

1. The probability distribution of the random variable X is given by the formula

$$P(X = r) = k(r^2 - 1) \text{ for } r = 2, 3, 4, 5.$$

i. Show the probability distribution in a table, and find the value of k .

[3]

2. The probability distribution for the discrete random variable X is shown in Fig. 3.

x	0	1	2	3	4
$P(X = x)$	$0.4a$	$0.5a$	$0.3a$	$0.2a$	$0.1a$

Fig. 3

(a) Calculate the value of the constant a .

[2]

(b) Calculate $P(X \geq 2)$.

[2]

[1]

3. The probability distribution of the discrete random variable X is given in Fig. 4.

r	0	1	2	3	4
$P(X = r)$	0.2	0.15	0.3	k	0.25

Fig. 4

(a) Find the value of k .

[2]

X_1 and X_2 are two independent values of X .

(b) Find $P(X_1 + X_2 = 6)$.

[3]

4. The discrete random variable X takes the values $r = 0, 1, 2, 3, 4$ with probabilities

$$P(X = r) = k(r + 1)(r + 2).$$

(a) Calculate the value of the constant k . [2]

(b) Calculate $P(X < 3)$, giving your answer as a fraction in its lowest terms. [2]

5. Roxanne is employed by an employment agency called Supertemps. In any given week she may be required to work up to a maximum of 5 days.

Both Roxanne and her partner, Alex, suggest ways in which the number of days, X , Roxanne is required to work in a week may be modelled.

- Roxanne thinks that X may be modelled using the discrete uniform distribution.
- Alex suggests the following formula to model the probability distribution of X .

$$P(X = x) = k(2x - 5)^2 \text{ for } x = 0, 1, 2, 3, 4, 5.$$

(a) Calculate the value of k for Alex's model. [2]

Alex and Roxanne record the number of days Roxanne is required to work in each of the first 42 weeks of her employment. The results are summarised in Fig. 9.

Number of days	0	1	2	3	4	5
Frequency	13	7	1	0	7	14

Fig. 9


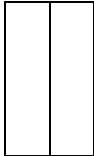
[6]

(b) Investigate how well each model fits the data.

END OF QUESTION paper

Mark scheme

Question	Answer/Indicative content	Marks	Part marks and guidance											
1	<table border="1" data-bbox="219 268 1072 384"> <tr> <td>r</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>$P(X=r)$</td> <td>$3k$</td> <td>$8k$</td> <td>$15k$</td> <td>$24k$</td> </tr> </table> <p data-bbox="219 427 432 451">i $3k + 8k + 15k + 24k = 1$</p> <p data-bbox="219 692 293 716">i $k = 0.02$</p>	r	2	3	4	5	$P(X=r)$	$3k$	$8k$	$15k$	$24k$	<p data-bbox="1137 320 1171 344">B1</p> <p data-bbox="1137 427 1171 451">M1</p> <p data-bbox="1137 692 1171 716">A1</p>	<p data-bbox="1234 301 1626 363">For correct table (to k or correct probabilities 0.06, 0.16, 0.30, 0.48)</p> <p data-bbox="1234 496 1447 555">or $k = 1/50$ (with or without working)</p> <p data-bbox="1234 603 1435 627">Examiner's Comments</p> <p data-bbox="1234 675 1644 916">Nearly all candidates were able to calculate the correct coefficients of k and sum the terms to get $50k$. Work was generally neatly presented and well structured. Only a very few candidates failed to get the correct answer of $1/50$. A small number of candidates did not show the probabilities in a table, thus losing 1 mark.</p>	<p data-bbox="1684 427 2056 451">For their four multiples of k added and = 1.</p> <p data-bbox="1684 675 2119 734">Allow M1A1 even if done in part (ii) – link part (ii) to part (i)</p>
r	2	3	4	5										
$P(X=r)$	$3k$	$8k$	$15k$	$24k$										
	Total	3												
2	<p data-bbox="219 1046 568 1070">$0.4a + 0.5a + 0.3a + 0.2a + 0.1a = 1$ soi</p> <p data-bbox="219 1177 309 1265">$a = \frac{2}{3}$</p>	<p data-bbox="1099 1038 1211 1062">M1(AO1.1b)</p> <p data-bbox="1099 1145 1211 1169">A1(AO1.1b)</p> <p data-bbox="1137 1257 1173 1281">[2]</p>	<table border="1" data-bbox="1234 1114 1323 1193"> <tr> <td></td> <td></td> </tr> </table>											
	<p data-bbox="219 1313 501 1401">$\frac{2}{3}(0.3 + 0.2 + 0.1)$</p>	<p data-bbox="1099 1334 1211 1358">M1(AO1.1b)</p>	<table border="1" data-bbox="1234 1310 1541 1441"> <tr> <td><i>their</i> $\frac{2}{3}$</td> <td></td> </tr> </table>	<i>their</i> $\frac{2}{3}$										
<i>their</i> $\frac{2}{3}$														

