(1)

(e)

(a)	Describe	now a stratified sample	e of 200 staff could be tal	CII.
(b)	Explain a	an advantage of using a	ı stratified sample rather t	han a simple random sample
			and an independent random The results are summaris Mean score (\bar{x})	Variance of
		F. 11	52	scores (s ²)
		Full time staff Part time staff	52	19
	L			

After all the staff had completed a training course the 80 full time staff and the 80 part time staff were given another test of policy awareness. The value of the test statistic z was 2.53

State an assumption you have made in carrying out the test in part (c).

(f) Comment on the awareness of company policy for the full time and part time staff in light of this result. Use a 1% level of significance. (2)

	(g)	Interpret yo	ur answers to j	part (c) and par	t (f).		(Total 17 marks	1) s)
2.		0 names fron	n the directory				systematic sample	2)
	(b)	Give one ad	lvantage and o	ne disadvantag	e of			
		(i) quota	sampling,					
		(ii) system	matic sampling	g.			(Total 6 marks	4) s)
3.	distri	buted. A rand		5 ropes is take		bing ropes are no th, in metres, of		
		120.3	120.1	120.4	120.2	119.9		
	(a)		nbiased estima ced by the con		n and the varia	ance of the lengt	hs of the climbing	5)
	wants	s to make sur	e that there is	a probability of	at least 0.90 t	eviation of 0.2 m hat the estimate of its true value	of the population	
	(b)	Find the min	nimum sample	size required.			(Cotal 11 marks	6) s)

4.	A researcher is hired by a cleaning company to survey the opinions of employees on a proposed
	pension scheme. The company employs 55 managers and 495 cleaners.

To collect data the researcher decides to give a questionnaire to the first 50 cleaners to leave at the end of the day.

(a) Give 2 reasons why this method is likely to produce biased results.

(2)

- (b) Explain briefly how the researcher could select a sample of 50 employees using
 - (i) a systematic sample,
 - (ii) a stratified sample.

(6)

Using the random number tables in the formulae book, and starting with the top left hand corner (8) and working across, 50 random numbers between 1 and 550 inclusive were selected. The first two suitable numbers are 384 and 100.

(c) Find the next two suitable numbers.

(2)

(Total 10 marks)

- **5.** Describe one advantage and one disadvantage of
 - (a) quota sampling,

(2)

(b) simple random sampling.

(2)

(Total 4 marks)

6. A school has 15 classes and a sixth form. In each class there are 30 students. In the sixth form there are 150 students. There are equal numbers of boys and girls in each class. There are equal numbers of boys and girls in the sixth form. The head teacher wishes to obtain the opinions of the students about school uniforms.

Explain how the head teacher would take a stratified sample of size 40.

(Total 7 marks)

7.	(a)	State two reasons why stratified sampling might be chosen as a method of sample carrying out a statistical survey.	ing when
			(2)
	(b)	State one advantage and one disadvantage of quota sampling.	(2) (Total 4 marks)
8.	There	e are 64 girls and 56 boys in a school.	
	Expla	ain briefly how you could take a random sample of 15 pupils using	
	(a)	a simple random sample,	(3)
	(b)	a stratified sample.	(3) (Total 6 marks)
9.	-	ain briefly what you understand by	
	(a)	a statistic,	(2)
	(b)	a sampling distribution.	(2) (Total 4 marks)

(2)

10.	Exp	lain how to obtain a sample from a population using	
	(a)	stratified sampling,	(2)
	(b)	quota sampling.	(2)
	Give	e one advantage and one disadvantage of each sampling method. (Total 8 ma	(4) arks)
11.		ag contains a large number of coins of which 30% are 50p coins, 20% are 10p coins and the are 2p coins.	
	(a)	Find the mean μ and the variance σ^2 of this population of coins.	(4)
	A ra	ndom sample of 2 coins is drawn from the bag one after the other.	
	(b)	List all possible samples that could be drawn.	(2)
	(c)	Find the sampling distribution of \overline{X} , the mean of the coins drawn.	(4)
	(d)	Find $P(2 \le \overline{X} < 7)$.	

