

1. Maria planned a statistical investigation into trees of a certain variety. She wished to test whether there is positive linear correlation between the height of a tree and the circumference of its trunk at the base.

(a) State, with a reason, whether a 1-tail or a 2-tail test is more appropriate. [1]

Maria recorded the height and circumference of a random sample of 10 trees of this variety in a wood near her home. She calculated the product-moment correlation coefficient for her sample and found that the value was 0.642.

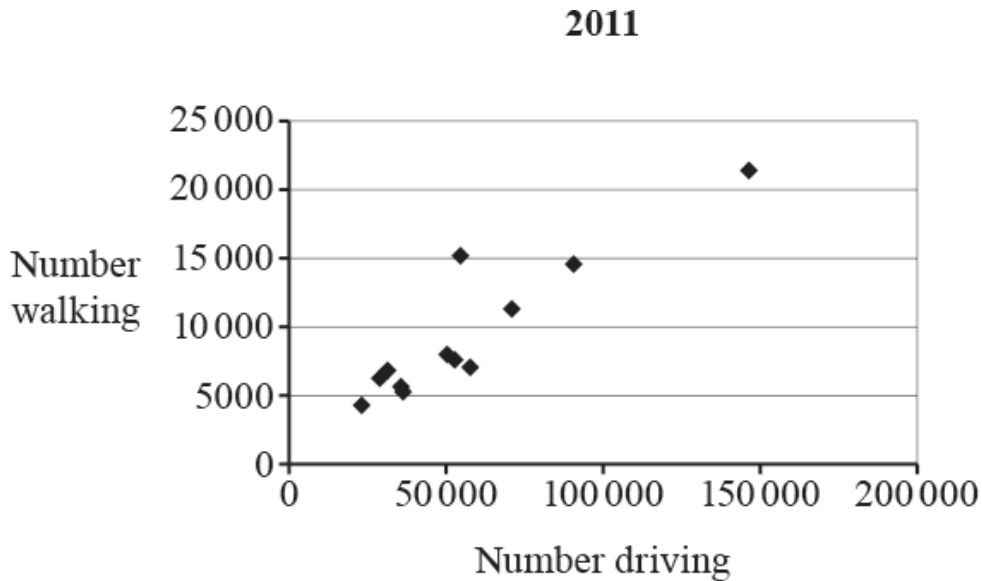
(b) Use the table below to carry out the test at the 2.5% significance level. [5]

(c) Give two reasons why it would not be appropriate to use Maria's results to draw a conclusion about all trees of this variety. [2]

**Critical values of Pearson's product-moment correlation coefficient.**

	1-tail test	5%	2.5%	1%	0.5%
	2-tail test	10%	5%	2.5%	1%
<i>n</i>	9	0.5822	0.6664	0.7498	0.7977
	10	0.5494	0.6319	0.7155	0.7646
	11	0.5214	0.6021	0.6851	0.7348
	12	0.4973	0.5760	0.6581	0.7079

2. The scatter diagram shows data, taken from the pre-release data set (see <http://www.ocr.org.uk/Images/308727-units-h230-and-h240-large-data-set-lds-sample-assessment-material.xlsx>), for several Local Authorities in one region of the UK in 2011. The diagram shows, for each Local Authority, the number of workers who drove to work, and the number of workers who walked to work.



- (a) Four students calculated the value of Pearson's product-moment correlation coefficient for the data in the diagram. Their answers were 0.913, 0.124,  $-0.913$  and  $-0.124$ . One of these values is correct. Without calculation state, with a reason, which is the correct value. [2]

- (b) Sanjay makes the following statement.

"The diagram shows that, in **any** Local Authority, if there are a large number of people who drive to work there will be a large number who walk to work."

Give a reason why this statement is incorrect. [2]