		0.4	A1(AO1.1b)		Discrete Probability Distributions
			[2]		
	c	positive skew	B1(AO1.2)		
			[1]		
		Total	2		
3	a	<div style="border: 1px solid black; padding: 5px; display: inline-block;"> $0.2 + 0.15 + 0.3 + k + 0.25 = 1$ </div> oe	M1(AO1.1)		
		$k = 0.1$	A1(AO1.1)		
			[2]	<u>Examiner's Comments</u> Candidates generally did this correctly, with many showing exactly the working given in the mark scheme.	
	b	k^2 seen $0.3 \times 0.25 \times 2 + k^2$ 0.16	M1(AO3.1a)	Or $0.3 \times 0.25 \times 2$ seen Allow slip eg omission of 2; or insertion of 2 Ft k from (a) for M1M1	
			M1(AO1.1)		
			A1(AO1.1)		
			[3]		

					<p><u>Examiner's Comments</u></p> <p>This part caused considerable difficulty, with some candidates omitting it, others drawing a possibility space with equally likely outcomes, and others copying information from the table given in the question.</p> <p>Candidates who realised that a total of 6 could be made either from 3 and 3 or else from 2 and 4 sometimes did not realise that 4 and 2 is also possible; others thought the probability of 3 and 3 had to be counted twice.</p>	Discrete Probability Distributions																
		Total	5																			
4	a	$k(1 \times 2 + 2 \times 3 + 3 \times 4 + 4 \times 5 + 5 \times 6) = 1$ $k = \frac{1}{70}$	M1 (AO1.1) A1 (AO1.1) [2]	<table border="1"><tr><td></td><td></td></tr></table>																		
	b	$\frac{2+6+12}{70}$ $= \frac{2}{7}$	M1 (AO1.1) A1 (AO1.1) [2]	<table border="1"> <tr> <td>FT their k</td> <td>Allow 1. $P(X \leq 3)$ method</td> </tr> </table>	FT their k	Allow 1. $P(X \leq 3)$ method																
FT their k	Allow 1. $P(X \leq 3)$ method																					
		Total	4																			
5	a	$k(25 + 9 + 1 + 1 + 9 + 25) = 1$ $k = \frac{1}{70}$	M1 (AO 3.3) A1(AO 1.1) [2]																			
	b	Roxannes model <table border="1"> <tr> <td>day</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>s</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> </table>	day	0	1	2	3	4	5	s								<table border="1"><tr><td></td><td></td></tr></table>				
day	0	1	2	3	4	5																
s																						

	<table border="1" data-bbox="219 76 913 124"> <tr> <td>f_e</td> <td>7</td> <td>7</td> <td>7</td> <td>7</td> <td>7</td> <td>7</td> </tr> </table> <p data-bbox="219 180 640 236">Correct for 1 and 4 days, but otherwise a poor fit Alexs model</p> <table border="1" data-bbox="219 272 896 408"> <tr> <td>day s</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>f_e</td> <td>15</td> <td>5.4</td> <td>0.6</td> <td>0.6</td> <td>5.4</td> <td>15</td> </tr> </table> <p data-bbox="219 568 1061 624">The expected frequencies are all within 2 of the observed frequencies, so Alex's model appears to be a good fit.</p>	f_e	7	7	7	7	7	7	day s	0	1	2	3	4	5	f_e	15	5.4	0.6	0.6	5.4	15	<p data-bbox="1104 89 1211 113">B1 (AO 3.4)</p> <p data-bbox="1126 161 1189 217">B1(AO 3.5a)</p> <p data-bbox="1104 304 1211 328">M1(AO 3.4)</p> <p data-bbox="1104 376 1211 400">A1(AO 1.1)</p> <p data-bbox="1104 448 1211 472">B1(AO 2.4)</p> <p data-bbox="1126 520 1189 576">B1(AO 3.5a)</p> <p data-bbox="1144 632 1171 655">[6]</p>	<table border="1" data-bbox="1238 76 1664 746"> <tr> <td data-bbox="1238 76 1451 746"> <p data-bbox="1238 552 1442 738">A0 if expected frequencies are rounded to nearest integer</p> </td> <td data-bbox="1451 76 1664 746"></td> </tr> </table>	<p data-bbox="1238 552 1442 738">A0 if expected frequencies are rounded to nearest integer</p>		<p data-bbox="1760 68 2145 92">Discrete Probability Distributions</p>
f_e	7	7	7	7	7	7																					
day s	0	1	2	3	4	5																					
f_e	15	5.4	0.6	0.6	5.4	15																					
<p data-bbox="1238 552 1442 738">A0 if expected frequencies are rounded to nearest integer</p>																											
	<p data-bbox="219 799 264 823">Total</p>	<p data-bbox="1144 799 1171 823">8</p>																									