



Oxford Cambridge and RSA

MODEL SOLUTIONS

H

GCSE (9–1) Mathematics

J560/05 Paper 5 (Higher Tier)

Thursday 8 November 2018 – Morning

Time allowed: 1 hour 30 minutes



You may use:

- geometrical instruments
- tracing paper

Do not use:

- a calculator



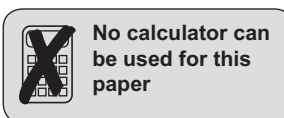
First name										
Last name										
Centre number						Candidate number				

INSTRUCTIONS

- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number and candidate number.
- Answer **all** the questions.
- Read each question carefully before you start to write your answer.
- Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided. If additional space is required, use the lined page(s) at the end of this booklet. The question number(s) must be clearly shown.
- Do **not** write in the barcodes.

INFORMATION

- The total mark for this paper is **100**.
- The marks for each question are shown in brackets [].
- This document consists of **20** pages.



Answer **all** the questions.

1 Work out.

(a) $\sqrt[3]{64} \times 2^{-1}$

$$4 \times \frac{1}{2} =$$

(a) 2 [2]

(b) $4.3 \times 10^5 + 3.8 \times 10^4$
Give your answer in standard form.

$$\begin{array}{r} = \quad 430,000 \\ + \quad 38,000 \\ \hline 468,000 \\ \underbrace{\hspace{10em}}_5 \end{array}$$

(b) 4.68×10^5 [3]

2 By writing each number correct to 1 significant figure, find an estimate for this calculation.

$$\frac{606.3 \times 0.312}{19.93}$$

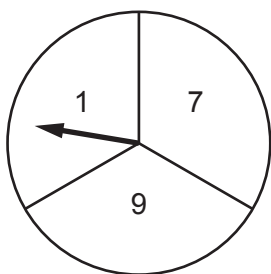
$$\begin{array}{l} 606.3 \approx 600 \\ 0.312 \approx 0.3 \\ 19.93 \approx 20 \end{array}$$

$$\frac{600 \times 0.3}{20} = \frac{180}{20} =$$

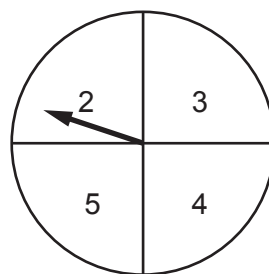
..... ≈ 9 [3]

3

3 Geoff has two fair spinners.



Spinner A



Spinner B

He spins both spinners and **multiplies** the numbers on each spinner.

(a) Complete the table.

		Spinner A		
		1	7	9
Spinner B	2	2	14	18
	3	3	21	27
	4	4	28	36
	5	5	35	45

[1]

(b) Geoff wants to work out the probability that the outcome of the multiplication is an even number or a prime number. Here is his working.

The probability the outcome is an even number is $\frac{6}{12}$.

The probability the outcome is a prime number is $\frac{3}{12}$.

The probability the outcome is an even number or a prime number is $\frac{6}{12} + \frac{3}{12} = \frac{9}{12}$.

Geoff is wrong.
Explain his error and give the correct answer.

Even and prime are not mutually exclusive, 2 is in both categories [2]

$\frac{8}{12} = \frac{2}{3}$

4

- 4 A solid metal block has mass 500g and volume 125cm³.

Work out the density of the block.
Give the units of your answer.

$$\text{Density} = \frac{\text{mass}}{\text{volume}}$$

$$\text{Density} = \frac{500}{125} = 4$$

..... 4 g/cm^3 [3]

- 5 The depth of water in a garden pond is 57.8cm.
The depth decreases by 0.3cm per day.

- (a) Assume the depth continues to decrease at the same rate.

After how many days will the depth reach 54.2cm?

$$57.8 - 54.2 = 3.6 \text{ cm decrease}$$

$$\begin{aligned} \text{This takes: } & 3.6 \div 0.3 \\ & = 12 \text{ days} \end{aligned}$$

(a) 12 days [3]

- (b) If the depth of water decreases at a slower rate, what effect will this have on your answer to part (a)?

