


Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Pearson Edexcel		Centre Number			Candidate Number				
International GCSE		<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>			<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>				
Thursday 18 June 2020									
Morning (Time: 2 hours)					Paper Reference 4PM1/02R				
Further Pure Mathematics									
Paper 2R									
Calculators may be used.								Total Marks	

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

International GCSE in Further Pure Mathematics Formulae sheet

Mensuration

Surface area of sphere = $4\pi r^2$

Curved surface area of cone = $\pi r \times$ slant height

Volume of sphere = $\frac{4}{3}\pi r^3$

Series

Arithmetic series

Sum to n terms, $S_n = \frac{n}{2}[2a + (n - 1)d]$

Geometric series

Sum to n terms, $S_n = \frac{a(1 - r^n)}{(1 - r)}$

Sum to infinity, $S_\infty = \frac{a}{1 - r}$ $|r| < 1$

Binomial series

$$(1 + x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$$

Calculus

Quotient rule (differentiation)

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry

Cosine rule

In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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Answer all TEN questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

- 1 The n th term of an arithmetic series A is a_n
The n th term of a geometric series G is t_n

For these two series

$$a_1 = t_1 \quad a_{10} = t_3 = 48 \quad a_{10} = 4t_2$$

Find

- (i) the common ratio of G ,
(ii) the common difference of A .

(6)

(Total for Question 1 is 6 marks)



2

$$f(x) = x^3 + px + q \quad \text{where } p \text{ and } q \text{ are constants.}$$

The remainder when $f(x)$ is divided by $(x - 1)$ is -12

The remainder when $f(x)$ is divided by $(x - 4)$ is 30

(a) Find the value of p and the value of q . (6)

Using your values of p and q

(b) show that $f(3) = 0$ (1)

(c) Express $f(x)$ as a product of linear factors. (3)

(d) Hence solve the equation $f(x) = 0$ (1)

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Question 2 continued

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(Total for Question 2 is 11 marks)



3

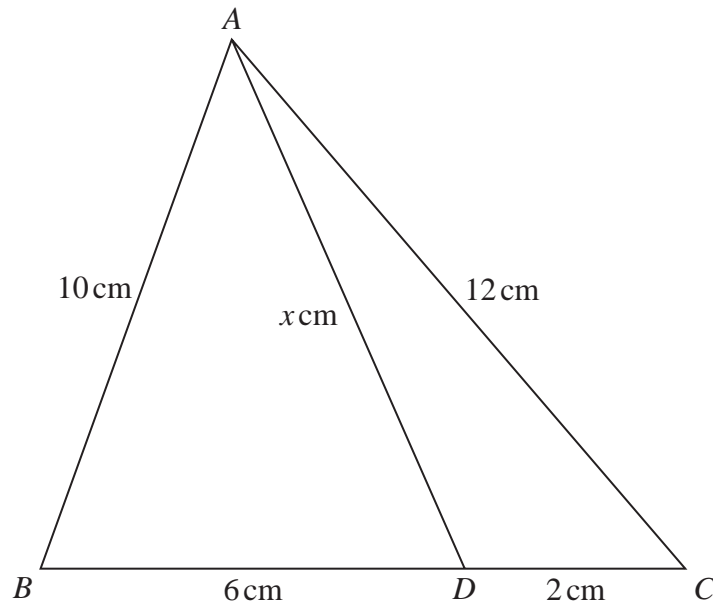
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accurately drawn

Figure 1

Figure 1 shows the triangle ABC in which $AB = 10\text{ cm}$ and $AC = 12\text{ cm}$.
The point D lies on BC such that $BD = 6\text{ cm}$, $DC = 2\text{ cm}$ and $AD = x\text{ cm}$.

- (a) Show that $x = 11$ (4)
- (b) Find the area, in cm^2 to 3 significant figures, of triangle ADB . (4)

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6



Question 3 continued

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(Total for Question 3 is 8 marks)



- 4 (a) Complete the table of values for $y = 2x + 1 + \frac{2}{x^2}$

Give your answers to 2 decimal places where appropriate.

x	0.5	1	1.5	2	2.5	3	3.5
y		5			6.32		8.16

(2)

- (b) On the grid opposite, draw the graph of $y = 2x + 1 + \frac{2}{x^2}$ for $0.5 \leq x \leq 3.5$

(2)

- (c) Use your graph to obtain estimates, to 1 decimal place, of the roots of the equation

$$2x + \frac{2}{x^2} = 7 \quad \text{in the interval } 0.5 \leq x \leq 3.5$$

(2)

- (d) By drawing a suitable straight line on the grid, obtain estimates, to 1 decimal place, of the roots of the equation

$$\frac{3x}{2} + \frac{2}{x^2} = 5 \quad \text{in the interval } 0.5 \leq x \leq 3.5$$

