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Mark Scheme (Results)

Summer 2013

GCE Statistics 3 (6691/01)

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

1. The total number of marks for the paper is 75.

2. The Edexcel Mathematics mark schemes use the following types of marks:

- **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- **A** marks: accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod – benefit of doubt
- ft – follow through
- the symbol $\surd$ will be used for correct ft
- cao – correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw – ignore subsequent working
- awrt – answers which round to
- SC: special case
- oe – or equivalent (and appropriate)
- dep – dependent
- indep – independent
- dp decimal places
- sf significant figures
- $*$ The answer is printed on the paper
- ⌐ The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.

6. If a candidate makes more than one attempt at any question:
   - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
   - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.

8. In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme.

Question Number	Scheme	Marks
1.		

Cholesterol Level	High	Low	
High	7.6	12.4	20
Low	30.4	49.6	80
	38	62	100

M1A1 (2)

H_0 : Cholesterol level is independent of intake of saturated fats(no association) B1

H_1 : Cholesterol level is not independent of intake of saturated fats (association) (1)

O	E	$\frac{(O-E)^2}{E}$	$\frac{O^2}{E}$
12	7.6	2.547… or $\frac{242}{95}$	18.947… or $\frac{360}{19}$
8	12.4	1.56129… or $\frac{242}{155}$	5.161… or $\frac{160}{31}$
26	30.4	0.6368… or $\frac{121}{190}$	22.236… or $\frac{845}{38}$
54	49.6	0.3903… or $\frac{121}{310}$	58.790… or $\frac{3645}{62}$

dM1 A1

$\sum\frac{(O-E)^2}{E}$=5.1358234.. or $\frac{1.2^2}{7.6}+\frac{8^2}{12.4}+\frac{26^2}{30.4}+\frac{54^2}{49.6}-100=5.14$ (awrt **5.14**) A1 (3)

$\nu=(2-1)(2-1)=1$ B1

$\chi^2_1(0.05)=3.841$ B1 (2)

5.14 > 3.841 so sufficient evidence to reject H_0 [Condone "accept H_1"] M1

Association between cholesterol level and saturated fat intake A1 (2)

Total 10

Notes

Minimum working use part marks: E_i (2), Hyp (1), 5.14 (3), 3.841 (2), Conclusion (2)

1st M1 for some use of $\frac{\text{Row Total}\times\text{Col.Total}}{\text{Grand Total}}$. May be implied by correct E_i

1st A1 for all expected frequencies correct. Allow M1A0 for E_i rounded to integers

1st B1 for both hypotheses. Must mention "cholesterol" and "fats" at least once
Use of "relationship" or "correlation" or "connection" is B0

2nd dM1 for at least 2 correct terms (as in 3rd or 4th column) or correct expressions with their E_i
Dependent on 1st M1 Accept 2sf accuracy for the M mark

2nd A1 for all correct terms. May be implied by a correct ans.(2 dp or better)
Allow truncation eg 2.54… 3rd A1 for awrt 5.14

2nd B1 for correct degrees of freedom (may be implied by a cv of 3.841)

3rd M1 for a correct statement linking their test statistic and their cv(cv could be 2.705 or > 3.5)
Contradictory statements score M0 e.g. "significant, do not reject H_0"

4th A1 for a correct comment in context - must mention "cholestorol" and "fats"
condone "relationship" or "connection" here but **not** "correlation".
e.g. "There is evidence of a relationship between cholesterol level and fat intake"
No follow through. If e.g hypotheses are the wrong way round A0 here.

Question Number	Scheme	Marks
2(a)	<table><tr><td>Uni</td><td>*A*</td><td>*B*</td><td>*C*</td><td>*D*</td><td>*E*</td><td>*F*</td><td>*G*</td><td></td></tr><tr><td>Staff-Stu</td><td>2</td><td>4</td><td>3</td><td>5</td><td>7</td><td>1</td><td>6</td><td></td></tr><tr><td>Satisfaction</td><td>3</td><td>2</td><td>6</td><td>4</td><td>5</td><td>1</td><td>7</td><td></td></tr><tr><td>[*d*]</td><td>–1</td><td>2</td><td>–3</td><td>1</td><td>2</td><td>0</td><td>–1</td><td></td></tr><tr><td>d^2</td><td>1</td><td>4</td><td>9</td><td>1</td><td>4</td><td>0</td><td>1</td><td>20</td></tr></table>	M1A1A1
	$r_s = 1 - \frac{6\times 20}{7(49-1)} = 0.642857....$ (accept $\frac{9}{14}$) (awrt **0.643)**	dM1A1
		(5)
(b)	H_0: $\rho = 0$	
	$H_{1:}$ $\rho \neq 0$ ($\rho > 0$)	B1
	Critical value is ± 0.7857(± 0.7143 for a one tailed test)	B1
	0.643<cv so insufficient evidence to reject H_0	
	There is insufficient evidence to suggest a (positive) correlation between staff-student ratio and satisfaction.	B1ft
		(3)
		Total 8

