

Mark Scheme (Results)

Summer 2016

Pearson Edexcel GCSE In Mathematics B (2MB01) Higher (Calculator) Unit 3



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NOTES ON MARKING PRINCIPLES

- 1 All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- 2 Mark schemes should be applied positively.
- 3 All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e if the answer matches the mark scheme. Note that in some cases a correct answer alone will not score marks unless supported by working; these situations are made clear in the mark scheme. Examiners should be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- 4 Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- 5 Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
- 6 Mark schemes will award marks for the quality of written communication (QWC). The strands are as follows:
 - i) *ensure that text is legible and that spelling, punctuation and grammar are accurate so that meaning is clear* Comprehension and meaning is clear by using correct notation and labelling conventions.
 - ii) select and use a form and style of writing appropriate to purpose and to complex subject matter Reasoning, explanation or argument is correct and appropriately structured to convey mathematical reasoning.
 - iii) organise information clearly and coherently, using specialist vocabulary when appropriate.
 The mathematical methods and processes used are coherently and clearly organised and the appropriate mathematical vocabulary used.

7 With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks. Send the response to review, and discuss each of these situations with your Team Leader.

If there is no answer on the answer line then check the working for an obvious answer.

Partial answers shown (usually indicated in the ms by brackets) can be awarded the method mark associated with it (implied).

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks; transcription errors may also gain some credit. Send any such responses to review for the Team Leader to consider.

If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

8 Follow through marks

Follow through marks which involve a single stage calculation can be awarded without working since you can check the answer yourself, but if ambiguous do not award.

Follow through marks which involve more than one stage of calculation can only be awarded on sight of the relevant working, even if it appears obvious that there is only one way you could get the answer given.

9 Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: e.g. incorrect cancelling of a fraction that would otherwise be correct

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect e.g. algebra.

10 Probability

Probability answers must be given a fractions, percentages or decimals. If a candidate gives a decimal equivalent to a probability, this should be written to at least 2 decimal places (unless tenths).

Incorrect notation should lose the accuracy marks, but be awarded any implied method marks.

If a probability answer is given on the answer line using both incorrect and correct notation, award the marks.

If a probability fraction is given then cancelled incorrectly, ignore the incorrectly cancelled answer.

11 Linear equations

Full marks can be gained if the solution alone is given on the answer line, or otherwise unambiguously indicated in working (without contradiction elsewhere). Where the correct solution only is shown substituted, but not identified as the solution, the accuracy mark is lost but any method marks can be awarded (embedded answers).

12 Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another.

13 Range of answers

Unless otherwise stated, when an answer is given as a range (e.g 3.5 - 4.2) then this is inclusive of the end points (e.g 3.5, 4.2) and includes all numbers within the range (e.g 4, 4.1)

Guidance on the use of codes within this mark scheme					
M1 – method mark A1 – accuracy mark B1 – Working mark C1 – communication mark QWC – quality of written communication oe – or equivalent cao – correct answer only ft – follow through sc – special case dep – dependent (on a previous mark or conclusion)					
indep – independent isw – ignore subsequent working					

PAP	PAPER: 5MB3H/01						
Qu	lestion	Working	Answer	Mark	Notes		
1*			Decision (supported)	3	M1 for correct first step e.g. $15 \div 3$ M1 for complete method C1 for correct decision with accurate figures		
2	(a)		Correct diagram	2	B2 cao (B1 for correct orientation)		
	(b)		Enlargement, sf 4, centre (0, 1)	3	B1 for enlargement B1 for scale factor 4 B1 for centre (0, 1)		
3			$w = \frac{d+5}{2}$	2	M1 for attempt to add 5 to both sides or divide both sides by 2 as a first step, eg $d + 5 = 2w$ oe or $\frac{d}{2} = w - \frac{5}{2}$ oe A1 for $w = \frac{d+5}{2}$ oe		