(e) Use the sampling distribution of \overline{X} to verify $E(\overline{X}) = \mu$ and $Var(\overline{X}) = \frac{1}{2} \sigma^2$. (5) (Total 17 marks)

1. Label full time staff 1 - 6000, part time staff 1 - 4000 M1

Use random numbers to select

M1

Simple random sample of 120 full time staff and 80 part time staff

A1

3

Note

- 1st M1 for attempt at labelling full-time and part-time staff. One set of correct numbers.
- 2nd M1 for mentioning use of random numbers
- 1st A1 for s.r.s. of 120 full-time and 80 part-time
- Enables estimation of statistics / errors for each strata or "reduce (b) **B**1 1 variability" or "more representative" or "reflects population structure" NOT "more accurate"
- (c) $H_0: \mu_f = \mu_p, H_1: \mu_f \neq \mu_p$ (accept μ_1, μ_2) s.e. = $\sqrt{\frac{21}{80} + \frac{19}{80}}$, $z = \frac{52 - 50}{\sqrt{\frac{21}{80} + \frac{19}{80}}} = (2\sqrt{2})$ M1, M1

$$= 2.828...$$
 (awrt **2.83**) A1

Two tailed critical value z = 2.5758 (or prob of awrt 0.002 (<0.005) **B**1 or 0.004 (<0.01)) [2.828 > 2.5758 so] significant evidence to reject H_0 dM1 There is evidence of a difference in policy awareness between full A1ft 7 time and part time staff

Note

- 1st M1 for attempt at s.e. – condone one number wrong. NB correct s.e. $=\sqrt{\frac{1}{2}}$
- 2^{nd} M1 for using their s.e. in correct formula for test statistic. Must be $\frac{\pm (52 - 50)}{\sqrt{\frac{p}{q} + \frac{r}{s}}}$
- 3rd dM1 dep. on 2nd M1 for a correct statement based on their normal cv and their test statistic
- 2nd A1 for correct comment in context. Must mention "scores" or "policy awareness" and types of "staff". Award A0 for a one-tailed comment. Allow ft
- Can use mean full time and mean part time **B**1 ~ Normal **B**1 2

Note

for mention of mean(s) or use of \overline{X} , provided \overline{X} clearly 1st B1 refers to full-time or part-time

2nd B1 for stating that distribution can be assumed normal e.g. "mean score of the test is normally distributed" gets B1B1 Have assumed $s^2 = \sigma^2$ or variance of sample = variance of population (e) 1 2.53 < 2.5758, not significant <u>or</u> do not reject H₀ (f) M1So there is insufficient evidence of a difference in mean awareness A1ft 2 Note M1 for correct statement (may be implied by correct contextualised comment) **A**1 for correct contextualised comment. Accept "no difference in mean scores". Allow ft Training course has closed the gap between full time staff and part B1 1 (g) time staff's mean awareness of company policy. **Note** for correct comment in context that implies training was effective. This must be supported by their (c) and (f). Condone one-tailed comment here. [17]

2. (a) Randomly select a number between 00 and 499 (001 and 500) B1 select every 500th person B1 2

Note

1st B1 for idea of using random numbers to select the first from1 – 500 (o.e.)

2nd B1 for selecting every 500th (name on the list)

If they are clearly trying to carry out

stratified sample then score B0B0

B1

2

(b) (i	i)	Quota Adantage: Representative sample can be achieved (with small sample size) Cheap (costs kept to a minimum) not "quick" Administration relatively easy	B1	
		Disadvantage		
		Not possible to estimate sampling errors (due to lack of randomness)		
		Not a random process	B1	2
		Judgment of interviewer can affect choice of sample $-$ <u>bias</u>		
		Non-response not recorded		
		Difficulties of defining controls e.g. social class		
		Note		
		Score B1 for any one line		
		1 st B1 for Quota advantage		
		2 nd B1 for Quota disadvantage		
(:	ii)	Systematic		
		Advantage:	B1	
		Simple or easy to use not "quick" or "cheap" or "efficient"		

Only random if the ordered list is (truly) random

It is suitable for large <u>samples</u> (not populations)

Requires a list of the population <u>or</u> must assign a number to each member of the pop.

