

# Mark Scheme (Results) Summer 2010

GCE

GCE Statistics S3 (6691/01)

Edexcel is one of the leading examining and awarding bodies in the UK and throughout the world. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers.

Through a network of UK and overseas offices, Edexcel's centres receive the support they need to help them deliver their education and training programmes to learners.

For further information, please call our GCE line on 0844 576 0025, our GCSE team on 0844 576 0027, or visit our website at [www.edexcel.com](http://www.edexcel.com).

If you have any subject specific questions about the content of this Mark Scheme that require the help of a subject specialist, you may find our **Ask The Expert** email service helpful.

Ask The Expert can be accessed online at the following link:

<http://www.edexcel.com/Aboutus/contact-us/>

Summer 2010

Publications Code UA024774

All the material in this publication is copyright

© Edexcel Ltd 2010

### Hypothesis Tests (Final M1A1)

For an incorrect comparison (e.g. probability with z value) even with a correct statement and/or comment award M0A0

For a correct or no comparison with more than one statement one of which is false  
Award M0A0 (This is compatible with the principle above of contradictory statements being penalised)

Apply these rules to all questions



June 2010  
 Statistics S3 6691  
 Mark Scheme

Question Number	Scheme	Marks
Q1	<p><math>H_0: \mu = 80, H_1: \mu &gt; 80</math></p> $z = \frac{83 - 80}{\frac{15}{\sqrt{100}}} = 2$ <p><math>2 &gt; 1.6449</math> (accept 1.645 or better)</p> <p>Reject <math>H_0</math> <u>or</u> significant result <u>or</u> in the critical region                      Managing director's claim is supported.</p>	<p>B1,B1</p> <p>M1A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p style="text-align: right;"><b>7</b></p>
<p>2<sup>nd</sup> M1A1</p> <p>Critical Region</p>	<p>1<sup>st</sup> B1 for <math>H_0</math>. They must use <math>\mu</math> not <math>x, p, \lambda</math> or <math>\bar{x}</math> etc</p> <p>2<sup>nd</sup> B1 for <math>H_1</math> (must be <math>&gt; 80</math>). Same rules about <math>\mu</math>.</p> <p>1<sup>st</sup> M1 for attempt at standardising using 83, 80 and <math>\frac{15}{\sqrt{100}}</math>. Can accept <math>\pm</math>.</p> <p>May be implied by <math>z = \pm 2</math></p> <p>1<sup>st</sup> A1 for + 2 only</p> <p>3<sup>rd</sup> B1 for <math>\pm 1.6449</math> seen (or probability of 0.0228 or better)</p> <p>2<sup>nd</sup> M1 for a correct statement about "significance" or rejecting <math>H_0</math> (or <math>H_1</math>) based on their <math>z</math> value and their 1.6449 (provided it is a recognizable critical value from normal tables) <u>or</u> their probability (<math>&lt; 0.5</math>) and significance level of 0.05.                      Condone their probability <math>&gt; 0.5</math> compared with 0.95 for the 2<sup>nd</sup> M1</p> <p>2<sup>nd</sup> A1 for a correct contextualised comment. Must mention "director" and "claim" <u>or</u> "time" and "use of Internet". No follow through.</p> <p>If no comparison or statement is made but a correct contextualised comment is given the M1 can be implied.                      If a comparison is made it must be <u>compatible</u> with statement otherwise M0                      e.g. comparing 0.0228 with 1.6449 is M0 or comparing probability 0.9772 with 0.05 is M0                      comparing -2 with - 1.6449 is OK provided a correct statement accompanies it                      condone -2 <math>&gt;</math> -1.6449 provided their statement correctly rejects <math>H_0</math>.</p> <p>They may find a critical region for <math>\bar{X}</math>: <math>\bar{X} &gt; 80 + \frac{15}{\sqrt{100}} \times 1.6449 = \text{awrt } 82.5</math></p> <p>1<sup>st</sup> M1 for <math>80 + \frac{15}{\sqrt{100}} \times (z \text{ value})</math></p> <p>3<sup>rd</sup> B1 for 1.645 or better</p> <p>1<sup>st</sup> A1 for awrt 82.5</p> <p>The rest of the marks are as per the scheme.</p>	