(5)

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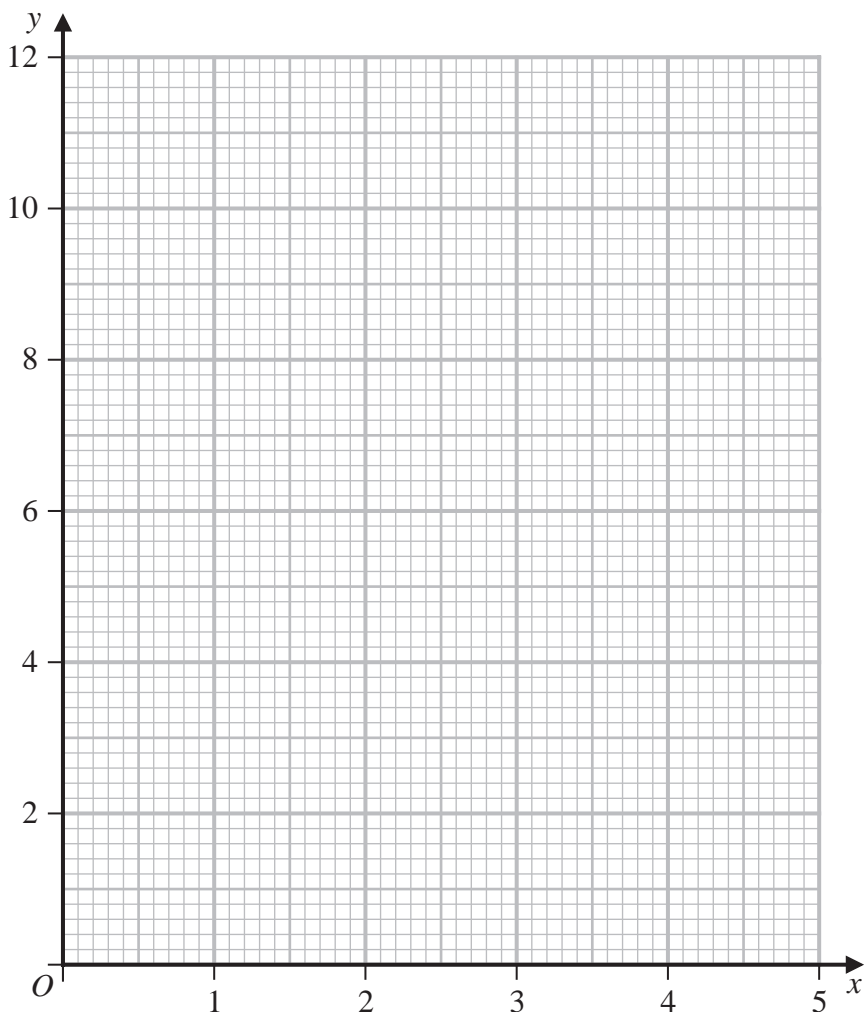


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Question 4 continued



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Question 4 continued

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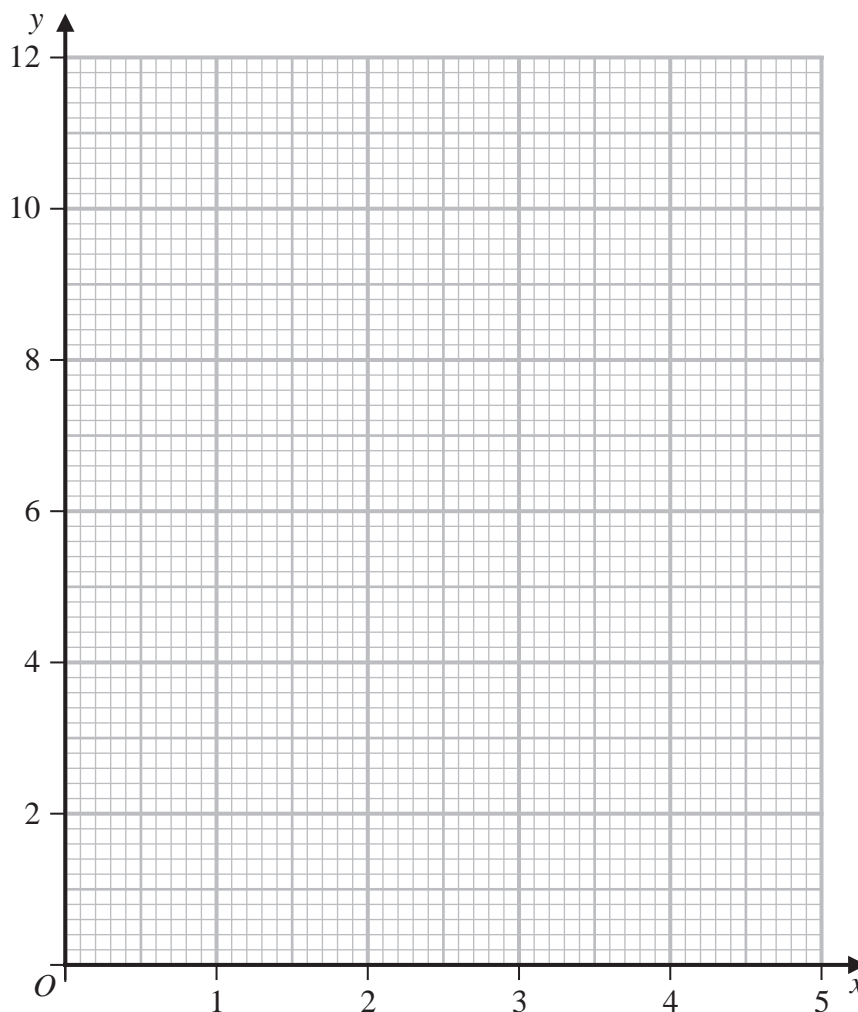
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Question 4 continued

