

| Question Number | Scheme | Marks |
|-----------------|--|---|
| 1. | <p>Total in School = $(15 \times 30) + 150 = 600$</p> <p>random sample of $\frac{30}{600} \times 40$ $= \underline{2}$ from each of the 15 classes</p> <p>random sample of $\frac{150}{600} \times 40$ $= \underline{10}$ from sixth form;</p> <p>Label the boys in each class from 1 – 15 and the girls from 1 – 15. use random numbers to select 1 girl and 1 boy</p> <p>Label the boys in the sixth form from 1 – 75 and the girls from 1 – 75. use random numbers to select <u>5</u> different boys and 5 different girls.</p> | <p>B1</p> <p>(Use of $\frac{40}{their\ 600}$) M1 A1</p> <p>Either A1</p> <p>B1 B1</p> <p>B1</p> <p>(7)</p> |

| Question Number | Scheme | Marks |
|-----------------|---|---|
| 2. (a) | $E(R) = 20 + 10 = 30$ | B1 (1) |
| (b) | $\text{Var}(R) = 4 + 0.84, = 4.84$ | M1, A1 (2) |
| (c) | $R \sim N(30, 4.84)$ (Use of normal with their (a),(b)) $P(28.9 < R < 32.64) = P(R < 32.64) - P(R < 28.9)$ $= P\left(Z < \frac{32.64 - 30}{2.2}\right) - P\left(Z < \frac{28.9 - 30}{2.2}\right)$ Stand their σ and μ $= P(Z < 1.2) - P(Z < -0.5)$ $= 0.8849 - (1 - 0.6915)$ Correct area $= 0.8849 - 0.3085 = 0.5764$ (accept AWRT 0.576) | B1ft M1 A1, A1 M1 A1 (6) |

| | | |
|---------------|--|--|
| <p>3. (a)</p> | $\hat{\mu} = \frac{82 + 98 + 140 + 110 + 90 + 125 + 150 + 130 + 70 + 110}{10}$ $= 110.5$ $\hat{\sigma}^2 = \frac{1}{9}(128153 - 10 \times 110.5^2)$ $= 672.28$ | <p>M1 A1 B1 M1 A1 (5)</p> |
| <p>(b)</p> | <p>95% confidence limits are</p> $110.5 \pm 1.96 \times \frac{25}{\sqrt{10}}$ <p>95% conf. lim. = AWRT(95, 126)</p> | <p>(condone use of 5 instead of 25) (for 1.96) M1 B1 A1√ A1 A1 (5)</p> |
| <p>(c)</p> | <p>Number of intervals = $\frac{95}{100} \times 15$</p> $= 14.25$ | <p>(Allow 14 or 14.3 if method is clear) M1 A1 (2)</p> |
| | | <p>12</p> |

4.

H_0 : No association between gender and acceptance
 H_1 : gender and acceptance are associated

| | Accept | Not accept | Total |
|---------|-----------|------------|-------|
| Males | 170 (180) | 110 (100) | 280 |
| Females | 280 (270) | 140 (150) | 420 |
| Totals | 450 | 250 | 700 |

Expected Values

B1

M1 A1

| O | E | $\frac{(O - E)^2}{E}$ |
|-----|-----|-----------------------|
| 170 | 180 | 0.5556 |
| 110 | 100 | 1.0000 |
| 280 | 270 | 0.3704 |
| 140 | 150 | 0.6667 |

$$\sum \frac{(O - E)^2}{E} = 2.59 \text{ (Yates' 2.34)}$$

(Condone use of Yates')

M1 A1

$$\nu = 1; (5\%) = 3.841$$

B1; B1

$3.841 > 2.59$. There is insufficient evidence to reject H_0
 There is no association between a persons gender and their acceptance (of the offer of a flu jab.)

M1
 A1√

(9)

9

| | | |
|--------|--|--|
| 5. (a) | <p>μ_b = mean mark of boys, μ_g = mean mark of girls.</p> <p>$H_0 : \mu_b = \mu_g$ $H_1 : \mu_b \neq \mu_g$</p> $z = \frac{53 - 50}{\sqrt{\frac{144}{80} + \frac{144}{80}}}$ <p>= 1.58 Critical region $z \geq 1.96$ 1.58 < 1.96 insufficient evidence to reject H_0. No diff. between mean scores of boys and girls.</p> | <p>both</p> <p>B1</p> <p>M1 A1</p> <p>A1 B1 M1 A1</p> <p>(7)</p> |
| (b) | <p>$H_0 : \mu_b = \mu_g$ $H_1 : \mu_b < \mu_g$</p> $z = \frac{62 - 59}{\sqrt{\frac{36}{80} + \frac{36}{80}}}$ <p>= 3.16</p> <p>Critical region $z \geq 1.6449$ (accept 1.645) 3.16 > 1.6449 sufficient evidence to reject H_0. the mean mark for boys is less than the mean mark of the girls.</p> | <p>B1</p> <p>M1</p> <p>A1 B1 A1</p> <p>(5)</p> |
| (c) | <p>Girls have improved more than boys or girls performed better than boys after 1 year</p> | <p>B1</p> <p>(1)</p> <p>13</p> |