<u>Note</u>

Disadvantage

Score B1 for any one line

1st B1 for Systematic Advantage

2nd B1 for Systematic Disadvantage

[6]

3. (a) Estimate of Mean =
$$\frac{600.9}{5}$$
 = 120.18 M1A1

Estimate of Variance =
$$\frac{1}{4} \{72216.31 - \frac{600.9^2}{5} \}$$

or
$$\frac{0.148}{4} = 0.037$$

A1ft A1 5

M1

<u>Note</u>

 $1^{\text{st}} M1$ for an attempt at Σx (accept 600 to 1sf)

$$1^{\text{st}} A1$$
 for $\frac{600.9}{5}$ = awrt 120 or awrt 120.2.

No working give M1A1 for awrt 120.2

2nd M1 for the use of a correct formula including a reasonable attempt at
$$\sum x^2$$
 (Accept 70 000 to 1sf) or $\sum (x - \overline{x})^2$ =0.15 (to 2 dp)

$$2^{\text{nd}}$$
 A1ft for a correct expression with correct $\sum x^2$ but can ft their mean (for expression – no need to check values if it is incorrect)

3rd A1 for 0.037 Correct answer with no working scores 3/3 for variance

(b)
$$P(-0.05 < \mu - \hat{\mu} < 0.05) = 0.90$$
 or $P(-0.05 < \overline{X} - \mu < 0.05)$
=0.90 [\le is OK]

$$\frac{0.05}{\frac{0.2}{\sqrt{n}}} = 1.6449$$
 M1 A1

$$n = \frac{1.6449^2 \times 0.2^2}{0.05^2}$$
 dM1

$$n = 43.29...$$
 A1

$$n = 44$$
 A1 6

<u>Note</u>

B1 for a correct probability statement or "width of 90% $CI = 0.05 \times 2 = 0.1$ "

1st B1 may be implied by 1st A1 scored or correct equation.

1st M1 for
$$\frac{0.05}{\frac{0.2}{\sqrt{n}}} = z$$
 value or $2 \times \frac{0.2}{\sqrt{n}} \times z = 0.1$

Condone 0.5 instead of 0.05 <u>or</u> missing 2 <u>or</u> 0.05 for 0.1 for M1

1st A1 for a correct equation including 1.6449

 2^{nd} dM1 Dependent upon 1^{st} M1 for rearranging to get $n = \dots$ Must see "squaring"

 2^{nd} A1 for n = awrt 43.3

 3^{rd} A1 for rounding up to get n = 44

Using e.g.1.645 instead of 1.6449 can score all the marks except the $1^{st}\,A1$

[11]

4. (a) Only cleaners – no managers i.e. not all types. OR Not a random sample B1g

1st 50 may be in same shift/group/share same views.

OR Not a random sample

(Allow "not a representative sample" in place of "not a random sample")

After 1st B1, comments should be in **context**, i.e. mention cleaners, managers, types of worker etc

1st B1g for one row

2nd B1h for both rows. "Not a random sample" only counts once. Score B1B0 or B1B1 or B0B0 on EPEN

- (b) (i) Label employees (1-550) or obtain an ordered list B1 Select <u>first</u> using <u>random numbers</u> (from 1-11) B1 Then select every 11^{th} person from the list B1
 - 1st B1 for idea of labelling or getting an ordered list. No need to see 1–550.
 - 2nd B1 selecting first member of sample using random numbers (1–11 need not be mentioned)

 3^{rd} B1 selecting every *n*th where n = 11.

[10]

5.

Label managers (1–55) and cleaners (1–495) (ii) M1Use random numbers to select... M1 ...5 managers and 45 cleaners A1 6 (c) 390, 372 (They must be in this order) B1, B1 2 1st M1 for idea of two groups and labelling both groups. (Actual numbers used not required) 2nd M1 for use of random numbers within each strata. Don't give for SRS from all 550. "Assign random numbers to managers and cleaners" scores M0M1 **A**1 for 5 managers and 45 cleaners. (This mark is dependent upon scoring at least one M) Advantages: (a) • does not require the existence of: a sampling frame a population list • <u>field work can be done quickly</u> as representative sample can be achieved with a small sample size • costs kept to a minimum (cheaply) administration relatively easy В1 non-response not an issue any one Disadvantages: not possible to estimate sampling errors interviewer choice and may not be able to judge easily / may lead to bias non-response not recorded **B**1 2 non-random process any one (b) Advantages: random process so possible to estimate sampling errors free from bias **B**1 any one

Disadvantages:

- not suitable when sample size is large
- <u>sampling frame required</u> which <u>may not exist</u> or may be difficult to construct for a large population