..... It would take longer, answer will
be bigger [1]

5

- 6 Sally has 30 feet of ribbon.

She cuts strips each of length $2\frac{2}{5}$ feet from the ribbon.

Sally says

I can cut 13 of these strips from this ribbon.

Is she correct?

Show how you decide.

$$30 \div 2\frac{2}{5} = 30 \div \frac{12}{5}$$

$$= 30 \times \frac{5}{12} = \frac{150}{12} = 12\frac{1}{2}$$

$$12.5 < 13$$

No, 13 strips can't be cut

[4]

- 7 Emily spent £2400 on holiday in 2017.
This was 20% more than she spent on holiday in 2016.

$$100 + 20 = 120\%$$

Calculate the amount she spent on holiday in 2016.

$$2400 = 120\%$$

$$\downarrow \div 12$$

$$200 = 10\%$$

$$\downarrow \times 10$$

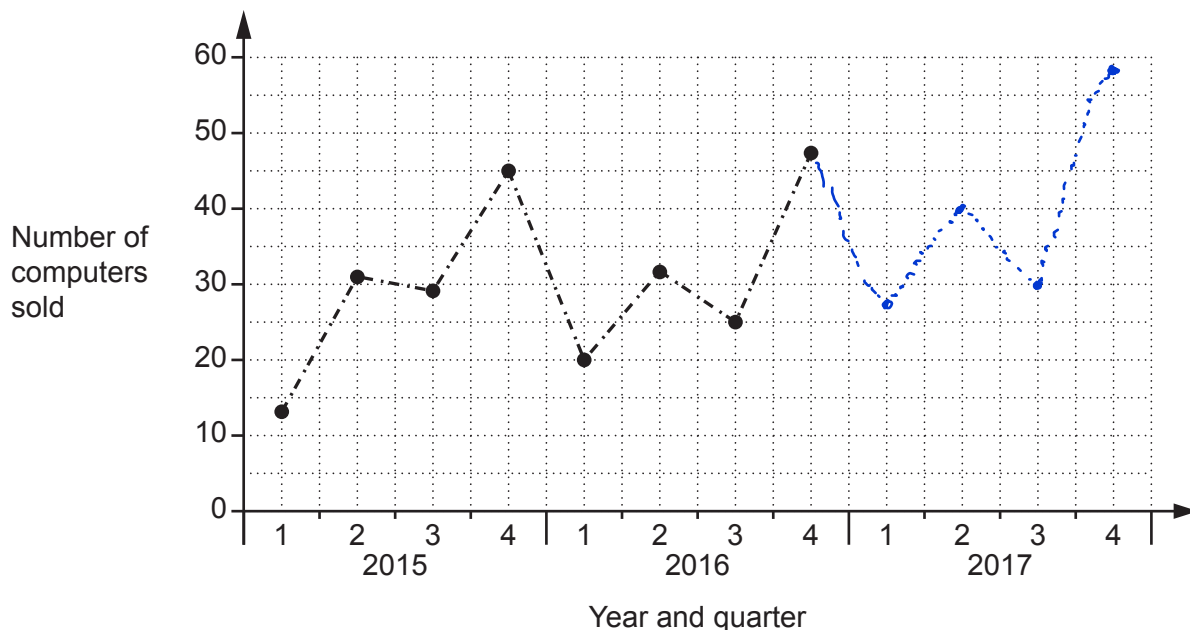
$$2000 = 100\%$$

£ 2000 [3]

8 The table shows the number of computers sold in Tom's shop each quarter from 2015 to 2017.

	2015				2016				2017			
Quarter	1	2	3	4	1	2	3	4	1	2	3	4
Number of computers sold	13	31	29	45	20	32	25	47	27	40	30	58

(a) Complete this graph using the information for 2017.



[2]

(b) Tom adds the three results for quarter 1 and he adds the three results for quarter 4. Tom says

The ratio of the **total** number of computers sold in quarter 1 compared to quarter 4 is 2 : 5.

Is he correct?