| | | |
|---------------|---|--|
| <p>6. (a)</p> | <p>$r = 27.07,$ $s = 18.04,$ $t = 0.11$ using tables or 0.12 using totals</p> | <p>M1 A1 B1 B1 ft (4)</p> |
| <p>(b)</p> | <p>H_0 : A Poisson model $Po(2)$ is a suitable model. both H_1 : A Poisson model $Po(2)$ is not a suitable model. Amalgamate data $\sum \frac{(O - E)^2}{E} = 3.28$ (awrt) $v = 6 - 1 = 5$ $\chi^2_5(5\%) = 11.070$ (follow through their degrees of freedom) $3.25 < 11.070$ There is insufficient evidence to reject H_0, <u>$Po(2)$ is a suitable model.</u></p> | <p>B1 M1 M1 A1 B1 B1ft A1ft (7)</p> |
| <p>(c)</p> | <p>The expected values, and hence $\sum \frac{(O - E)^2}{E}$ would be different, and the degrees of freedom would be 1 less.</p> | <p>B1 B1 (2)</p> <p style="text-align: right;">13</p> |

| 7. (a) | The variables cannot be assumed to be normally distributed | B1 (1) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------|--|-------------------------------------|-------|-------|-------|-------|-------|-----|----------|---|---|---|---|---|---|----------|---|---|---|---|---|---|-----|---|---|---|---|---|---|-------|---|---|---|---|---|---|---|
| (b) | <table border="1" data-bbox="225 232 1074 434"> <thead> <tr> <th></th> <th>20-29</th> <th>30-39</th> <th>40-49</th> <th>50-59</th> <th>60-69</th> <th>70+</th> </tr> </thead> <tbody> <tr> <td>Rank x</td> <td>5</td> <td>6</td> <td>4</td> <td>3</td> <td>1</td> <td>2</td> </tr> <tr> <td>Rank y</td> <td>6</td> <td>5</td> <td>4</td> <td>1</td> <td>3</td> <td>2</td> </tr> <tr> <td>d</td> <td>1</td> <td>1</td> <td>0</td> <td>2</td> <td>2</td> <td>0</td> </tr> <tr> <td>d^2</td> <td>1</td> <td>1</td> <td>0</td> <td>4</td> <td>4</td> <td>0</td> </tr> </tbody> </table> <p data-bbox="225 501 1294 546">$\sum d^2 = 10$ (follow through their rankings)</p> <p data-bbox="225 562 1517 645">$r_s = 1 - \frac{6\sum d^2}{n(n^2 - 1)} = 1 - \frac{60}{210} = 0.714$ ($\frac{5}{7}$ or awrt 0.714)</p> | | 20-29 | 30-39 | 40-49 | 50-59 | 60-69 | 70+ | Rank x | 5 | 6 | 4 | 3 | 1 | 2 | Rank y | 6 | 5 | 4 | 1 | 3 | 2 | d | 1 | 1 | 0 | 2 | 2 | 0 | d^2 | 1 | 1 | 0 | 4 | 4 | 0 | M1 A1 dM1 (depends on ranking attempt) A1 ft M1 A1 (6) |
| | 20-29 | 30-39 | 40-49 | 50-59 | 60-69 | 70+ | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Rank x | 5 | 6 | 4 | 3 | 1 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| Rank y | 6 | 5 | 4 | 1 | 3 | 2 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| d | 1 | 1 | 0 | 2 | 2 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| d^2 | 1 | 1 | 0 | 4 | 4 | 0 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| (c) | <p data-bbox="225 725 443 792">$H_0: \rho = 0$ $H_1: \rho \neq 0$ (or $\rho > 0$)</p> <p data-bbox="225 824 1401 860">$n = 6 \Rightarrow 5\%$ critical value = 0.8857 (or 0.8286)</p> <p data-bbox="225 891 1385 927">0.714 < 0.8857</p> <p data-bbox="225 931 1102 994">No evidence to reject H_0; No evidence of correlation between deaths from pneumoconiosis and lung cancer.</p> | B1 B1 B1 ✓ M1 A1 (5) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |