(s). The ques	tion number(s)
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