Show your reasoning.

$$Q1: 13 + 20 + 27 = 60$$

$$Q4: 45 + 47 + 58 = 150$$

$$Q1 : Q4$$

$$\div 30 \left(\begin{array}{l} 60 : 150 \\ \rightarrow 2 : 5 \leftarrow \end{array} \right) \div 30$$

2 : 5, yes he's correct

[2]

- (c) Make two comments about Tom's sales over the period 2015 to 2017.

Comment 1 Sales are increasing

Comment 2 Sales were weakest in 1st Quarter

[2]

- (d) Tom predicts that he will sell more than 60 computers in the 4th quarter of 2018.

What assumption has he made?

..... The trend in his sales will continue

..... increasing

[1]

- 9 Rearrange this formula to make y the subject.

$$x = y^2 + 7$$

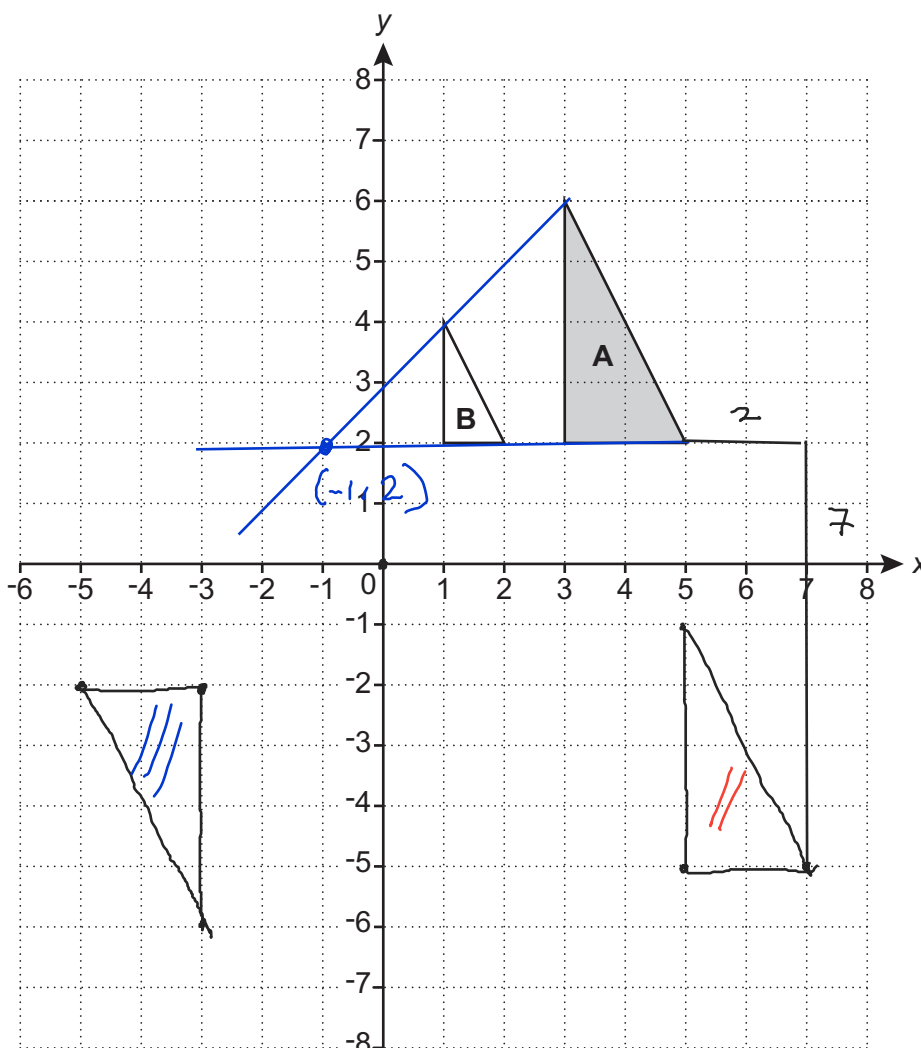
$$x - 7 = y^2$$

$$\sqrt{x - 7} = y$$

..... $y = \sqrt{x - 7}$

[2]

10 Triangle **A** and triangle **B** are drawn on the coordinate grid.



(a) (i) Draw the image of triangle **A** after a rotation of 180° about $(0, 0)$. // [2]

(ii) Draw the image of triangle **A** after a translation by the vector $\begin{pmatrix} 2 \\ -7 \end{pmatrix}$. -2 right 7 down // [2]

(b) Describe fully the **single** transformation that maps triangle **A** onto triangle **B**.

..... Enlargement, centre $(-1, 2)$, scale
 factor $\frac{1}{2}$ [3]

- 11 The price of a washing machine is reduced by 20% for a sale. Afterwards, the sale price is increased by 30%.

Joachim says

The washing machine is now 10% more expensive than before the sale.

Explain Joachim's error and work out the correct percentage change in the price of the washing machine from before the sale to after the sale.

Joachim's error is He has subtracted the two percentages

Reduced by 20% = $\times 0.8$ - 100% - 20%

Increased by 30% = $\times 1.3$ - 100% + 30%

Total change: $1 - 0.8 \times 1.3$

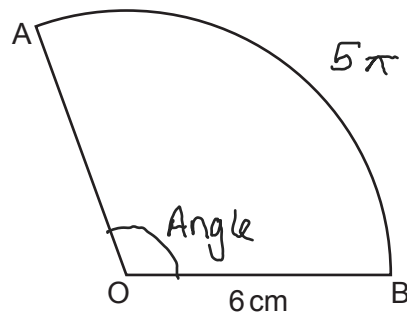
$$= 1 - \frac{4}{5} \times \frac{13}{10} = 1 - \frac{52}{50} = 1 - \frac{104}{100}$$

Percentage: $1 - \frac{104}{100} = \frac{4}{100} = 4\%$

Correct percentage change is 4 % [6]

10

- 12 AOB is a sector of a circle, centre O and radius 6 cm.
The length of arc AB is 5π cm.



Not to scale

Find the area of the sector.
Give your answer in terms of π .

Circumference: $\pi \times d \times \frac{\text{angle}}{360}$

$$12\pi \times \frac{\theta}{360} = 5\pi$$

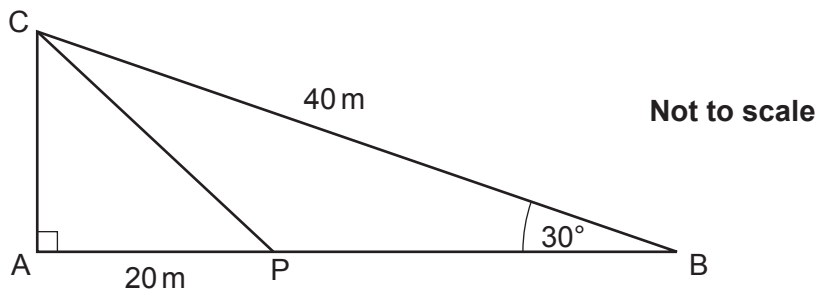
$$\frac{12\theta}{360} = 5$$

$$\frac{\theta}{30} = 5 \quad \therefore \theta = 150^\circ$$

$$\begin{aligned} \text{Area} &= \frac{\theta}{360} \times \pi r^2 \\ &= \frac{150}{360} \times \pi \times 6^2 \\ &= \frac{5}{12} \times 36\pi \\ &= 15\pi \end{aligned}$$

..... 15π cm² [5]

- 13 In the diagram, ABC is a right-angled triangle.
 P is a point on AB.
 BC = 40 m, AP = 20 m and angle ABC = 30°.



- (a) Show that AC = 20 m.

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

[3]

$$AC = 40 \sin 30 - \frac{1}{2}$$

$$AC = 20 \text{ m}$$

- (b) Find the length of PB.