	Notes
(a)	1st M1 for an attempt to rank the staff-students ratio or satisfaction (at least 4 correct)
	1st A1 for correct rankings for both (one or both may be reversed)
	2nd A1 for $\sum d^2$ =20 or correct d^2 row (NB $\sum d^2 = 92$ for one set of reversed ranks)
	2nd dM1 for use of the correct formula, follow through their $\sum d^2$ (Dependent on 1st M1)
	If answer is not correct, a correct expression is required.
	3rd A1 If $\sum d^2$ = 20 for awrt 0.643 or if $\sum d^2$ =92 for awrt – 0.643 (accept $\pm\frac{9}{14}$)
(b)	1st B1 for both hypotheses in terms of ρ, one tail H_1 must be compatible with their ranking
	Hypotheses just in words e.g. "no correlation" score B0
	2nd B1 for cv of 0.7857 or 0.7143 for one-tailed test (accept ±)
	Their cv must be compatible with their H_1 which may be in words
	If hypotheses are the wrong way around this must be B0 but 3rd B1 is possible.
	3rd B1ft for a correct contextualised comment. Must mention "ratio" or "no. of students per member of staff" and "satisfaction"
	Follow through their r_s and their cv (provided it is |cv| <1)
	Don't insist on the word "positive" for a one-tailed test
	Use of "association" is B0
	Independent of 1st B1 so if $\|r_s\|$ > |cv| must say there is sufficient evidence of …….(o.e.)
	and if $\|r_s\|$ < |cv| must say insufficient evidence of … (o.e.) regardless of their hypotheses
	Contradictory statements score B0
	(This mark is just testing interpretation of comparison of their r_s and their cv)

Question Number	Scheme	Marks
3(a)i	**Quota Sampling:**	
e.g	Advantages: Fieldwork can be done **quick**ly, or administering the test is **easy**, or costs are kept to a minimum (**cheap**), or gives estimates for each course. or OK for large populations or sampling frame not required (o.e.)	
e.g	Disadvantages: **Non-random** process or not possible to estimate the sampling errors, or non response not recorded, or interviewer can introduce **bias** in sample choice. (o.e.)	B1
3(a)ii	**Stratified Sampling:**	
e.g.	Advantages: Can give accurate estimates as it is a **random** process, or gives estimates for each course or **representative** of [BUT not "proportional" to] the whole population. (o.e.)	
e.g.	Disadvantages: Sampling frame required, or strata may not be clear as some students overlap courses or not suitable for large populations. (o.e.)	B1
		(2)
3(b)	Total enrolments=1000 (may be implied by calculations)	B1
	Leisure and Sport= $\frac{420}{1000}\times 100 = 42$	M1
	Information Technology= $\frac{337}{1000}\times 100 = 33.7 = 34$	
	Health and Social Care= $\frac{200}{1000}\times 100 = 20$	
	Media Studies= $\frac{43}{1000}\times 100 = 4.3 = 4$	A1
		(3)
3(c)	The college's information system would be used to identify each student and which course they are enrolled on.	
	i.e. idea of **sampling frame** or **list** for **each course**.	B1
	Use of **random numbers** to select required number of students **from each course**	B1
		(2)
		Total 7