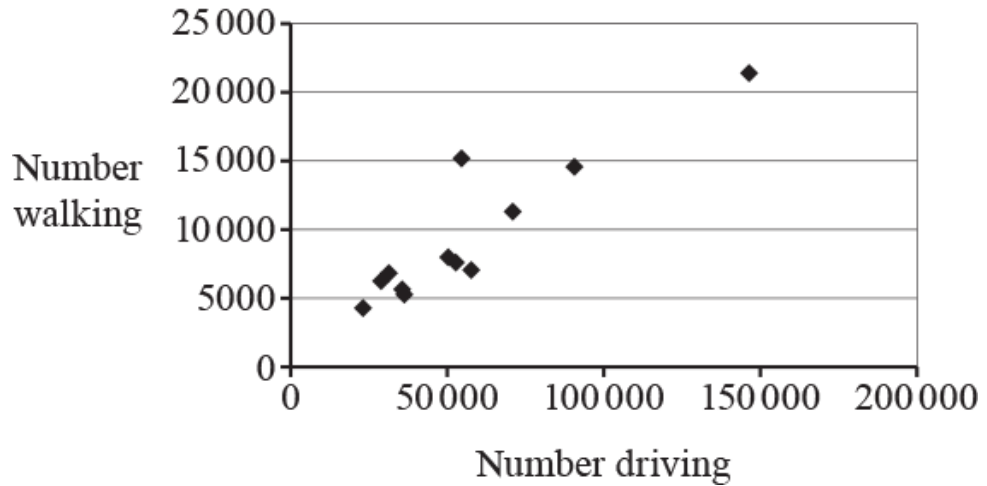
- (c) Rosie makes the following statement.

"The diagram must be wrong because it shows good positive correlation. If there are more people driving to work, there will be fewer people walking to work, so there would be negative correlation." [1]

Explain briefly why Rosie's statement is incorrect. [1]

- The diagram shows a fairly close relationship between the two variables. One point on (d) the diagram represents a Local Authority where this relationship is less strong than for the others. On the diagram below, label this point A. [1]

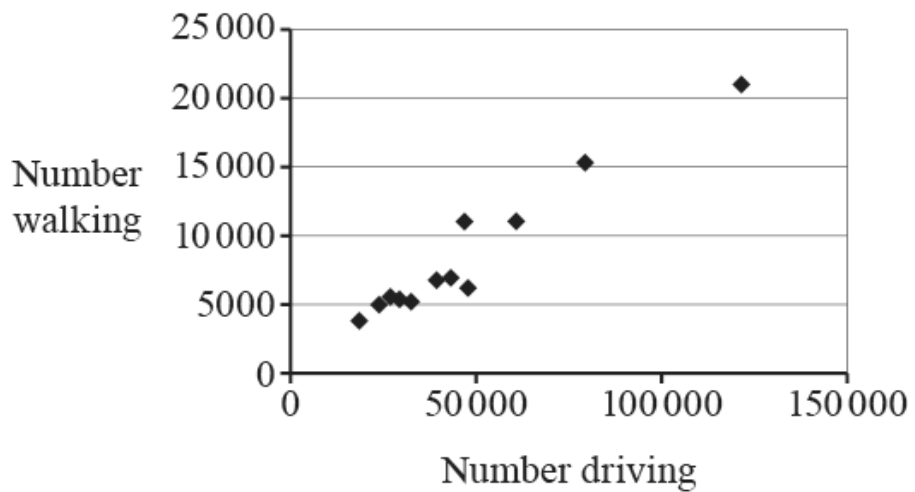
**2011**



- (e) Given that the point A represents a metropolitan borough, suggest a reason why the relationship is less strong for this Local Authority than for the others in the region. [1]

The scatter diagram below shows the corresponding data for the same region in 2001.

**2001**



- (f) (i) State a change that has taken place in the metropolitan borough represented by the point A between 2001 and 2011. [1]  
 (ii) Suggest a possible reason for this change. [1]

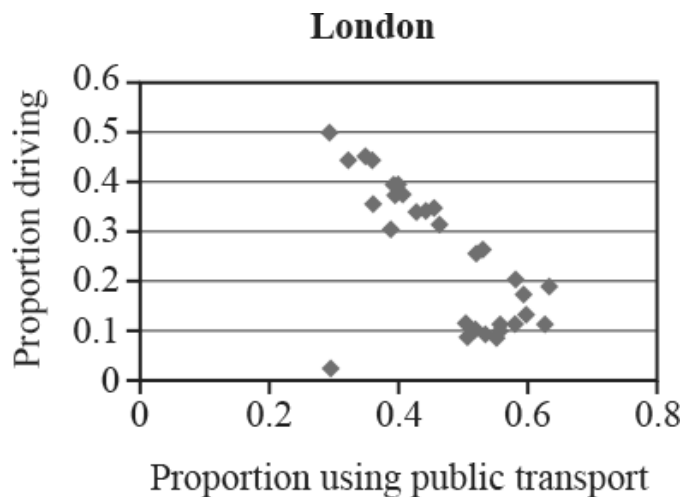
3. Christa used Pearson's product-moment correlation coefficient,  $r$ , to compare the use of public transport with the use of private vehicles for travel to work in the UK.

