



Mathematics

Advanced GCE

Unit 4733: Probability and Statistics 2

Mark Scheme for January 2011

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Mark schemes should be read in conjunction with the published question papers and the Report on the Examination.

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Mark Scheme

January 2011

1		$\hat{\alpha} = \bar{x} = \frac{468}{52} = 52$	B1	52 stated
		$\mu = x = \frac{1}{9} = 32$	M1	Correct method for biased estimator
		24820	M1	Multiply by 9/8
		$\frac{-52^2}{9}$ [= 55.78]		[if single formula, allow M0 M1 if wrong but divisor 8 seen
		0		anywhere]
		$\hat{\sigma}^2 = \frac{9}{2} \times 53.78 = 60.5$	A1 4	Answer 60.5 or exact equivalent
		8		
2		$53.28 - \mu_{-1.06}$	M1dep	Standardise with \sqrt{n} once & equate to z, allow sign, square/ \sqrt{n}
		$\frac{1}{5/\sqrt{n}} = 1.90$		errors
		u = 51.65	A1	twice, signs correct, zs may be wrong
		$\frac{\mu - 51.05}{5} = 1.3$	B1	Both correct z values seen
		$5/\sqrt{n}$	depM1	Solve to get \sqrt{n} or μ , needs first M1
		$\sqrt{n} = 10, \qquad n = 100$	AÎ	n = 100, not from wrong signs
		$\mu =$ 52.3	B1 6	a.r.t. 52.3. right arithmetic needed but \sqrt{n} can be omitted
3		B(200, 0.0228)	M1	B(200, 0.0228) stated or implied
_		Po(4.56)	A1	Po(4.56) stated or implied, allow 4.6 here
		4.56 ²	M1	Correct formula for $P(\leq 2) \pm 1$ term. any λ (tables: M0)
		$e^{-4.50}(1+4.56+\frac{1.50}{2})$	A1	Correct formula, 4.56 needed
		- 0 167	A1	Answer, a.r.t. 0.167 [0.16694]
		= 0.107	B1 6	Both, can be merely asserted. If numbers, must be these
		<i>n</i> large of $n > 50$, <i>p</i> small of $np < 5$		SR interpolation: clear method M1, answer A2
				MR: typically B(200, 0.228) \approx N(45.6, 3.52); M1A1;
				standardise correctly M1: state $nn na > 5$ B1
4	(i)	r:d = 2134 - 230	M1	Standardise z with $\sqrt{50}$ ignore sign or $\sqrt{0}$ or squaring errors
-	(1)	Either $z = \frac{21311}{45} \frac{250}{50}$		Standardise 2, with 1990, ignore sign of 1 of squaring errors
		45/ \sqrt{50}		z-value a r t -2.61 or <i>p</i> in range [0.0044, 0.005)
		= -2.608	Al	Correctly compare $(-)^2.576$, signs consistent.
		-2.608 < -2.576 or 0.0047 < 0.005	BI	or p explicitly with 0.005
	Or	6126	M1	$230 - z\sigma/\sqrt{50}$ allow $\sqrt{10}$ or squaring errors allow + but not
		C_{V} is $230-2.576 \times \frac{11}{\sqrt{50}} = 213.0$	B1	250° 2.07 (50, and 1° + or squaring errors, and 1° = out not inst +: $7 = 2.576$
		$\sqrt{30}$		Just 1, 2, 2, 5 / 6
		213.4 < 213.0	Al	Explicitly compare 213.4 with 213.6
		Reject H ₀ . Significant evidence	M1	"Reject", FT, needs correct method and form of
		that population mean is not 230	A1 FT 5	comparison; interpreted, acknowledge uncertainty
	(ii)	Yes, population distribution is not	B2 2	<i>Not</i> , "yes, sample size is large" but ignore " <i>can</i> use it as"
		known to be normal		SR: Both right and wrong answers: B1
				α "Yes as it must be assumed normal": B1
5		$H_0: \lambda = 12; H_1: \lambda > 12$	B2	Both correct: B2. Allow μ . One error, B1, but <i>not x</i> , <i>r</i> etc.
		<i>Either</i> : $P(\ge 19) = 1 - P(\le 18)$	M1	Po(12) stated or implied, e.g. 0.9787
		= 1 - 0.9626		
		= 0.0374	A1	0.0374, or 0.9626 if compared with 0.9
		< 0.1	B1	Explicitly compare $P(\geq 19)$ with 0.1, or $P(\leq 18)$ with 0.9
		<i>Or</i> : CR is ≥ 18 , $p = 0.063$	A1	\geq 18 and 0.063 stated
		19 ≥ 18	B1	Explicit comparison of CV (right-hand CR) with 19
		Reject H ₀ . Significant evidence of	M1	"Reject" FT, needs correct method and comparison, e.g. not
		increase in mean number of		from \leq 19 or = 19, withhold if inconsistent
		applicants	A1 FT 7	Interpreted in context, acknowledge uncertainty