	Notes
	Do not penalise for lack of context in part (a)
(a)	1st B1 for an advantage and a disadvantage for quota sampling (must be 1st or labelled (i))
	2nd B1 for an advantage and a disadvantage for stratified sampling (2nd or labelled (ii))
	Do not allow opposite pairs e.g. "quicker/easier" for quota sampling and "takes a long time/more difficult" for stratified or quota "easy to use" but strat. "hard for large populations"
	Do not allow same reason for both e.g. "gives estimates for each course"
(b)	M1 for one correct calculation, ft their "1000"
	A1 for 42, 34, 20 and 4 only
(c)	1st B1 for some mention of a suitable sampling frame. Need not give the specific term but a suitable source of list is required for all students in each course.
	2nd B1 for mentioning use of random numbers or some random selection process for each course. If they are describing systematic sampling score B0 here

Question Number	Scheme	Marks
4 (a)	$\bar{x} = \dfrac{8\times1.5+12\times4+13\times5.5+9\times7+8\times10}{50} = \dfrac{274.5}{50} = 5.49$ **(*)**	B1cso
	$s^2 = \dfrac{8\times1.5^2+12\times4^2+13\times5.5^2+9\times7^2+8\times10^2}{49} - \dfrac{50}{49}5.49^2, = 6.88$ **(*)**	M1,A1cso
		(3)
(b)	$a = \quad 50\times \mathrm{P}(6 < X < 8) = 50\times \mathrm{P}(0.194.. < Z < 0.956..)$	M1
	a = 12.81 (tables) <u>or</u> 12.68 (calc)	A1
	$b = 50 - (28.85 + a)$ = 8.34 (tables) <u>or</u> 8.47 (calc)	A1ft
		(3)
(c)	H_0: Normal distribution is a good fit H_1: Normal distribution is not a good fit	B1
	Class / O / E / $\frac{O^2}{E}$ / $\frac{(O-E)^2}{E}$	M1
	0-3 / 8 / 8.56 / 7.4766… / 0.0366…	
	3-5 / 12 / 12.73 / 11.31186…. / 0.0418…	
	5-6 / 13 / 7.56 / 22.354497… / 3.9144…	A1
	6-8 / 9 / 12.68 or (12.81) / (6.32) ~ 6.38801.. / 1.0680...~ (1.13)	
	8-12 / 8 / (8.34) or 8.47 / 7.556080…~ (7.67) / (0.013) ~ 0.0260..	
	$\sum \frac{O^2}{E} - N = 5.087\ldots \sim 5.1400\ldots$ awrt **(5.09 ~ 5.14)**	A1
	$\nu = 5-3 = 2$ (for 5 – 3 or 2 can be implied by 5.991 seen)	B1
	$\chi^2_2(0.05) = 5.991$	B1
	5.09<5.991 so insufficient evidence to reject H_0	M1
	Normal distribution is a good fit.	A1 (8)
		Total 14

	Notes
(a)	B1cso for denominator of 50 and at least 3 products on num <u>or</u> 274.5 on num
	M1 for a correct expression with at least 3 correct products on num or $\frac{1844.25}{49} - \frac{1507.005}{49}$ <u>or</u> $\frac{337.245}{49}$ <u>or</u> $\left(\frac{7377}{200} - 5.49^2\right)\times\frac{50}{49}$ etc Allow 3sf accuracy
	A1cso for 6.88 with M1 scored and no incorrect working seen
(b)	M1 a full method for a or b using the normal dist. Correct use of (6), 8, 5.49 and $\sqrt{6.88}$ seen
	1st A1 for a in range 12.68 ~ 12.81 or b in range 8.34~ 8.47 or awrt these values
	2nd A1ft for 50 – 28.85 – their a (or b) (but requires M1). Allow awrt 3sf. Must add up to 50
(c)	1st B1 for both hypotheses. B0 if they include 5.49 or 6.88. Condone X~N(μ, σ^2) etc
	1st M1 for attempting $\frac{(O-E)^2}{E}$ or $\frac{O^2}{E}$, at least 3 correct expressions or values.
	1st A1 for at least 4 correct calcs - 3rd or 4th column. (2 dp or better and allow e.g. 7.47) Allow any value in the ranges for the last two rows.
	2nd A1 for a test statistic that is awrt 5.09 ~ 5.14. Award M1A1A1 if this is obtained.
	2nd M1 for a correct statement based on their test statistic (> 1) and their cv (> 3.8) Contradictory statements score M0 e.g. "significant" do not reject H_0.
	3rd A1 for a correct comment suggesting that normal model is suitable <u>or</u> manager's belief is correct. **No f t** . Condone mention of 5.49 or 6.88 here. Hypotheses wrong way round scores A0