- (a) Using the pre-release data set for all 348 UK Local Authorities, she considered the following four variables.

Number of employees using public transport	$x$
Number of employees using private vehicles	$y$
Proportion of employees using public transport	$a$
Proportion of employees using private vehicles	$b$

- (i) Explain, in context, why you would expect strong, positive correlation between  $x$  and  $y$ . [1]
- (ii) Explain, in context, what kind of correlation you would expect between  $a$  and  $b$ . [2]

- (b) Christa also considered the data for the 33 London boroughs alone and she generated the following scatter diagram.



One London Borough is represented by an outlier in the diagram.

- (i) Suggest what effect this outlier is likely to have on the value of  $r$  for the 32 London Boroughs. [1]
- (ii) Suggest what effect this outlier is likely to have on the value of  $r$  for the whole country. [1]
- (iii) What can you deduce about the area of the London Borough represented by the outlier? Explain your answer. [1]

4. In an experiment involving a bivariate distribution ( $X, Y$ ) a random sample of 7 pairs of values was obtained and Pearson's product-moment correlation coefficient  $r$  was calculated for these values.

The value of  $r$  was found to be 0.894. Use the table below to test, at the 5% significance level,

- (a) whether there is positive linear correlation in the population, stating your hypotheses and conclusion clearly.

[5]

1-tail test	5%	2.5%	1%	0.5%
2-tail test	10%	5%	2%	1%
$n$				
1	—	—	—	—
2	—	—	—	—
3	0.9877	0.9969	0.9995	0.9999
4	0.9000	0.9500	0.9800	0.9900
5	0.8054	0.8783	0.9343	0.9587
6	0.7293	0.8114	0.8822	0.9587
7	0.6694	0.7545	0.8329	0.9745
8	0.6215	0.7067	0.7887	0.8343
9	0.5882	0.6664	0.7498	0.7977
10	0.5494	0.6319	0.7155	0.7646

Scatter diagrams for four sets of bivariate data, are shown.

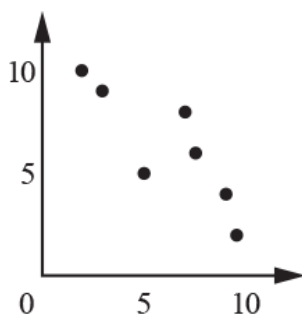


Diagram A

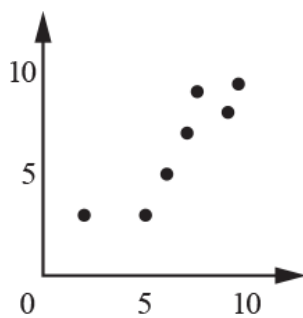


Diagram B

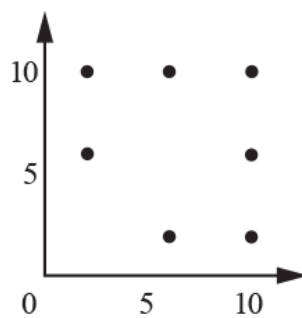


Diagram C

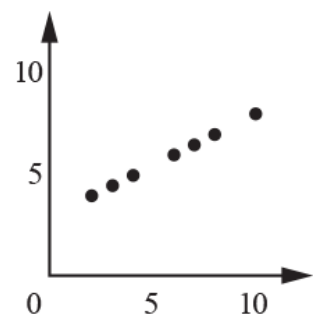


Diagram D

It is given that  $r = 0.894$  for **one** of these diagrams.

- (b) For each of the **other** diagrams, state how you can tell that  $r \neq 0.894$ .

[3]

5. Laxmi wishes to test whether there is linear correlation between the mass and the height of adult males.

(a) State, with a reason, whether Laxmi should use a 1-tail or a 2-tail test. [1]

Laxmi chooses a random sample of 40 adult males and calculates Pearson's product-moment correlation coefficient,  $r$ . She finds that  $r = 0.2705$ .

(b) Use the table below to carry out the test at the 5% significance level. [5]

Critical values of Pearson's product-moment correlation coefficient.