Question Number	Scheme	Marks
Q2	<p style="text-align: center;">[ <math>P \sim N(90,9)</math> and <math>J \sim N(91,12)</math> ]</p> <p>(a) <math>(J - P) \sim N(1, 21)</math>  <math>P(J &lt; P) = P(J - P &lt; 0)</math>  <math>= P\left(Z &lt; \frac{0-1}{\sqrt{21}}\right)</math>  <math>= P(Z &lt; -0.2182\dots)</math>  <math>= 1 - 0.5871 = 0.4129</math>  calculator (0.4136....)</p> <p>(b) <math>X = (J_1 + J_2 + \dots + J_{60}) - (P_1 + P_2 + \dots + P_{60})</math>  <math>E(X) = 60 \times 91 - 60 \times 90 = 60</math> [stated as <math>E(X) = 60</math> or <math>X \sim N(60, \dots)</math>]  <math>\text{Var}(X) = 60 \times 9 + 60 \times 12 = 1260</math>  <math>P(X &gt; 120) = P\left(Z &gt; \frac{120-60}{\sqrt{1260}}\right)</math>  <math>= P(Z &gt; 1.69030\dots)</math>  <math>= 1 - 0.9545 = 0.0455</math></p>	<p>M1, A1</p> <p>dM1</p> <p>A1 (4)</p> <p>M1</p> <p>B1</p> <p>A1</p> <p>M1</p> <p>A1 (5)</p> <p style="text-align: right;"><b>9</b></p>
Use of means	<p>(a) 1<sup>st</sup> M1 for attempting <math>J - P</math> and <math>E(J - P)</math> or <math>P - J</math> and <math>E(P - J)</math>  1<sup>st</sup> A1 for variance of 21 (Accept <math>9 + 12</math>). Ignore any slip in <math>\mu</math> here.  2<sup>nd</sup> dM1 for attempting the correct probability and standardising with their mean and sd. This mark is dependent on previous M so if <math>J - P</math> ( or <math>P - J</math> ) is not being used score M0  If their method is not crystal clear then they must be attempting <math>P(Z &lt; -ve \text{ value})</math> or <math>P(Z &gt; +ve \text{ value})</math> i.e. their probability <u>after</u> standardisation should lead to a prob. <math>&lt; 0.5</math> so e.g. <math>P(J - P &lt; 0)</math> leading to 0.5871 is M0A0 unless the M1 is clearly earned.  2<sup>nd</sup> A1 for awrt 0.413 or 0.414</p> <p style="text-align: center;"><b>The first 3 marks may be implied by a correct answer</b></p> <p>(b) 1<sup>st</sup> M1 for a clear attempt to identify a correct form for <math>X</math>. This may be implied by correct variance of 1260  B1 for <math>E(X) = 60</math>. Can be awarded even if they are using <math>X = 60J - 60P</math>. Allow <math>P - J</math> and <math>-60</math>  1<sup>st</sup> A1 for a correct variance. If 1260 is given the M1 is scored by implication.  2<sup>nd</sup> M1 for attempting a correct probability and standardising with 120 and their 60 and 1260  If the answer is incorrect a full <u>expression</u> must be seen following through their values  for M1 e.g. <math>P\left(Z &gt; \frac{120 - \text{their } 60}{\sqrt{\text{their variance}}}\right)</math>. If using <math>-60</math>, should get <math>P\left(Z &lt; \frac{-120 - -60}{\sqrt{\text{their variance}}}\right)</math></p> <p>Attempt to use <math>\bar{J} - \bar{P}</math> for 1<sup>st</sup> M1, <math>E(\bar{J} - \bar{P}) = 1</math> for B1 and <math>\text{Var}(\bar{J} - \bar{P}) = 0.35</math> for A1  Then 2<sup>nd</sup> M1 for standardisation with 2, and their 1 and 0.35</p>	