Question Number	Scheme	Marks
5 (a)	Let $L \sim \mathrm{N}(50, 25)$ and $S \sim \mathrm{N}(15, 9)$	
	Let $X = L - (S_1 + S_2 + S_3)$	B1
	$\mathrm{E}(X) = 50 - 3\times 15 = 5$	B1
	$\mathrm{Var}(X) = 25 + 3\times 9 = 52$	M1A1
	$\mathrm{P}(X < 0) = \mathrm{P}\left(Z < \frac{-5}{\sqrt{52}}\right)$	dM1
	$= \mathrm{P}(Z < -0.693..)$	
	=0.244 or 0.2451 (tables) (awrt **0.244 ~ 0.245)**	A1
		(6)
(b)	Let $Y = L - 3S$	B1
	$\mathrm{E}(Y) = 50 - 3\times 15 = 5$	B1
	$\mathrm{Var}(Y) = 25 + 3^2 \times 9 = 106$	M1A1
	$\mathrm{P}(Y > 0) = \mathrm{P}\left(Z > \frac{-5}{\sqrt{106}}\right)$	dM1
	$= \mathrm{P}(Z > -0.4856..)$	
	=0.686 or 0.6879 (tables) (awrt **0.686 ~ 0.688)**	A1
		(6)
		Total 12

Notes

(a)

1st B1 for forming a suitable variable X explicitly seen. Do not give for $L - 3S$ but allow $L - (S + S + S)$

2nd B1 for $\mathrm{E}(X) = 5$ (or -5 if their X is defined the other way around)

1st M1 for an attempt at $\mathrm{Var}(X) = \mathrm{Var}(L) + 3\mathrm{Var}(S)$. Do not condone 5 for "25" or 3 for "9"

1st A1 for 52

2nd dM1 for attempting the correct probability and standardising with their mean and sd.
This mark is dependent on 1st M1 so if X is not being used or wrong variance score M0
If their method is not crystal clear then they must be attempting $\mathrm{P}(Z <$ -ve value)
or
$\mathrm{P}(Z >$ +ve value) i.e. their probability after standardisation should lead to a prob. < 0.5

2nd A1 for awrt 0.244 ~ 0.245

Correct ans. only scores 5/6 (or 6/6 if 1st B1) but must be clearly labelled as (a) or the first answer.

(b)

1st B1 for defining a new variable $[Y =] \pm (L - 3S)$. May be implied by a correct variance.

2nd B1 for $\mathrm{E}(Y) = 5$ (or -5 if their Y is defined as $Y = 3S - L$)

1st M1 for an attempt at $\mathrm{Var}(Y) = \mathrm{Var}(L) + 3^2\,\mathrm{Var}(S)$. Do not condone 5 for "25" or 3 for "9"

1st A1 for 106 only

2nd dM1 for attempting the correct probability and standardising with their mean and sd.
This mark is dependent on 1st M1 so if Y is not being used or wrong variance score M0
If their method is not crystal clear then they must be attempting $\mathrm{P}(Z >$ -ve value)
or
$\mathrm{P}(Z <$ +ve value) i.e. their probability after standardisation should lead to a prob. > 0.5

2nd A1 for an awrt 0.686 ~ 0.688

Correct answer only scores 6/6 but must be clearly labelled as (b) or the second answer.

Question Number	Scheme	Marks
6 (a)	$H_0 : \mu_{new} - \mu_{old} = 1$	B1
	$H_1 : \mu_{new} - \mu_{old} > 1$	B1
	$z = \dfrac{7 - 5.5 - 1}{\sqrt{\dfrac{0.5}{60} + \dfrac{0.75}{70}}} = 3.62254...$ (awrt **3.62**)	M1 A1A1 A1
	Critical value $z = 1.6449$ (allow $\pm$)	B1
	[3.62 >1.6449] so sufficient evidence to reject H_0	dM1
	Evidence that the mean yield of new variety is more than 1 kg greater than the old variety.	A1
		(9)
(b)	Mean yield is normally distributed	B1
	Sample size is large. Must state or imply that **in this case** sample size is large	B1
		(2)
		Total 11