	1-tail test	5%	2.5%	1%	0.5%
	2-tail test	10%	5%	2.5%	1%
$n$	38	0.2709	0.3202	0.3760	0.4128
	39	0.2673	0.3160	0.3712	0.4076
	40	0.2638	0.3120	0.3665	0.4026
	41	0.2605	0.3081	0.3621	0.3978

END OF QUESTION paper

# Mark scheme

Question			Answer/Indicative content	Marks	Guidance			
1		a	1-tail. Testing for "positive" linear correlation	E1(AO 3.1b) [1]	or Expect larger circumference to go with larger height oe			
		b	$H_0: \rho = 0$ $H_1: \rho > 0$ where $\rho$ is lin correlation coeff in pop Comp 0.642 with 0.6319 Reject $H_0$ . There is evidence of +ve (linear) corr'n between height & circ of trees of this variety (in this wood)	B1(AO1.1) B1(AO2.5) M1(AO1.1) M1(AO1.1) A1(AO2.2b) [5]	B1B0 for 1 error, eg undefined $\rho$ or 2-tail In context, not definite.	Allow omission of "linear" throughout Allow without "linear" and / or "in this wood"		
		c	eg sample is small conditions in other areas may be different	E1(AO 3.5a) E1(AO 3.5a) [2]	<table border="1" style="width: 100%; height: 100%;"> <tr> <td style="width: 50%;"></td> <td style="width: 50%;"></td> </tr> </table>			
<b>Total</b>				8				
2		a	Points close to straight line with +ve gradient Hence 0.913 is the correct value	B1(AO 2.4) B1(AO 2.2b) [2]	Dep on 1st B1			

		b	Sample is from one area, hence not random oe	E2(AO 2.3 2.2b)  [2]	Or might be different relationship elsewhere	Allow E1 for "Sample is small"				
		c	Both depend on the size (of the pop) of area.	E1(AO 2.4)  [1]	<table border="1" style="width: 100px; height: 30px;"><tr><td style="width: 50px;"></td><td style="width: 50px;"></td></tr></table>					
		d	Correct point indicated (54200, 15300)	B1(AO 3.2b)  [1]	<table border="1" style="width: 100px; height: 30px;"><tr><td style="width: 50px;"></td><td style="width: 50px;"></td></tr></table>					
		e	More local jobs (so higher proportion walk)	E1(AO 2.2b)  [1]	Any sensible equivalent,					
		f	<table border="1" style="width: 100%;"><tr><td style="width: 50px; text-align: center;">(i)</td><td>Eg Fewer walk to work</td></tr></table>	(i)	Eg Fewer walk to work	E1(AO 2.2b)  [1]				
(i)	Eg Fewer walk to work									
		<table border="1" style="width: 100%;"><tr><td style="width: 50px; text-align: center;">(ii)</td><td>Eg Some businesses within the borough have closed down or have moved to the outskirts</td></tr></table>	(ii)	Eg Some businesses within the borough have closed down or have moved to the outskirts	E1(AO 2.2b)  [1]					
(ii)	Eg Some businesses within the borough have closed down or have moved to the outskirts									
		<b>Total</b>		<b>9</b>						
3		a	<table border="1" style="width: 100%;"><tr><td style="width: 50px; text-align: center;">(i)</td><td>Both the number of employees using public transport and the number of employees using private vehicles depend on the LA population.</td></tr><tr><td style="width: 50px; text-align: center;">(ii)</td><td>Negative If a large prop use public transport then a smaller</td></tr></table>	(i)	Both the number of employees using public transport and the number of employees using private vehicles depend on the LA population.	(ii)	Negative If a large prop use public transport then a smaller	E1 (AO 2.1)  [1]           E1Ind (AO 2.2b)	or similar, but must be in context. Ignore all else	NOT No. using pt is prop to no. using pv
(i)	Both the number of employees using public transport and the number of employees using private vehicles depend on the LA population.									
(ii)	Negative If a large prop use public transport then a smaller									
					<p><b>Examiner's Comments</b></p> <p>Most candidates answered correctly, showing a good understanding of the difference between this part and part (a)(ii). A few, however, wrote that as the number of employees using public transport increases, the number using private will decrease.</p>					
					Ignore "strong" or "slight" etc	NOT Inverse prop'n				