PAPE	ER: 5MB3	3H/01			
Qu	estion	Working	Answer	Mark	Notes
4			22.5	4	M1 for $4(x-8) = 2x + 13$ M1 for expansion of bracket or division of all terms by 4, eg $4x - 32 = 2x + 13$, or $x - 8 = \frac{2x}{4} + \frac{13}{4}$ M1 for isolating x and number terms eg $2x = 45$, $\frac{x}{2} = \frac{45}{4}$ A1 for $\frac{45}{2}$ or 22.5 OR M1 for $(180 - 64) \div 2$ (= 58) M1 for $4(x - 8) = "58"$ or $2x + 13 = "58"$ or "58" - 13 (= 45) M1 for isolating x and number terms eg $4x = 90$, $2x = 45$ or "45" $\div 2$ A1 for $\frac{45}{2}$ or 22.5 OR M1 for $64 + 4(x - 8) + 2x + 13$ M1 for $64 + 4(x - 8) + 2x + 13 = 180$ M1 for isolating x and number terms eg $6x = 135$ A1 for $\frac{45}{2}$ or 22.5
5			Correct region shaded	3	M1 for a circle centre M or N (accept arc of sufficient length to define the region) M1 for circle centre M radius 5 cm and circle centre N radius 3 cm (accept arc of sufficient length to define the region) A1 for correct region shaded

PAPER: 5MB31	H/01			
Question	Working	Answer	Mark	Notes
*6	9	Conclusion (supported)	4	M1 for $\pi \times 120^2$ (= 45 216 - 45 249) M1 for " $\pi \times 120^{2"}$ ÷ 1800 A1 for 25 - 25.2 C1 ft (dep on M2) for appropriate conclusion from their figures OR M1 for $\pi \times 120^2$ (= 45 216 - 45 249) M1 for 20 × 1800 A1 for 36 000 and 45 216 - 45 249 C1 ft (dep on M2) for appropriate conclusion from their figures OR M1 for $\pi \times 120^2$ (= 45 216 - 45 249) M1 for " $\pi \times 120^{2"}$ ÷ 20 A1 for 2260 - 2263 C1 ft (dep on M2) for appropriate conclusion from their figures OR M1 for 1800 × 20 M1 for 36 000 ÷ π (=11 457 - 11 465) A1 for 107(.0) C1 ft (dep on M2) for appropriate conclusion from their figures
7		161.50	5	M2 for a correct method to decrease 6720 by 20%, eg 6720 × 0.8 (= 5376) or 6720 × 0.2 (= 1344 and 6720 – 1344 (= 5376)) (M1 for a correct method to find 20% of 6720 eg 6720 × 0.2 or $\frac{20}{100}$ × 6720 (= 1344)) M1 for subtracting 1500 (= 3876) after a percentage calculation M1 "3876" ÷ 24 after the subtraction of 1500 A1 for 161.5(0)

PAPE	R: 5MB3	3H/01				
Ques	stion		Working	Answer	Mark	Notes
8		$\begin{array}{c} 3\\ 3.1\\ 3.2\\ 3.3\\ 3.4\\ 3.5\\ 3.6\\ 3.7\\ 3.8\\ 3.9\\ 4\\ 3.71\\ 3.72\\ 3.73\\ 3.74\\ 3.75\\ \end{array}$	42 45.(291) 48.(768) 52.(437) 56.(304) 60.(375) 64.(656) 69.(153) 73.(872) 78.(819) 84 69.6(14811) 70.(078848) 70.5(45117) 71.(013624) 71.4(84375)	3.7	4	B2 for a trial between 3 and 4 exclusive (B1 for a trial at 3 or 4) B1 for a different trial of $3.7 < x \le 3.75$ B1 (dep on at least one previous B1) for 3.7 NB. Trials should be evaluated to at least 2 sf truncated or rounded for values of x correct to 1 decimal place. Trials should be evaluated to at least 1 dp truncated or rounded for values of x correct to 2dp. NB No working scores 0 marks even if answer is correct
9				618	4	M1 for a method to find an area which is part of the cross section M1 (dep) for a complete method to find the total area of the cross section M1 (dep M1) for their cross sectional area × 12 A1 cao OR M1 for a method to find the volume of cuboid, $8 \times 8 \times 12$ (= 768) M1 for a method to find the volume of the triangular prism, $\frac{1}{2} \times 5 \times 5 \times 12$ (= 150) M1 (dep M2) for a complete method for the volume of the prism A1 cao