Question Number	Scheme	Marks
Q3 (a)	$E \sim N(0, 0.5^2)$ or $X \sim N(w, 0.5^2)$ $P( E  < 0.6) = P\left( Z  < \frac{0.6}{0.5}\right)$ or $P( X - w  < 0.6) = P\left( Z  < \frac{0.6}{0.5}\right)$ $= P( Z  < 1.2)$ $= 2 \times 0.8849 - 1 = 0.7698$ awrt <b>0.770</b>	M1 A1 (2)
(b)	$\bar{E} \sim N\left(0, \frac{1}{64}\right)$ or $\bar{X} \sim N\left(w, \frac{0.5^2}{16}\right)$ $P( \bar{E}  < 0.3) = P\left( Z  < \frac{0.3}{\frac{1}{8}}\right)$ or $P( \bar{X} - w  < 0.3) = P\left( Z  < \frac{0.3}{\frac{1}{8}}\right)$ $= P( Z  < 2.4)$ $= 2 \times 0.9918 - 1 = 0.9836$ awrt <b>0.984</b>	M1 M1, A1 A1 (4)
(c)	$35.6 \pm 2.3263 \times \frac{1}{8}$ <b>(35.3, 35.9)</b>	M1 B1 A1, A1 (4) <b>10</b>
(a)	1 <sup>st</sup> M1 for identifying a correct probability (they must have the 0.6) and attempting to standardise. Need   . This mark can be given for 0.8849 - 0.1151 seen as final answer. 1 <sup>st</sup> A1 for awrt 0.770. NB an answer of 0.3849 or 0.8849 scores M0A0 (since it implies no   ) <b>M1 may be implied by a correct answer</b>	
(b)	1 <sup>st</sup> M1 for a correct attempt to define $\bar{E}$ or $\bar{X}$ but must attempt $\frac{\sigma^2}{n}$ . Condone labelling as $E$ or $X$ This mark may be implied by standardisation in the next line. 2 <sup>nd</sup> M1 for identifying a correct probability statement using $\bar{E}$ or $\bar{X}$ . Must have 0.3 and    1 <sup>st</sup> A1 for correct standardisation as printed or better 2 <sup>nd</sup> A1 for awrt 0.984 <b>The M marks may be implied by a correct answer.</b>	
Sum of 16, not means	1 <sup>st</sup> M1 for correct attempt at suitable sum distribution with correct variance ( $= 16 \times \frac{1}{4}$ ) 2 <sup>nd</sup> M1 for identifying a correct probability. Must have 4.8 and    1 <sup>st</sup> A1 for correct standardisation i.e. need to see $\frac{4.8}{\sqrt{4}}$ or better	
(c)	M1 for $35.6 \pm z \times \frac{0.5}{\sqrt{16}}$ B1 for 2.3263 or better. Use of 2.33 will lose this mark but can still score $\frac{3}{4}$ 1 <sup>st</sup> A1 for awrt 35.3 2 <sup>nd</sup> A1 for awrt 35.9	

Question Number	Scheme	Marks																																
Q4 (a)	<table border="1" data-bbox="309 304 1238 555"> <tr> <td>Distance rank</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> </tr> <tr> <td>Depth rank</td> <td>1</td> <td>2</td> <td>4</td> <td>3</td> <td>6</td> <td>7</td> <td>5</td> </tr> <tr> <td><math> d </math></td> <td>0</td> <td>0</td> <td>1</td> <td>1</td> <td>1</td> <td>1</td> <td>2</td> </tr> <tr> <td><math>d^2</math></td> <td>0</td> <td>0</td> <td>1</td> <td>1</td> <td>1</td> <td>1</td> <td>4</td> </tr> </table> <p data-bbox="225 629 347 678"><math>\sum d^2 = 8</math></p> <p data-bbox="225 689 467 763"><math>r_s = 1 - \frac{6 \times 8}{7 \times 48}</math></p> <p data-bbox="320 786 528 860"><math>= \frac{6}{7} = 0.857142</math></p> <p data-bbox="1145 801 1289 837">awrt <b>0.857</b></p>	Distance rank	1	2	3	4	5	6	7	Depth rank	1	2	4	3	6	7	5	$ d $	0	0	1	1	1	1	2	$d^2$	0	0	1	1	1	1	4	M1 M1 M1A1 M1 A1 (6) B1 B1 M1 A1ft (4) <b>10</b>
Distance rank	1	2	3	4	5	6	7																											
Depth rank	1	2	4	3	6	7	5																											
$ d $	0	0	1	1	1	1	2																											
$d^2$	0	0	1	1	1	1	4																											
(a)	<p data-bbox="225 1238 1054 1274">1<sup>st</sup> M1 for an attempt to rank the depths against the distances</p> <p data-bbox="225 1279 1051 1314">2<sup>nd</sup> M1 for attempting <math>d</math> for their ranks. Must be using ranks.</p> <p data-bbox="225 1319 919 1355">3<sup>rd</sup> M1 for attempting <math>\sum d^2</math> (must be using ranks)</p> <p data-bbox="225 1359 890 1395">1<sup>st</sup> A1 for sum of 8 (or 104 for reverse ranking)</p> <p data-bbox="225 1400 1501 1491">4<sup>th</sup> M1 for use of the correct formula with their <math>\sum d^2</math>. If answer is not correct an expression is required.</p> <p data-bbox="225 1496 1497 1532">2<sup>nd</sup> A1 for awrt (<math>\pm</math>) 0.857. Sign should correspond to ranking (so use of 104 should get -0.857)</p>																																	
(b)	<p data-bbox="225 1865 1501 1901">1<sup>st</sup> B1 for both hypotheses in terms of <math>\rho</math>, <math>H_1</math> must be one tail and compatible with their ranking</p> <p data-bbox="225 1906 715 1942">2<sup>nd</sup> B1 for cv of 0.8929 (accept <math>\pm</math>)</p> <p data-bbox="225 1946 1430 1982">M1 for a correct statement relating their <math>r_s</math> with their cv but cv must be such that <math> cv  &lt; 1</math></p> <p data-bbox="225 1986 1437 2078">A1ft for a correct contextualised comment. Must mention “researcher” and “claim” <u>or</u> “distance (from bank)” and “depth (of water)” Follow through their <math>r_s</math> and their cv (provided it is <math> cv  &lt; 1</math>) Use of “association” is A0</p>																																	