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(Total for Question 4 is 11 marks)



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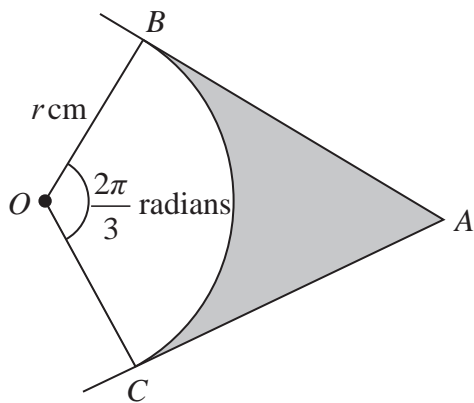


Diagram NOT accurately drawn

Figure 2

In Figure 2, AB and AC are tangents to a circle with centre O and radius r cm.

The points B and C lie on the circle so that OBC is a sector of this circle and $\angle BOC = \frac{2\pi}{3}$ radians.

Given that the area of the shaded region is 10 cm^2 ,

find, to 3 significant figures, the value of r .

(8)

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Question 5 continued

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(Total for Question 5 is 8 marks)



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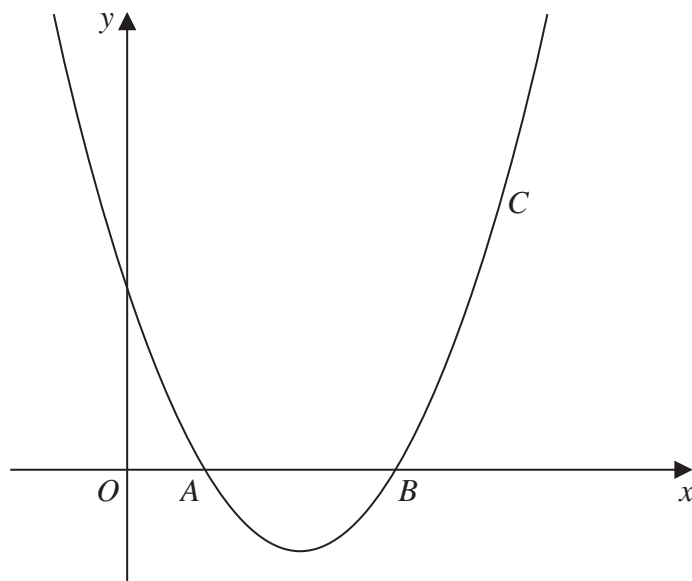
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Figure 3

The curve C with equation $y = x^2 - 5x + 4$ crosses the x -axis at the points A and B , as shown in Figure 3

- (a) Find the coordinates of A and the coordinates of B . (3)

The tangent to C at A meets the tangent to C at B at the point T .

- (b) Find the coordinates of T . (6)

The normal to C at A meets the normal to C at B at the point N .

- (c) Find the coordinates of N . (3)

- (d) Find the area of the quadrilateral $ATBN$. (3)

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Question 6 continued

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Question 6 continued

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Question 6 continued

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(Total for Question 6 is 15 marks)



P 6 2 2 8 4 A 0 1 7 3 2

- 7 (a) Find the set of values of k for which the equation $kx^2 - 4x + 2k = 7$ has real roots (4)

Given that the roots of the equation $kx^2 - 4x + 2k = 7$ are α and β ,

- (b) form a quadratic equation with roots $\frac{\alpha + 1}{\alpha}$ and $\frac{\beta + 1}{\beta}$

Give each coefficient in terms of k . (8)

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Question 7 continued

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 12 marks)



8 Solve the equation $\log_3 x - 2\log_x 3 = 1$

(7)

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Question 8 continued

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(Total for Question 8 is 7 marks)