			prop drive (and vice versa)	E1ind (AO 2.4)  [2]	<table border="1"> <tr> <td>or similar in context</td> <td>NOT "as a increases <i>b</i> decreases" unless in context</td> </tr> </table> <p><u>Examiner's Comments</u></p> <p>Many candidates understood the point, although some of these worded their answers badly, referring to the "numbers" (rather than "proportions") using the two types of transport, without making it clear that they were discussing each individual LA rather than all LAs together.</p>	or similar in context	NOT "as a increases <i>b</i> decreases" unless in context
or similar in context	NOT "as a increases <i>b</i> decreases" unless in context						
	b	(i)	Decrease the size of <i>r</i> or Make <i>r</i> less negative	E1 (AO 2.2b)  [1]	<table border="1"> <tr> <td>Make (value of ) <i>r</i> increase <i>r</i> closer to 0 Ignore eg "greatly" Ignore all else</td> <td>NOT Make <i>r</i> decrease NOT Weaken the corr'n NOT Make corr'n less</td> </tr> </table> <p><u>Examiner's Comments</u></p> <p>Some candidates stated that <i>r</i> would decrease, or that the value of <i>r</i> would decrease, both of which are incorrect. It is possible that what they meant was that the <u>size</u> of <i>r</i> would decrease, which is correct, but unfortunately these candidates could not be credited the mark. Some candidates ensured that there was no ambiguity by saying that <i>r</i> would "become less negative" or "move closer to 0" or "decrease in magnitude". Some candidates gave inadequate answers such as "It will weaken the correlation" or "It will weaken the value of <i>r</i>". There were a few irrelevant answers such as "The outlier will skew the distribution."</p>	Make (value of ) <i>r</i> increase <i>r</i> closer to 0 Ignore eg "greatly" Ignore all else	NOT Make <i>r</i> decrease NOT Weaken the corr'n NOT Make corr'n less
Make (value of ) <i>r</i> increase <i>r</i> closer to 0 Ignore eg "greatly" Ignore all else	NOT Make <i>r</i> decrease NOT Weaken the corr'n NOT Make corr'n less						
		(ii)	Little effect (because the population of the LA is small compared with the whole population)	E1 (AO 2.2b)  [1]	<table border="1"> <tr> <td>or No effect or similar Ignore all else</td> <td></td> </tr> </table> <p><u>Examiner's Comments</u></p> <p>Many good answers were seen.</p>	or No effect or similar Ignore all else	
or No effect or similar Ignore all else							
		(iii)	Ignore all reference to public transport <u>Type 1 answers</u> People don't travel far to work	E1 (AO 2.4)	<table border="1"> <tr> <td><u>Type 2 answers</u> Any suggested</td> <td></td> </tr> </table>	<u>Type 2 answers</u> Any suggested	
<u>Type 2 answers</u> Any suggested							

			Jobs are close High proportion walk (or cycle)	[1]	<p>reason why few drive eg Few garages; Parking expensive or similar in context</p> <p>NOT just Few drive</p>
			<b>Total</b>	<b>6</b>	
4	a		<p><math>H_0</math>: There is no linear correlation between <math>X</math> and <math>Y</math></p> <p><math>H_1</math>: There is positive linear correlation between <math>X</math> and <math>Y</math></p> <p>Compare with 0.6694</p> <p>Reject <math>H_0</math></p> <p>There is evidence of positive linear correlation between <math>X</math> &amp; <math>Y</math></p>	<p>B1 (AO1.1)</p> <p>B1 (AO2.5)</p> <p>B1 (AO1.1)</p> <p>M1 (AO1.1)</p> <p>A1 (AO2.2b) [2]</p>	<p>B1B0 for one error,</p> <p>eg omission of "linear" OR "+ve"</p> <p>Or <math>\rho = 0</math></p> <p>Or <math>\rho &gt; 0</math></p> <p>In context, not definite</p>
	b		<p>A: Negative (linear) correlation</p> <p>C: No (linear) correlation</p> <p>D: <math>r = 1</math></p>	<p>E1 (AO1.2)</p> <p>E1 (AO2.2a)</p> <p>E1 (AO1.2) [3]</p>	<p>or points not close to straight line, or <math>r = 0</math></p> <p>Allow without "linear"</p> <p>Allow without "linear"</p>

Hypothesis Testing using Pearson's Correlation Coefficient

					Not "r small" or "poor correlation"	
			<b>Total</b>	<b>8</b>		
5		a	1-tail, because expect mass and height to be positively correlated	B1 (AO 1.1) [1]	1-tail because generally expect taller people to be heavier	or equivalent
		b	$H_0: \rho = 0$ $H_1: \rho > 0$ where $\rho$ is pmcc for population comp 0.2638 Reject $H_0$ There is evidence that the mass and height of adult males are positively correlated	B1 (AO 1.1) B1 (AO 2.5) B1 (AO 1.1) M1 (AO 2.2b) A1 (AO 3.5a) [5]	Omit definition of $\rho$ : B1B0	
			<b>Total</b>	<b>6</b>		