Question Number	Scheme	Marks																																																					
Q5	<table border="1" data-bbox="220 293 1214 465"> <thead> <tr> <th>Finances</th> <th>Worse</th> <th>Same</th> <th>Better</th> <th></th> </tr> </thead> <tbody> <tr> <td>Income</td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>Under £15 000</td> <td>10.54</td> <td>10.54</td> <td>12.92</td> <td>34</td> </tr> <tr> <td>£15 000 and above</td> <td>20.46</td> <td>20.46</td> <td>25.08</td> <td>66</td> </tr> <tr> <td></td> <td>31</td> <td>31</td> <td>38</td> <td>100</td> </tr> </tbody> </table> <p data-bbox="220 510 1085 546"><math>H_0</math> : State of finances and income are independent (not associated)</p> <p data-bbox="220 557 1085 593"><math>H_1</math> : State of finances and income are not independent (associated)</p> <table border="1" data-bbox="220 636 823 965"> <thead> <tr> <th><math>O_i</math></th> <th><math>E_i</math></th> <th><math>\frac{(O_i - E_i)^2}{E_i}</math></th> <th><math>\frac{O_i^2}{E_i}</math></th> </tr> </thead> <tbody> <tr> <td>14</td> <td>10.54</td> <td>1.1358....</td> <td>18.59..</td> </tr> <tr> <td>11</td> <td>10.54</td> <td>0.0200....</td> <td>11.48..</td> </tr> <tr> <td>9</td> <td>12.92</td> <td>1.1893...</td> <td>6.269..</td> </tr> <tr> <td>17</td> <td>20.46</td> <td>0.5851...</td> <td>14.12..</td> </tr> <tr> <td>20</td> <td>20.46</td> <td>0.0103...</td> <td>19.55..</td> </tr> <tr> <td>29</td> <td>25.08</td> <td>0.6126...</td> <td>33.53..</td> </tr> </tbody> </table> <p data-bbox="220 992 1324 1070"><math>\sum \frac{(O_i - E_i)^2}{E_i} = 3.553... \quad \text{or} \quad \sum \frac{O_i^2}{E_i} - 100 = 103.553... - 100 = 3.553... \quad (\text{awrt } \mathbf{3.55})</math></p> <p data-bbox="220 1081 486 1117"><math>\nu = (3 - 1)(2 - 1) = 2</math></p> <p data-bbox="220 1128 359 1164">cv is 5.991</p> <p data-bbox="220 1176 1117 1211">3.553 &lt; 5.991 so insufficient evidence to reject <math>H_0</math> <u>or</u> not significant</p> <p data-bbox="220 1223 1173 1258">There is no evidence of association between state of finances and income.</p>	Finances	Worse	Same	Better		Income					Under £15 000	10.54	10.54	12.92	34	£15 000 and above	20.46	20.46	25.08	66		31	31	38	100	$O_i$	$E_i$	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$	14	10.54	1.1358....	18.59..	11	10.54	0.0200....	11.48..	9	12.92	1.1893...	6.269..	17	20.46	0.5851...	14.12..	20	20.46	0.0103...	19.55..	29	25.08	0.6126...	33.53..	<p data-bbox="1353 383 1401 450">M1 A1</p> <p data-bbox="1353 546 1401 577">B1</p> <p data-bbox="1353 786 1401 817">M1</p> <p data-bbox="1353 860 1401 891">A1</p> <p data-bbox="1353 1021 1401 1052">A1</p> <p data-bbox="1353 1088 1401 1120">B1</p> <p data-bbox="1353 1131 1401 1162">B1</p> <p data-bbox="1353 1173 1401 1205">M1</p> <p data-bbox="1353 1216 1401 1247">A1</p> <p data-bbox="1481 1294 1520 1326"><b>10</b></p>
Finances	Worse	Same	Better																																																				
Income																																																							
Under £15 000	10.54	10.54	12.92	34																																																			
£15 000 and above	20.46	20.46	25.08	66																																																			
	31	31	38	100																																																			
$O_i$	$E_i$	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$																																																				
14	10.54	1.1358....	18.59..																																																				
11	10.54	0.0200....	11.48..																																																				
9	12.92	1.1893...	6.269..																																																				
17	20.46	0.5851...	14.12..																																																				
20	20.46	0.0103...	19.55..																																																				
29	25.08	0.6126...	33.53..																																																				
	<p data-bbox="220 1350 1252 1429">1<sup>st</sup> M1 for some use of <math>\frac{\text{Row Total} \times \text{Col.Total}}{\text{Grand Total}}</math>. May be implied by correct <math>E_i</math></p> <p data-bbox="220 1429 805 1464">1<sup>st</sup> A1 for all expected frequencies correct</p> <p data-bbox="220 1464 1436 1543">B1 for both hypotheses. Must mention “state” or “finances” and “income” at least once Use of “relationship” or “correlation” or “connection” is B0</p> <p data-bbox="220 1543 1492 1579">2<sup>nd</sup> M1 for at least two correct terms (as in 3<sup>rd</sup> or 4<sup>th</sup> column) or correct expressions with their <math>E_i</math></p> <p data-bbox="220 1579 1500 1615">2<sup>nd</sup> A1 for all correct terms. May be implied by a correct answer.(2 dp or better-allow eg 1.13...)</p> <p data-bbox="220 1615 1468 1664">3<sup>rd</sup> M1 for a correct statement linking their test statistic and their cv . Must be <math>\chi^2</math> not normal.</p> <p data-bbox="220 1664 1468 1776">4<sup>th</sup> A1 for a correct comment in context - must mention “state” or “finances” and “income” condone “relationship” or “connection” here but <b>not</b> “correlation”. No follow through. e.g. “There is no evidence of a relationship between finances and income”</p>																																																						