5MB	3H 01				
Qu	estion	Working	Answer	Mark	Notes
10	(a)		15.2	3	M1 for $12.7^2 + 8.3^2$ or $161.29 + 68.89$ or 230.18 M1 for $\sqrt{"(12.7^2 + 8.3^2)"}$ or $\sqrt{"161.29 + 68.89"}$ or $\sqrt{230.18}$ A1 for 15.2 or 15.17(168)
	(b)		16.1	3	M1 for $\sin 40^{\circ} = \frac{DE}{25}$ oe or $\frac{DE}{\sin 40} = \frac{25}{\sin 90}$ oe M1 for 25 sin 40° A1 for 16.1 or 16.06(969)
11	(a)		4.081	2	M1 for 8.875 or $\frac{71}{8}$ or 2.979or 4.08 A1 for 4.081 or 4.0809(5)
	(b)		4 × 10 ⁻³	2	M1 for 4×10^n , $n \neq -3$ or $a \times 10^{-3}$, $a \neq 4$ or 0.004 or 0.4×10^{-2} or 1/250 A1 cao
12			x < 2	2	M1 for an attempt to isolate x and number terms or multiply all terms by 2, or for $\frac{3}{2}x < 3$ or $-\frac{3}{2}x < -3$ or $x = 2$ A1 cao
13	(a)		0, 6, 4, -6	2	B2 for all values correct (B1 for any one value correct)
	(b)		Graph drawn	2	M1 ft (provided B1 in (a) for at least 6 points plotted correctly from their table A1 cao for correct curve drawn from $(-4, -6)$ to $(3, -6)$
	(c)		1.5 to 1.6 and -2.5 to -2.6	2	M1 for correct use $y = 2$ (may be implied by one correct estimate) or correct use of formula. A1 for 1.5 to 1.6 and -2.5 to -2.6

5MB3H 01				
Question	Working	Answer	Mark	Notes
14*	Sher Yas Old 19300 12560 New 20265 13502 Inc 965 942	Correct comparison (supported)	3	M1 for a correct method to calculate the population at the beginning of the 10 year period for at least one place. eg $\frac{20265}{1.05}$ (= 19 300) oe or $\frac{13502}{1.075}$ (= 12 560) oe A1 for 965 (Sherbury) and 942(Yaston) C1 (dep on M1) ft for statement comparing increases leading to conclusion based on two comparable amounts eg increase in Sherbury is greater than increase in Yaston
15	$20x + 10y = 356x - 10y = -48x = -\frac{1}{2}y = \frac{9}{2}OR12x + 6y = 2112x - 20y = -9626y = 117y = \frac{9}{2}x = -\frac{1}{2}$	$-\frac{1}{2}, \frac{9}{2}$	4	 M1 for a correct process to eliminate either variable (condone one arithmetic error) A1 cao for either x or y M1 (dep on M1) for correct substitution of found value into one of the equations or appropriate method after starting again (condone one arithmetic error) A1 cao OR M1 for full method to rearrange and substitute to eliminate either variable (condone one arithmetic error) A1 cao for either x or y M1 (dep on M1) for correct substitution of found value into one of the equations or appropriate method after starting again (condone one arithmetic error) A1 cao for either x or y M1 (dep on M1) for correct substitution of found value into one of the equations or appropriate method after starting again (condone one arithmetic error) A1 cao NB Trial and improvement methods score 0 marks unless both x and y are correct
16		226	2	M1 for angle $ABC = 180 - 67 (= 113)$ A1 cao OR M1 for obtuse angle $AOC = 2 \times 67 (= 134)$ A1 cao

5MB3H 01				
Question	Working	Answer	Mark	Notes
17		- 2.82, 19.82	3	M1 for $\frac{17 \pm \sqrt{(-17)^2 - 4 \times 1 \times -56}}{2 \times 1}$ (condone one sign error) or $\left(x - \frac{17}{2}\right)^2$ oe M1 for $\frac{17 \pm \sqrt{513}}{2}$ or for method leading to $\frac{17}{2} \pm \sqrt{\frac{513}{4}}$ oe A1 for answers in the range 19.82 to 19.825; -2.82 to -2.825
18		21.2	4	M1 for correct use of sine rule to find AB or BC, eg $\frac{6}{\sin 25} = \frac{AB}{\sin 120}$ or $\frac{6}{\sin 25} = \frac{BC}{\sin(180-120-25)}$ M1 for $(AB =) \frac{6}{\sin 25} \times \sin 120 (= 12.2(951))$ or $(BC =) \frac{6}{\sin 25} \times \sin 35 (= 8.1(431))$ M1(dep M2) for method to find area, eg $0.5 \times 6 \times "AB" \sin 35$ or $0.5 \times 6 \times "BC" \sin 120$ A1 for answer in the range $21.1 - 21.2$ OR (with perpendicular from A meeting BC extended at a point X) M1 for method to find BX M1 (dep M2) for $0.5 \times "AX" \times "BC"$ A1 for answer in the range $21.1 - 21.2$
*19		0.38 because the LB and UB agree to that number of figures	5	B1 for 10.75 or 10.85 or 10.84999 B1 for 75.055 or 75.065 or 75.064999 M1 for $\sqrt{\frac{10.85}{75.055}}$ as UB OR $\sqrt{\frac{10.75}{75.065}}$ as LB A1 (dep on all previous marks) for both 0.3802 and 0.3784 must clearly come from working with correct values C1 for 0.38 from 0.3784 and 0.3802 and "both LB and UB round to 0.38" NB An answer of 038(932) without working scores no marks