9 Given that

$$x = e^{-t} \sin 2t$$

show that

$$\frac{d^2x}{dt^2} + 2\frac{dx}{dt} + 5x = 0 \quad (8)$$

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Question 9 continued

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Question 9 continued

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Question 9 continued

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(Total for Question 9 is 8 marks)



10

$$f(x) = 32x^3 - 33x + 1$$

(a) Show that $f(1) = 0$ (1)

(b) Hence using an algebraic method solve $f(x) = 0$ (4)

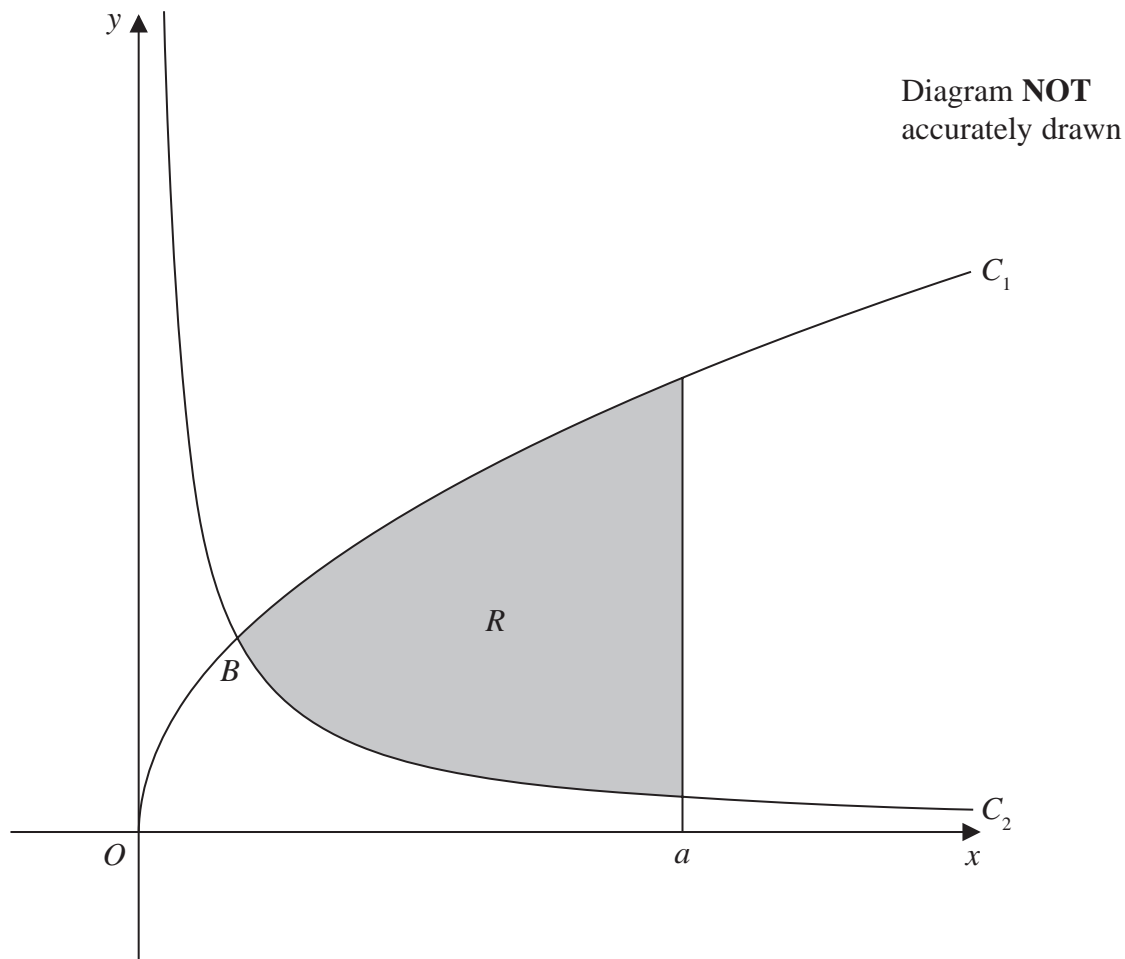


Figure 4

The region R , shown shaded in Figure 4, is bounded by the curve C_1 with equation $y = \sqrt{x}$, by the curve C_2 with equation $y = \frac{1}{8x}$ and by the line with equation $x = a$

The curves C_1 and C_2 intersect at the point B , with x coordinate p , where $p < a$

(c) Find the value of p . (2)

The region R is rotated through 360° about the x -axis to generate a solid with volume $\frac{27\pi}{64}$

(d) Use algebraic integration to find the value of a . (7)

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Question 10 continued

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Question 10 continued

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Question 10 continued

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(Total for Question 10 is 14 marks)

TOTAL FOR PAPER IS 100 MARKS