Question Number	Scheme						Marks																																			
Q6	<table border="1"> <tr> <td>Distance from centre of site (m)</td> <td>0-1</td> <td>1-2</td> <td>2-4</td> <td>4-6</td> <td>6-9</td> <td>9-12</td> </tr> <tr> <td><math>b - a</math></td> <td>1</td> <td>1</td> <td>2</td> <td>2</td> <td>3</td> <td>3</td> </tr> <tr> <td>No of artefacts</td> <td>22</td> <td>15</td> <td>44</td> <td>37</td> <td>52</td> <td>58</td> </tr> <tr> <td><math>P(a \leq X &lt; b)</math></td> <td><math>\frac{1}{12}</math></td> <td><math>\frac{1}{12}</math></td> <td><math>\frac{1}{6}</math></td> <td><math>\frac{1}{6}</math></td> <td><math>\frac{1}{4}</math></td> <td><math>\frac{1}{4}</math></td> </tr> <tr> <td><math>228 \times P(a \leq X &lt; b)</math></td> <td>19</td> <td>19</td> <td>38</td> <td>38</td> <td>57</td> <td>57</td> </tr> </table>						Distance from centre of site (m)	0-1	1-2	2-4	4-6	6-9	9-12	$b - a$	1	1	2	2	3	3	No of artefacts	22	15	44	37	52	58	$P(a \leq X < b)$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{4}$	$\frac{1}{4}$	$228 \times P(a \leq X < b)$	19	19	38	38	57	57	M1 A1 A1
	Distance from centre of site (m)	0-1	1-2	2-4	4-6	6-9	9-12																																			
	$b - a$	1	1	2	2	3	3																																			
	No of artefacts	22	15	44	37	52	58																																			
	$P(a \leq X < b)$	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{4}$	$\frac{1}{4}$																																			
	$228 \times P(a \leq X < b)$	19	19	38	38	57	57																																			
	<table border="1"> <thead> <tr> <th>Class</th> <th><math>O_i</math></th> <th><math>E_i</math></th> <th><math>\frac{(O_i - E_i)^2}{E_i}</math></th> <th><math>\frac{O_i^2}{E_i}</math></th> </tr> </thead> <tbody> <tr> <td>0-1</td> <td>22</td> <td>19</td> <td><math>\frac{9}{19} = 0.4736\dots</math></td> <td>25.57...</td> </tr> <tr> <td>1-2</td> <td>15</td> <td>19</td> <td><math>\frac{16}{19} = 0.8421\dots</math></td> <td>11.84...</td> </tr> <tr> <td>2-4</td> <td>44</td> <td>38</td> <td><math>\frac{36}{38} = 0.9473\dots</math></td> <td>50.94...</td> </tr> <tr> <td>4-6</td> <td>37</td> <td>38</td> <td><math>\frac{1}{38} = 0.0263\dots</math></td> <td>36.02...</td> </tr> <tr> <td>6-9</td> <td>52</td> <td>57</td> <td><math>\frac{25}{57} = 0.4385\dots</math></td> <td>47.43...</td> </tr> <tr> <td>9-12</td> <td>58</td> <td>57</td> <td><math>\frac{1}{57} = 0.0175\dots</math></td> <td>59.01...</td> </tr> </tbody> </table>						Class	$O_i$	$E_i$	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$	0-1	22	19	$\frac{9}{19} = 0.4736\dots$	25.57...	1-2	15	19	$\frac{16}{19} = 0.8421\dots$	11.84...	2-4	44	38	$\frac{36}{38} = 0.9473\dots$	50.94...	4-6	37	38	$\frac{1}{38} = 0.0263\dots$	36.02...	6-9	52	57	$\frac{25}{57} = 0.4385\dots$	47.43...	9-12	58	57	$\frac{1}{57} = 0.0175\dots$	59.01...	M1 A1