B1 2

any one

NO REPETITION / OPPOSITES

[4]

6. Total in School =
$$(15 \times 30) + 150 = 600$$

random sample of
$$\frac{30}{600} \times 40$$

(Use of
$$\frac{40}{their600}$$
)

= 2 from each of the 15 classes

A1

random sample of
$$\frac{150}{600} \times 40$$

Either

= 10 from sixth form;

A1

Label the boys in each class from 1-15 and the girls from 1-15. use random numbers to select 1 girl and 1 boy

B1

Label the have in the sinth form from 1 75 and the sinte from

B1 B1

Label the boys in the sixth form from 1-75 and the girls from 1-75. use random numbers to select <u>5</u> different boys and 5 different girls.

[7]

- 7. (a) Population divides into <u>mutually exclusive</u>; <u>groups</u> distinct strata
- B1; B1 2

- (b) Advantages
 - enables fieldwork to be done quickly
 - costs kept to a minimum
 - administration is relatively easy

B1

Any one

Disadvantages

- non-random so not possible to estimate sampling errors
- subject to possible interviewer bias

B1 2

- non-response not recorded

Any one

[4]

Edexcel Internal Review

12

8.	(a)	Allocate a number between 1 and N (or equiv) to each pupil.		M1		
		Use <u>random number tables</u> , <u>computer or calculator</u> to select 15 <u>d</u> numbers between 1 and 120 (or equiv).	ifferent	B1		
		Pupils corresponding to these numbers become the sample.		B1	3	
	(b)	Allocate numbers $1-64$ to girls and $1-56$ to boys. Idea of different sets for boys and girls		M1		
		Select $\frac{64}{120} \times 15 = 8$ random numbers between $1 - 64$ for girls		M1		
		attempt find no				
		Select 7 random numbers between $1 - 56$ for boys. <i>Both 7 and 8</i>		A1	3	
		Bom 7 ana 0				[6]
9.	(a)	A <u>random variable</u> ; that is, a function involving <u>no unknown quantities</u>	B1;	; B1	2	
	(b)	If all possible samples are taken; then their values will form a distribution called the sampling distribution	B1;	; B1	2	F 41
						[4]
10.	(a)	groups of the population	g/1h	B1		
		Sample sizes within strata in strict proportion to numbers in each strata in the population Advantage:		B1		
		More accurate estimate of variance of population mean	ny one	B1		
		Difficult if strata are large				
			ny one	B1	4	

Non-random sampling (b)

B1

from groups of the population

B1 dep

Advantage:

Representative sample can be achieved with small sample size

Cheap (costs kept to a minimum)

Administration relatively easy

Any one (not quick) B1

Disadvantage

Not possible to estimate sampling errors due to lack of randomness

Judgment of interviewer can affect choice of sample - bias OK

Non-response not recorded

Difficulties of defining controls e.g. social class

Any one B1

[8]

11. (a)
$$\mu 0.3 \times 50 + 0.2 \times 10 + 0.5 \times 2 = 18$$

 $\sigma^2 = (0.3 \times 50^2 + 0.2 \times 10^2 + 0.5 \times 2^2) - 18^2 = 448$

M1 A1

M1 A1

4

(2,2)(50,2)

(2,50)

either, -1 each missing pair

B2

2

(c)

$\frac{-}{x}$	2	6	10	26	30	50
$P(\overline{X} = \overline{x})$	0.25	0.2	0.04	0.3	0.12	0.09

All means, probabs multiplied, -1 each error

B1 M1 A2 4

(d)
$$P(2 \le \overline{X} < 7) = 0.25 + 0.2 = 0.45$$

M1 A1∫ 2

Probabilities of 2 and 6 added, 0.45

E(
$$\overline{X}$$
) = 2 × 0.25 + 6 × 0.2.... = 18 $\Sigma xP(X = x)$ from table, 18 M1 A1
Var(\overline{X}) = 2² × 0.25 + 6² × 0.2 + ... - 18² = 224 M1 A1

$$\Sigma x^2 P(X=x) - (theirs)^2$$
, 224

So E(
$$\overline{X}$$
) = 18 = μ and Var(\overline{X}) = 224 = $\frac{1}{2}\sigma^2$ as required. A1 5

[17]

1. Most candidates knew how to take a stratified sample by taking simple random samples in each stratum but they often forgot to describe how to label the members of the strata.