	Notes
(a)	1st & 2nd B1 for hypotheses. Accept μ_1, μ_2 or μ_A, μ_B etc if there is some indication of which is which e.g. $A \sim N(\mu_A, 0.5)$
	1st M1 for an attempt at se. Condone switching 0.5 and 0.75 $\sqrt{\dfrac{0.5 \text{ or } 0.75}{60} + \dfrac{0.75 \text{ or } 0.5}{70}}$
	1st A1 for a correct expression for denominator of test statistic or 0.138… or $\sqrt{0.0190...}$
	2nd A1 for a correct numerator of test statistic (must have the -1)
	3rd A1 for awrt 3.62
	[Allow – 3.62 from numerator of 5.5 – 7 − − 1 and compatible H_1]
	3rd B1 for $\pm$ 1.6449 seen or
	probability of 0.0002 (tables) or 0.000145…(calc) [allow 0.0001]
	2nd dM1 dep. on 1st M1 for a correct statement based on their normal cv and their test statistic
	2nd A1 for correct comment in context. Must mention "yield" and "varieties" or "old" and "new" and "1"
	If second B mark is B0 award A0 here
ALT	**Pooled estimate:** If they calculate $s_p = \sqrt{0.41845...} = 0.64688...$ allow 1st M1, 1st A1 for expression (or awrt 0.114) and 2nd A1 if numerator correct but A0 for test statistic (4.39)
(b)	1st B1 for mention of mean (yield) and normal (distribution)
	2nd B1 for mention of sample (size) being large in this case

Question Number		Scheme	Marks
7	**(a)**	$\hat{\mu} = \bar{x} = \frac{33.29}{8} = 4.16125$ (awrt **4.16**)	B1
		$\hat{\sigma}^2 = s^2 = \frac{4.12^2 + 5.12^2 + ... - 8 \times \bar{x}^2}{7}$	M1
		$\hat{\sigma}^2 = s^2 = \frac{141.4035 - 138.528013}{7} = 0.41078...$ (awrt **0.411**)	A1
			(3)
	(b)	$\sum x = 33.29 + 32 \times 4.55 = 178.89,$ (awrt **179**)	B1
		$\sum x^2 = "141.4035" + 31 \times 0.25 + 32 \times 4.55^2 (= 811.6335)$ (awrt **812**)	M1A1
		Combined sample: $s^2 = \frac{811.6335 - \frac{178.89^2}{40}}{39} = 0.29724865...$ (awrt **0.297**)	M1A1
		$\frac{s}{\sqrt{n}} = \frac{\sqrt{0.297....}}{\sqrt{40}} = 0.0862$ (awrt **0.0862)**	M1A1
			(7)
	(c)	$\bar{x} \pm 1.96\frac{\sigma}{\sqrt{n}} = \frac{178.89}{40} \pm 1.96\frac{0.67}{\sqrt{40}}$	M1B1
		= (4.2646…, 4.67988…) awrt (**4.26**[or 4.265]**, 4.68**)	A1
			(3)
			Total 13

	Notes
(a)	M1 for an attempt at s^2: correct denom, clear attempt at $\sum x^2$ and ft their $\bar{x}$ Ans only 2/2
(b)	B1 for correct sum or mean or fully correct expression (accept mean = awrt 4.47) **May be in (c)** 1st M1 for their $141.4035 + 31 \times 0.25 + 32 \times 4.55^2$ or "141.4035" + 7.75+ 662.48 (accept 3sf) **Beware:** $32(0.25 + 4.55^2)$ + "141.4035" = awrt 812 but scores M0A0. 1st A1 for a fully correct expression (all to 3sf or better) or answer only = awrt 812 2nd M1 for a correct expression using their values 3rd M1 dependent on using a changed s^2 (not their 0.411 or 0.25) for $\frac{\sqrt{"0.297"}}{\sqrt{40}}$ This s^2 must be based on a combination of their 0.411 and 0.25 e.g. 0.661
(c)	M1 for $\bar{x} \pm z \times \frac{\sigma}{\sqrt{n}}$ for any z (> 1.5) and ft their $\bar{x}$ based on combining their 4.16 and 4.55, do not award for simply using 4.55 or their 4.16. Condone $\sigma = \sqrt{\text{their } 0.297}$ or their (b) B1 for z = 1.96 used in an attempt at a CI, may for example miss $\sqrt{n}$ A1 for both limits awrt 3sf. Allow lower limit of 4.265

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