5MB3H_01				
Question	Working	Answer	Mark	Notes
20		7.35	3	M1 for $y \propto \frac{1}{\sqrt{x}}$ or $y = \frac{k}{\sqrt{x}}$ or $9 = \frac{k}{\sqrt{4}}$ M1 for $k = 9\sqrt{4}$ (=18) A1 for 7.35 or 7.348
*21		$\frac{2}{3}(7\mathbf{a} + 3\mathbf{b})$ and correct conclusion	4	M1 for correct vector for \overrightarrow{OY} , or \overrightarrow{AP} eg $(\overrightarrow{OY}) = \overrightarrow{OA} + \overrightarrow{AY}$, or $\overrightarrow{OY} = \overrightarrow{OA} + \frac{2}{3}\overrightarrow{AP}$ may include terms in a and b , eg. 6 a + \overrightarrow{AY} , 4 b + 4 a - b + \overrightarrow{PY} or $\overrightarrow{AP} = \overrightarrow{AO} + \overrightarrow{OB} + \overrightarrow{BP}$ or $-6\mathbf{a} + 4\mathbf{b} + 4\mathbf{a} - \mathbf{b}$ or $-2\mathbf{a} + 3\mathbf{b}$ M1 for $(\overrightarrow{AY}) = \frac{2}{3}\overrightarrow{AP}$ or $\frac{2}{3}(-6\mathbf{a} + 4\mathbf{b} + 4\mathbf{a} - \mathbf{b})$ or $\frac{2}{3}(-2\mathbf{a} + 3\mathbf{b})$ or $(\overrightarrow{PY} = \frac{1}{3}\overrightarrow{PA}$ or $\frac{1}{3}(-4\mathbf{a} + \mathbf{b} - 4\mathbf{b} + 6\mathbf{a})$ or $\frac{1}{3}(2\mathbf{a} - 3\mathbf{b})$ M1 for correct expression for \overrightarrow{OY} in terms of a and b , eg $\frac{14}{3}\mathbf{a} + 2\mathbf{b}$ C1 for $\frac{2}{3}(7\mathbf{a} + 3\mathbf{b})$ and " \overrightarrow{OY} is parallel to the vector $7\mathbf{a} + 3\mathbf{b}$ " oe

PMT

Modifications to the mark scheme for Modified Large Print (MLP) papers.

Only mark scheme amendments are shown where the enlargement or modification of the paper requires a change in the mark scheme.

The following tolerances should be accepted on marking MLP papers, unless otherwise stated below: Angles: $\pm 5^{\circ}$ Measurements of length: ± 5 mm

PAPER	: 5MB3	H_01	
Ques	stion	Modification	Notes
Q2	(a)	Grid enlarged. Shading changed to dotty shading. Labels added to shapes. Image labelled shape A. Rotation given and labelled shape B. Question changed to 'Describe fully the single transformation which maps shape A to shape B. One row top and bottom, one column left and right has been removed. Three answer lines given.	2 cao (B1 for correct orientation in third quadrant or correct quarter turn)
Q2	(b)	Grid enlarged. Shading changed to dotty shading. Labels added next to the triangles 'triangle P' and 'triangle Q'. One column removed from the left.	B1 for enlargement B1 for scale factor 4 B1 for centre (0, 1)

PAPER: 5MB	3H_01	
Question	Modification	Notes
Q4	Diagram enlarged. MLP only – x changed to y. Braille only – measurements given in the text.	M1 for $4(x - 8) = 2x + 13$ M1 for expansion of bracket or division of all terms by 4, eg $4x - 32 = 2x + 13$, $x - 8 = 2x/4 + 13/4$ M1 for isolating x and number terms eg $2x = 45$, $x/2 = 45/4$ A1 for $45/2$ or 22.5 OR M1 for $(180 - 64) \div 2$ (= 58) M1 for $4(x - 8) = 58$ or $2x + 13 = 58$ M1 for isolating x and number terms eg $4x = 90$, $2x = 45$ A1 for $45/2$ or 22.5 OR M1 for $64 + 4(x - 8) + 2x + 13$ M1 for $64 + 4(x - 8) + 2x + 13 = 180$ M1 for isolating x and number terms eg $6x = 135$ A1 for $45/2$ or 22.5
Q5	Diagram kept the same size as original. Scale moved above the diagram and also put in the question paper.	B1 for circle centre M radius 5 cm B1 for circle centre N radius 3 cm B1 for correct region shaded