Give your answer in the form $a(\sqrt{3} - b)$, where a and b are integers.

$$AB = 40 \cos 30 - \frac{\sqrt{3}}{2}$$

$$= 20\sqrt{3}$$

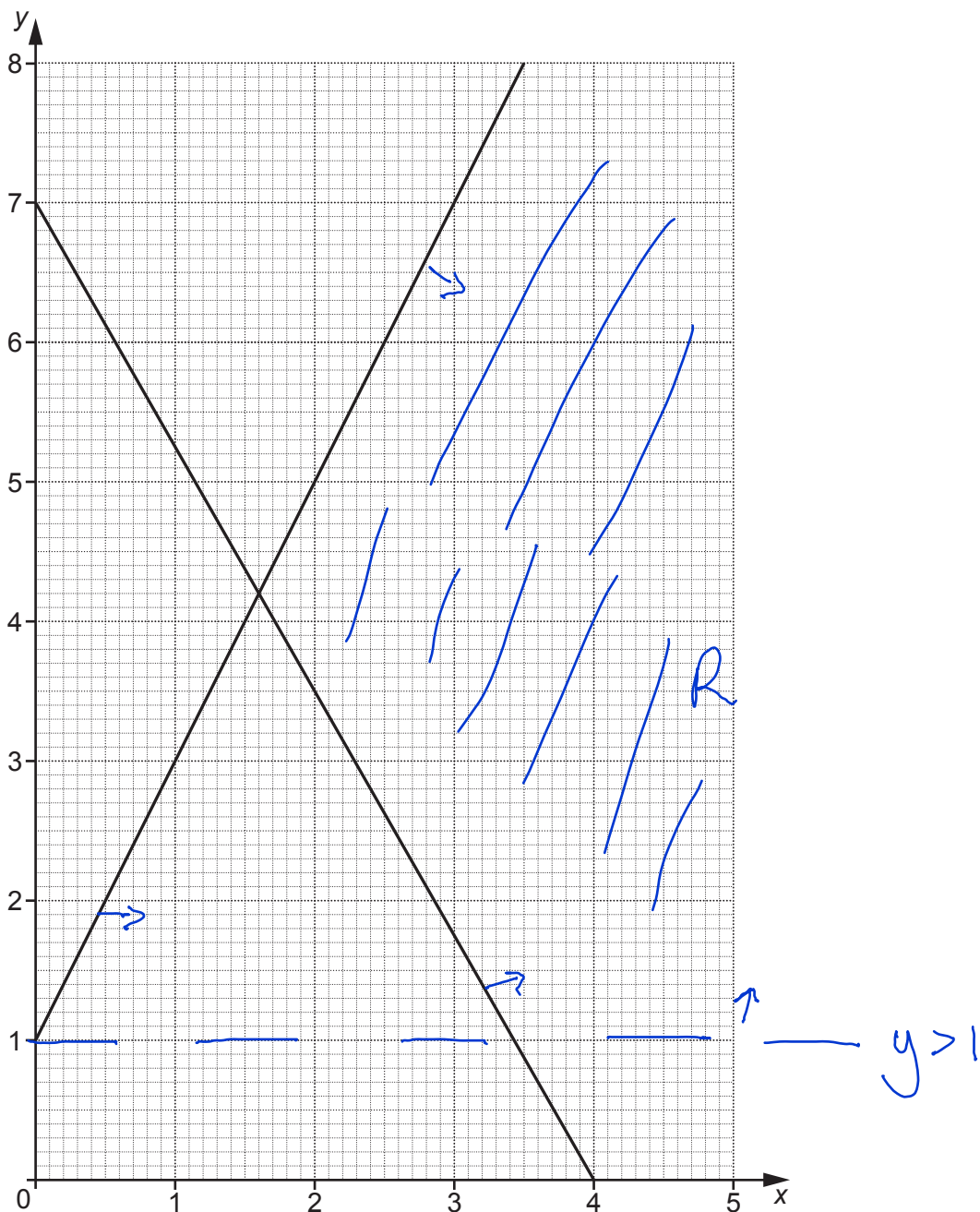
$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$PB = 20\sqrt{3} - 20$$

$$= 20(\sqrt{3} - 1)$$

(b) $20(\sqrt{3} - 1)$ [5]

14 The diagram shows the lines $y = 2x + 1$ and $7x + 4y = 28$.



The region R satisfies these inequalities.