	Class	$O_i$	$E_i$	$\frac{(O_i - E_i)^2}{E_i}$	$\frac{O_i^2}{E_i}$																																					
	0-1	22	19	$\frac{9}{19} = 0.4736\dots$	25.57...																																					
	1-2	15	19	$\frac{16}{19} = 0.8421\dots$	11.84...																																					
2-4	44	38	$\frac{36}{38} = 0.9473\dots$	50.94...																																						
4-6	37	38	$\frac{1}{38} = 0.0263\dots$	36.02...																																						
6-9	52	57	$\frac{25}{57} = 0.4385\dots$	47.43...																																						
9-12	58	57	$\frac{1}{57} = 0.0175\dots$	59.01...																																						
<p><math>H_0</math>: <u>continuous uniform</u> distribution <u>is</u> a good fit</p>						B1																																				
<p><math>H_1</math>: <u>continuous uniform</u> distribution <u>is not</u> a good fit</p>																																										
$\sum \frac{(O_i - E_i)^2}{E_i} = \frac{313}{114} = 2.75 \quad \text{or} \quad \sum \frac{O_i^2}{E_i} - 228 = 230.745\dots - 228 = \dots \quad (\text{awrt } \mathbf{2.75})$						dM1A1																																				
$\nu = 6 - 1 = 5$						B1																																				
$\chi^2_5(0.05) = 11.070$						B1ft																																				
$2.75 < 11.070$ , insufficient evidence to reject $H_0$						M1																																				
Continuous uniform distribution is a suitable model						A1																																				
<b>12</b>																																										
<p>1<sup>st</sup> M1 for calculation of at least 3 widths and attempting proportions/probs. <u>or</u> for 1:2:3 ratio seen</p> <p>1<sup>st</sup> A1 for correct probabilities</p> <p>2<sup>nd</sup> A1 for all correct expected frequencies</p> <p>2<sup>nd</sup> M1 for attempting <math>\frac{(O - E)^2}{E}</math> or <math>\frac{O^2}{E}</math>, at least 3 correct expressions or values.</p> <p>Follow through their <math>E_i</math> provided they are not all = 38</p> <p>3<sup>rd</sup> A1 for a correct set of calcs - 3<sup>rd</sup> or 4<sup>th</sup> column. (2 dp or better and allow e.g. 0.94...)</p> <p>3<sup>rd</sup> dM1 <b>dependent on 2<sup>nd</sup> M1</b> for attempting a correct sum or calculation (must see at least 3 terms and +)</p> <p><b>The first three Ms and As can be implied by a test statistic of awrt 2.75</b></p> <p>4<sup>th</sup> M1 for a correct statement based on their test statistic (<math>&gt; 1</math>) and their cv (<math>&gt; 3.8</math>)</p> <p>Contradictory statements score M0 e.g. "significant" do not reject <math>H_0</math>.</p> <p>5<sup>th</sup> A1 for a correct comment suggesting that continuous uniform model is suitable. No ft</p>																																										