In (b) the commonest correct response was about the sample being more representative of the population but some missed the point and simply said that stratified sampling was "easier".

The calculation in part (c) was carried out very well by most candidates. There were few errors with the standard error and most correctly concluded that there was evidence of a difference in policy awareness between the types of staff.

In part (d) most knew that the Central Limit Theorem had something to do with the normal distribution but they did not mention that it was the mean scores of full time and part time staff that can be assumed to be normally distributed.

There were some correct responses to part (e) but many just mentioned independence despite this being given in the stem to part (c) of the question.

Most gave a correct conclusion in part (f) and some correctly inferred in the final part that the training course had been effective.

Some had the correct idea in part (g) although their conclusions went further than the evidence suggested: they claimed that the scores of the part time staff had increased, which may well be the case, but the evidence presented was only sufficient to conclude that the "gap" between policy awareness of the types of staff has been closed.

- 2. Most candidates realised that they would need to sample every 500th name on the list in part (a) but a number did not explain how to select the first member of their sample at random from the first 500 names. In part (b) it was clear that many candidates had learnt some standard reasons from a textbook and nearly everyone scored something here. A few candidates confused systematic and stratified sampling in (ii) but for the most part this question was answered quite well.
- 3. Most answered part (a) well with the calculations being clearly laid out. Part (b) caused many problems. Many only considered one "tail" so they effectively used $P(\overline{X} \mu < 0.05) = 0.90$, there realised that the calculations from a confidence interval were involved and equations involving $\frac{0.2}{\sqrt{n}} \times z$ appeared but they were not always correct. Some did muddle through to the

correct answer but there were few clearly set out solutions.

- 4. Questions of this type are usually quite challenging for candidates and examiners alike. Candidates should be aware of how many marks the examiner is seeking to award in each part of the question and try and ensure that they make that many independent points. The use of bullet points rather than continuous prose might help both candidates and examiners.
 - In part (a) a number of candidates missed the fact that the sample contained no managers. Most knew how to take a systematic sample and explained the need to label the employees and pick every 11th one but a mechanism for selecting the first one at random was often not mentioned. The stratified sampling procedure was well known too and usually applied to this situation quite well. Some lost a mark for failing to label the managers and cleaners or for not using random numbers when selecting the samples from each strata. Part (c) proved an easy two marks for those who knew how to use the random number tables and most did know!
- 5. In part (a) they usually scored well, but there were few completely correct answers. Many candidates had little to offer but regurgitated text book definitions.
- 6. Most candidates calculated that there were 600 students in the school and they used classes and gender as strata. The calculations to determine the number of boys and girls from each class and the sixth form were often carried out correctly although sometimes they forgot there were 15 classes and simply suggested that a sample of 15 boys and 15 girls was taken rather than one boy and one girl from each class. The commonest omission was a failure to explain how the samples were taken from each stratum: labelling and using random numbers. There were a good number of fully or almost fully correct solutions from candidates who appreciated the depth of explanation required for a 7 mark question.
- 7. Many candidates were unaware of the reasons for the use of stratified sampling but most could give one advantage and one disadvantage of quota sampling.
- **8.** Full marks were rarely gained on this question. In part (a) while most candidates realised that they needed to allocate numbers and use some form of random number generator many did not mention the need to choose 15 different numbers and use the pupils corresponding to these numbers. In part (b) candidates usually failed to allocate different sets of numbers to the boys and the girls. Many managed to gain two marks by working out that samples of 8 girls and 7 boys were needed.
- 9. Very few candidates scored full marks on this question. It would appear that many of them had not learnt the definitions. A common answer to part (a) was the definition of a statistical model and in part (b) the candidates confused sampling distributions with a sampling frame or with the main distributions such as a Binomial.

- **10.** The definition of stratified sampling was attempted well, but candidates usually missed 'non-random' in the definition of quota sampling. Too many answers were vague and features were confused with advantages / disadvantages.
- 11. The first two parts were done well, with many gaining 6 marks. Thereafter it was clear that candidates had not focussed on this area of the syllabus. Candidates had great difficulty generating the correct means and many did not even try. Probabilities were achieved with varying success, but even strong candidates confused themselves by finding the expectation and variance of a sum of random variables. The candidates who wrote down the correct sampling distribution often went on to get full marks.