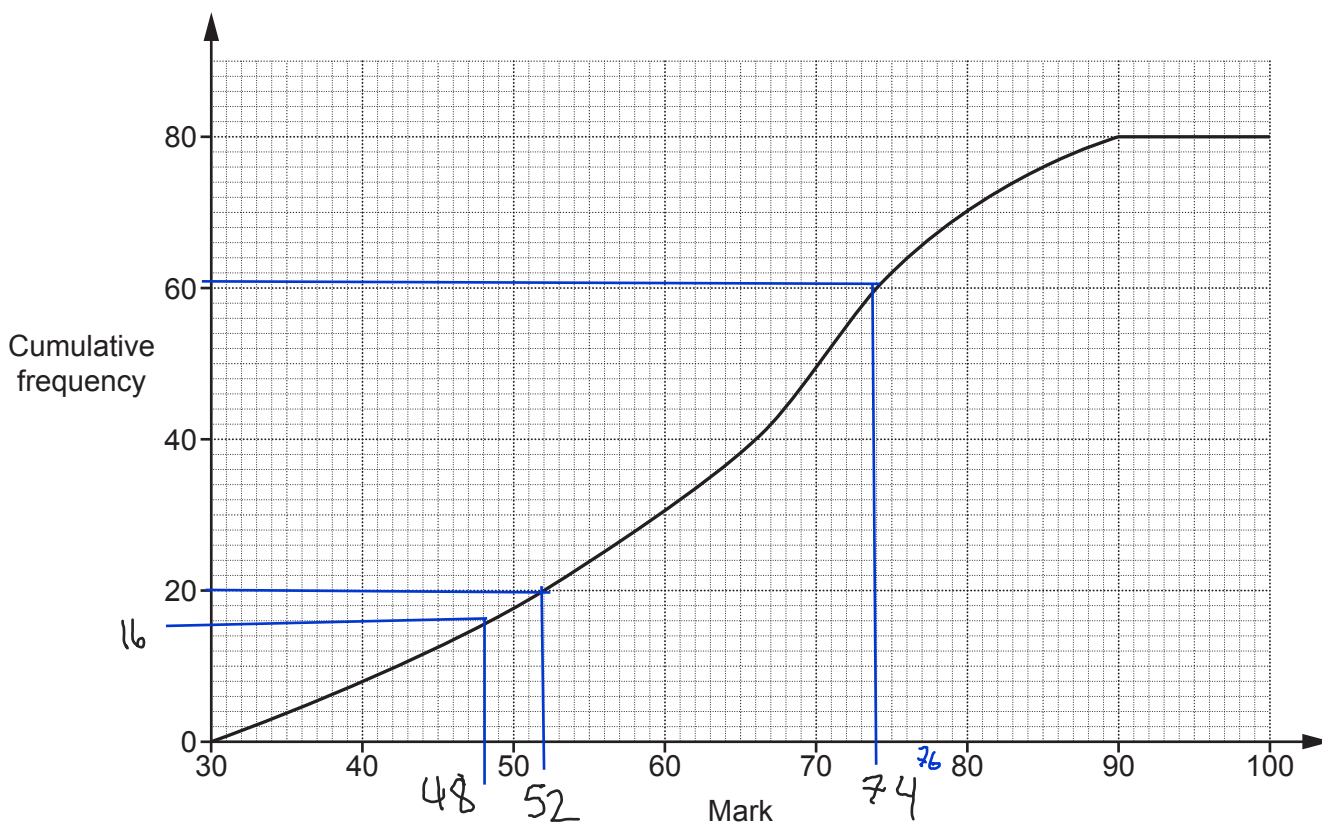
$$y \leq 2x + 1$$

$$7x + 4y \geq 28$$

$$y > 1$$

By drawing a third straight line, find and label the region R that satisfies these inequalities. [5]

- 15 The cumulative frequency graph shows information about the marks scored by a group of 80 students in a test.