Question Number	Scheme	Marks
Q7	(a) Label full time staff 1-6000, part time staff 1-4000 Use random numbers to select Simple random sample of 120 full time staff and 80 part time staff	M1 M1 A1 (3)
	(b) Enables estimation of statistics / errors for each strata <u>or</u> “reduce variability” <u>or</u> “more representative” <u>or</u> “reflects population structure” <b>NOT</b> “more accurate”	B1 (1)
	(c) $H_0: \mu_f = \mu_p, \quad H_1: \mu_f \neq \mu_p$ (accept $\mu_1, \mu_2$ ) $\text{s.e.} = \sqrt{\frac{21}{80} + \frac{19}{80}}, \quad z = \frac{52 - 50}{\sqrt{\frac{21}{80} + \frac{19}{80}}} = (2\sqrt{2})$ $= 2.828\dots$ (awrt <b>2.83</b> )	B1 M1,M1 A1
	Two tailed critical value $z = 2.5758$ (or prob of awrt 0.002 (<0.005) or 0.004 (<0.01)) [2.828 > 2.5758 so] significant evidence to reject $H_0$ There is evidence of a difference in policy awareness between full time and part time staff	B1 dM1 A1ft (7)
	(d) Can use mean full time and mean part time ~ Normal	B1 B1 (2)
	(e) Have assumed $s^2 = \sigma^2$ or variance of sample = variance of population	B1 (1)
	(f) $2.53 < 2.5758$ , not significant <u>or</u> do not reject $H_0$ So there is insufficient evidence of a difference in mean awareness	M1 A1ft (2)
	(g) Training course has closed the gap between full time staff and part time staff’s mean awareness of company policy.	B1 (1)
		<b>17</b>
	(a) 1 <sup>st</sup> M1 for attempt at labelling full-time and part-time staff. One set of correct numbers. 2 <sup>nd</sup> M1 for mentioning use of random numbers 1 <sup>st</sup> A1 for s.r.s. of 120 full-time and 80 part-time	
	(c) 1 <sup>st</sup> M1 for attempt at s.e. - condone one number wrong . NB correct s.e. = $\sqrt{\frac{1}{2}}$ 2 <sup>nd</sup> M1 for using their s.e. in correct formula for test statistic. Must be $\frac{\pm(52-50)}{\sqrt{\frac{p}{q} + \frac{r}{s}}}$ 3 <sup>rd</sup> dM1 <b>dep. on 2<sup>nd</sup> M1</b> for a correct statement based on their normal cv and their test statistic 2 <sup>nd</sup> A1 for correct comment in context. Must mention “scores” or “policy awareness” and types of “staff”. Award <b>A0</b> for a one-tailed comment. Allow ft	
	(d) 1 <sup>st</sup> B1 for mention of mean(s) <u>or</u> use of $\bar{X}$ , provided $\bar{X}$ clearly refers to full-time or part-time 2 <sup>nd</sup> B1 for stating that distribution can be assumed normal e.g. “mean score of the test is normally distributed” gets B1B1	
	(f) M1 for correct statement (may be implied by correct contextualised comment) A1 for correct contextualised comment. Accept “no difference in mean scores”. Allow ft	
	(g) B1 for correct comment in context that implies training was effective. This must be supported by their (c) and (f). Condone one-tailed comment here.	





Further copies of this publication are available from  
Edexcel Publications, Adamsway, Mansfield, Notts, NG18 4FN

Telephone 01623 467467  
Fax 01623 450481

Email [publications@linneydirect.com](mailto:publications@linneydirect.com)

Order Code UA024774 Summer 2010

For more information on Edexcel qualifications, please visit [www.edexcel.com/quals](http://www.edexcel.com/quals)

Edexcel Limited. Registered in England and Wales no.4496750  
Registered Office: One90 High Holborn, London, WC1V 7BH