PAPER: 5MB	3H_01	
Question	Modification	Notes
Q6	Diagram enlarged. Cross changed to a filled in circle. Arrow heads removed.	M1 for $\pi \times 120^2$ (= 45238) M1 for " $\pi \times 120^{2"} \div 1800$ A1 for 25.0 – 25.2 C1 for "surface is large enough as 25 > 20" oe OR M1 for $\pi \times 120^2$ (= 45238) M1 for 20 × 1800 A1 for 36000 C1 for "surface is large enough as 36000 < 45238" oe OR M1 for $\pi \times r^2 = 1800 \times 20$ M1 for $36000 \div \pi$ (=11459) A1 for 107.0 C1 for "surface is large enough as 107< 120" oe
Q9	Model provided for all candidates. Diagram enlarged and provided for MLP.	 M1 for a method to find an area which is part of the cross section M1 (dep) for a complete method to find the total area of the cross section M1 (dep M2) for a complete method for the volume of the prism A1 cao OR M1 for a method to find the volume of cuboid, 8 × 8 × 12 M1 for a method to find the volume of the triangular prism M1 (depM2) for a complete method for the volume of the prism

PAPER: 5MB3H_01			
Question		Modification	Notes
Q10	(a)	Diagram enlarged. Braille only: measurements given in the text.	M1 for $12.7^2 + 8.3^2$ or $161.29 + 68.89$ or 230.18 M1 for $\sqrt{161.29 + 68.89}$ or $\sqrt{230.18}$ A1 for 15.2 or 15.17(168)
Q10	(b)	Diagram enlarged. Braille only – measurements given in the text.	M1 for sin $40^{\circ} = \frac{DE}{25}$ oe M1 for 25 sin 40° A1 for 16.1 or 16.06(969)
Q13	(a)	Wording added 'There are four spaces to fill.'	B2 for all values correct (B1 for any one value correct)
Q13	(b)	Grid enlarged.	M1 ft for at least 6 points plotted correctly from their table A1 cao for correct curve drawn from (-4, -6) to (3, -6)
Q16		Diagram enlarged. Dot added at centre.	M1 for angle ABC = $180 - 67$ (= 113) A1 cao OR M1 for obtuse angle AOC = 2×67 (= 134) A1 cao

PAPER: 5MB3H_01			
Question	Modification	Notes	
Q18	Diagram enlarged.	M1 for correct use of sine rule to find <i>AB</i> or <i>BC</i> , eg $\frac{6}{\sin 25} = \frac{AB}{\sin 120}$ M1 for $(AB =) \frac{6}{\sin 25} \times \sin 120$ or $(BC =) \frac{6}{\sin 25} \times \sin 35$ M1(dep M2) for method to find area, eg $0.5 \times 6 \times AB \sin 35$ or $0.5 \times 6 \times BC \sin 120$ A1 for answer in the range $21.1 - 21.2$ OR (with perpendicular from <i>A</i> meeting <i>BC</i> extended at a point <i>X</i>) M1 for method to find <i>AX</i> M1 for method to find <i>BX</i> M1(dep M2) for $0.5 \times "AX" \times "BC"$ A1 for answer in the range $21.1 - 21.2$	
Q21	Diagram enlarged.	M1 for correct vector for \overrightarrow{OY} , eg $(\overrightarrow{OY}) = \overrightarrow{OA} + \overrightarrow{AY}$, may include terms in a and b , eg. $6\mathbf{a} + \overrightarrow{AY}$, 4 b $+ 4\mathbf{a} - \mathbf{b} + \overrightarrow{PY}$ M1 for $(\overrightarrow{AY} =)\frac{2}{3}\overrightarrow{AP}$ or $(\overrightarrow{PY} =)\frac{1}{3}\overrightarrow{PA}$ M1 for correct expression for \overrightarrow{OY} in terms of a and b , eg $\frac{14}{3}\mathbf{a} + 2\mathbf{b}$ C1 for $\frac{2}{3}(7\mathbf{a} + 3\mathbf{b})$ and " \overrightarrow{OY} is parallel to the vector $7\mathbf{a} + 3\mathbf{b}$ " oe	

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