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Mark Scheme

6	(i)	If one customer arrives, it does not	B1		Answer that shows correct understanding of "independent", in
		change the probability that another			context; not just equivalent to "singly"
		one does so; customers probably	B1	2	Plausible reason, in context, nothing wrong, nothing that
		arrive in groups of at least 2			suggests "constant average rate"
	(ii)	0.1730	M1		Correct use of tables or formula, e.g3007, or .4405 from Po(5)
			Al	2	if $Po(7)$ stated; answer 0.173, 0.1730 or better
	(111)	Po(35)	BI		$Po(5\times7)$ stated or implied
		N(35, 35)	MI		Normal, μ = their λ
		$(40.5-35) = 1$ $\Phi(0.0207)$	AI M1		Both parameters correct, allow 35 ² , V35
		$1-\Phi\left \frac{10.5-55}{\sqrt{25}}\right = 1-\Phi(0.9297)$			Standardise 40 with λ , $\forall \lambda$, allow \forall , cc errors
				6	Both $\sqrt{\lambda}$ and cc correct
-		= 0.1763	AI D1	U	Answer, a.r.t. 0.1/6 [penalise 0.1/65]
7	(1)	N	BI		Horizontal line above axis
			BI D1	2	Concave decreasing curve above axis
			ы	3	Boin correct including approx relationship, not extending
	(;;)		M1		Δ the most $[f_{(i)}]_{ij}$ is the function of the effective for the effect
	(11)	$\int_{a}^{3} \frac{a}{a} dx = 1, \left \frac{-a}{a} \right _{a}^{3} = 1; a = \frac{3}{2}$	R1		Attempt J $f_X(x) dx$, limits 1, 3 at some stage, and equate to 1 Correct indefinite integral
		$\int_{1} x^{2} dx = 1 \int \left[x \right]_{1} dx = 2$		3	Correct indefinite integral Correctly obtain $3/2$ or 1.5 or exact equivalent
	(iii)		M1		Confectly obtain $5/2$ of 1.5 of exact equivalent
	(111)	$\int_{1}^{3} \frac{d}{dt} dx = \left[a \ln x \right]_{1}^{3}$		г	Attempt J $x_{1\chi}(x) dx$, minus 1, 5 at some stage
		$\frac{1}{x}$	A1F	г3	Answer any exact equivalent or a r t 1.65 FT on a or a ln 3
		$= \frac{3}{2} \ln 3$			Answer, any exact equivalent of a.i.t 1.05, 11 on a, of a in 5
	(iv)	T is equally likely to take any value	B1	1	Must be "values taken by T " (or "of T ") or clear equivalent
		between 1 and 3			Any hint that they think <i>T</i> is an <i>event</i> gets B0.
					α "Same chance of occurring anywhere between 1 and 3": 0
					β "For values of <i>T</i> between 1 and 3, <i>T</i> is equally likely": 0
					γ "Each value of T is equally likely to occur": 1
-					
8	(i)	B(40, 0.225)	M1		B(40, 0.225) stated or implied
8	(i)	B(40, 0.225) ≈ N(9, 6.975)	M1 M1		B(40, 0.225) stated or implied Normal, mean 9
8	(i)	$B(40, 0.225) \approx N(9, 6.975) \frac{5.5-9}{5} = -1.325$	M1 M1 A1		B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975
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8	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 M1 A1 A1 A1 B2 B1	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob.0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 M1 A1 A1 A1 B2 B1 M1 M1	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 M1 A1 A1 A1 B2 B1 M1	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7	M1 M1 A1 A1 B2 B1 B1 B1 B1 M1 A1 A1 F	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12 Withhold if inconsistent
9	(i) (ii) (i)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7	M1 M1 A1 A1 B2 B1 B1 B1 B1 M1 A1 A1 F1 A1 F1	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob. 0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7	M1 M1 A1 A1 B2 B1 B1 B1 B1 M1 A1 A1 B2 B1 M1 A1 F	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob.0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty [SR: Normal or Po: (i) M1, (ii) B2 maximum]
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob.0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty [SR: Normal or Po: (i) M1, (ii) B2 maximum] [0.9932 or 0.0068 probably B2 maximum]
9	(i) (ii) (ii) (iii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7 B(14, 0.8)	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 B1 B1 B1 B1 M1 A1 F M1 A1 F	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and √ <i>npq</i> , allow <i>npq</i> , no or wrong cc CC and √ <i>npq</i> correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" <i>α</i> "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow <i>π</i> . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV from correct tail and inequality with 12, <i>or</i> P(≥ 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs ≥ 13 or < 12; <i>p</i> method needs ≥ 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty [SR: Normal or Po: (i) M1, (ii) B2 maximum] [0.9932 or 0.0068 probably B2 maximum] B(14, 0.8) stated or implied, allow from B(14, 0.75)
9	(i) (ii) (ii) (iii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7 B(14, 0.8) P(≤ 12) from B(14, 0.8)	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 B1 B1 B1 B1 M1 A1 F1 M1 A1 F1 M1 M1 M1	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and √ <i>npq</i> , allow <i>npq</i> , no or wrong cc CC and √ <i>npq</i> correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" <i>α</i> "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV from correct tail and inequality with 12, <i>or</i> P(≥ 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs ≥ 13 or < 12; <i>p</i> method needs ≥ 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty [SR: Normal or Po: (i) M1, (ii) B2 maximum] [0.9932 or 0.0068 probably B2 maximum] B(14, 0.8) stated or implied, allow from B(14, 0.75) Attempt prob of acceptance region, e.g. 0.8990, $$ on (i)

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