- (a) Find the interquartile range.

$$\frac{80}{4} = 20$$

$$20 \times 3 = 60$$

$$74 - 52$$

(a) 22 [2]

- (b) The ratio of the number of students passing the test compared to failing the test is 4 : 1. Find the minimum mark needed to pass the test.

$$\begin{array}{r|l} 4 : 1 & \text{Total} \\ \times 16 \leftarrow & 5 \\ 64 : 16 & 80 \leftarrow \times 16 \end{array}$$

16 students fail
64 pass

(b) 48 [3]

16 Here is a sequence.

$$5 \qquad 5\sqrt{3} \qquad 15 \qquad 15\sqrt{3}$$



(a) Work out the next term.

$$\times \sqrt{3}$$

$$15\sqrt{3} \times \sqrt{3} = 15 \times 3$$

(a) 45 [1]

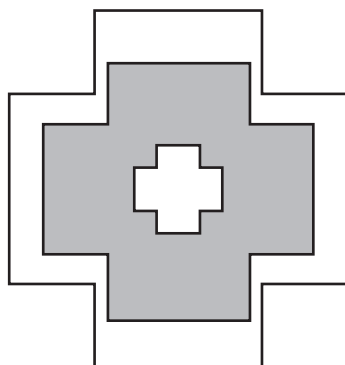
(b) Find the n th term.

$$5 \times (\sqrt{3})^{n-1}$$

(b) $5 \times (\sqrt{3})^{n-1}$ [3]

15

- 17 The diagram consists of three mathematically similar shapes.
The heights of the shapes are in the ratio 1 : 4 : 5.



Not to scale

Find the ratio

total shaded area : total unshaded area.

Give your answer in its simplest form.

$$\text{Total unshaded part: } 1 + 5 = 6$$

$$\text{Shaded part: } 4$$

$$\frac{6}{4} = \frac{3}{2}$$

$$3:2$$

total shaded area : total unshaded area 3 : 2 [4]

18 (a) (i) Write $x^2 + 4x - 16$ in the form $(x + a)^2 - b$.

$$4 \div 2 = 2 \quad (x + 2)^2 - 2^2 - 16$$

$$= (x + 2)^2 - 4 - 16 \quad \text{(a)(i) } \dots (x + 2)^2 - 20 \quad [3]$$

(ii) Solve the equation $x^2 + 4x - 16 = 0$.
Give your answers in surd form as simply as possible.

$$(x + 2)^2 - 20 = 0$$

$$\quad \quad \quad +20$$

$$(x + 2)^2 = 20$$

$$\quad \quad \quad \sqrt{}$$

$$(x + 2) = \pm \sqrt{20} \quad \text{---} \quad \sqrt{4 \times 5} = 2\sqrt{5}$$

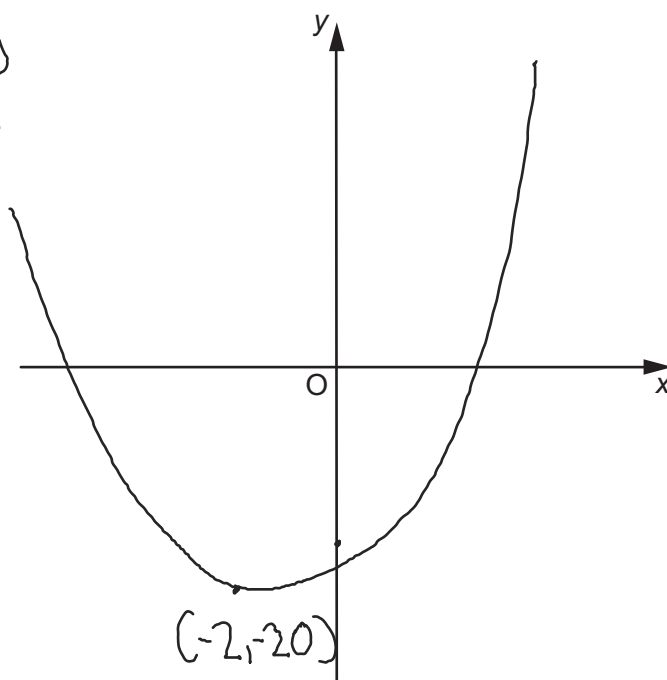
$$\quad \quad \quad -1$$

$$x = -2 \pm 2\sqrt{5}$$

(ii) $x = -2 + 2\sqrt{5}$ or $x = -2 - 2\sqrt{5}$ [4]

(b) Sketch the graph of $y = x^2 + 4x - 16$, showing clearly the coordinates of any turning points.

Turning point
 $(-2, -20)$
 $(-p, a)$



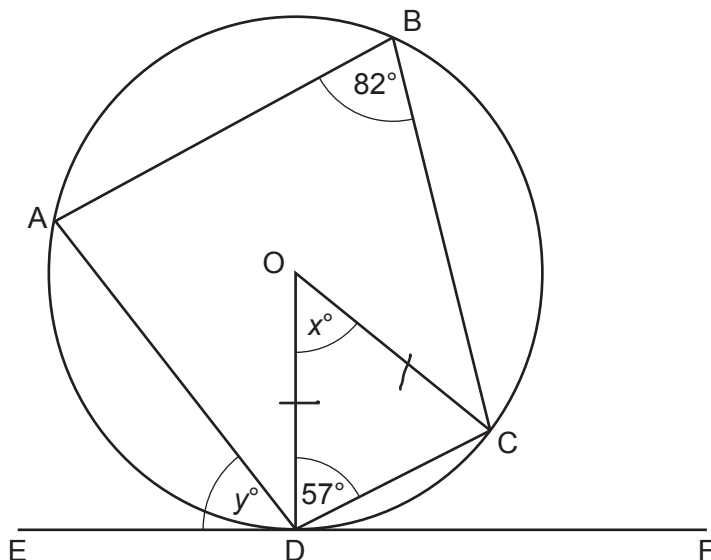
[3]

19 The diagram shows a circle, centre O.

Points A, B, C and D lie on the circumference of the circle.

EDF is a tangent to the circle.

Angle ABC = 82° and angle ODC = 57°.



Not to scale

(a) Work out the value of x.

$$\angle OCD = 57^\circ$$

same radius =
isosceles

$$180 - 57 - 57 =$$

$$180 - 114 =$$

(a) $x = \dots\dots\dots 66^\circ \dots\dots\dots [2]$

(b) Work out the value of y.

$$\angle AOD = 180 - 82 - 57 = 41^\circ \quad \text{- opposite cyclic angles add to } 180^\circ$$

$$\angle y = 90 - 41 = 49 \quad \text{Tangent meets at } 90^\circ$$

(b) $y = \dots\dots\dots 49^\circ \dots\dots\dots [3]$

20 (a) Prove that $(2x+1)(3x+2) + x(3x+5) + 2$ is a perfect square.

$$\underline{6x^2} + \underline{4x} + \underline{3x} + \underline{2} + \underline{3x^2} + \underline{5x} + \underline{2}$$

$$9x^2 + 12x + 4$$

factorise

$$\begin{array}{l} \times \text{ to } 9 \times 4 = 36 \\ + \text{ to } \quad \quad 12 \\ \hline 6, 6 \end{array}$$

$$\begin{array}{l|l} 9x^2 + 6x & + 6x + 4 \\ 3x(3x+2) & 2(3x+2) \end{array}$$

$$= (3x+2)(3x+2)$$

$$= (3x+2)^2, \text{ therefore it is a perfect square}$$

[6]

(b) Gemma says

The equation $(2x+1)(3x+2) + x(3x+5) + 2 = -12$ has no solutions.

Explain Gemma's reasoning.

$$9x^2 + 12x + 4 = -12$$

$$9x^2 + 12x + 16 = 0$$

[1]

$$b^2 - 4ac = 12^2 - 4 \times 9 \times 16 = -432$$

END OF QUESTION PAPER

$b^2 - 4ac < 0$, therefore it has no solutions

ADDITIONAL ANSWER SPACE

If additional space is required, you should use the following lined page(s). The question number(s) must be clearly shown in the margin(s).

A large area of lined paper for writing answers. It features a vertical margin line on the left side and horizontal dotted lines for writing. The lines are evenly spaced and extend across the width of the page.

A large area of the page is reserved for writing, featuring a vertical solid line on the left side and horizontal dotted lines extending across the page.



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