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Mark Scheme (Results)
January 2010

Statistics S2 (6684)

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January 2010
6684 Statistics S2
Mark Scheme

Question Number	Scheme	Marks
Q1 (a)	$X \sim B(20,0.05)$	B1 B1 (2)
(b)	P(X = 0) = 0.95^{20} = 0.3584859… or 0.3585 using tables .	M1 A1 (2)

(c)	$P(X > 4)$ =1 - $P(X \leq 4)$
	
	            = 1 − 0.9974
	
	            = 0.0026
		M1
		
		A1 (2)

(d)	Mean = $20 \times 0.05 = 1$ Variance = $20 \times 0.05 \times 0.95 = 0.95$	B1 B1 (2) Total [8]

Q1 (a)
 	
(b)
 	
(c)
 	
(d)
	Notes
	1ˢᵗ B1 for binomial
	2ⁿᵈ B1 for 20 and 0.05 o.e
	These must be in part (a)
	M1 for finding $(p)^{20}$ 0< p <1 this working needs to be seen if answer incorrect to gain the M1
	A1 awrt 0.358 or 0.359.
	
	M1 for writing 1 - $P(X \leq 4)$
	                    or 1 – [P(X = 0) + P(X = 1) + P(X = 2) + P(X = 3) + P(X = 4)]
	                    or 1 – 0.9974
	                    or 1 – 0.9568
	A1 awrt 0.0026 or 2.6×10^{-3}, do not accept a fraction e.g. 26/10000
	
	1ˢᵗ B1 for 1
	2ⁿᵈ B1 for 0.95
	
	NB In parts b, c and d correct answers with no working gain full marks	

Question Number		Scheme	Marks
Q2	(a)	$P(X < 0) \qquad = F(0)$	M1
		$= \dfrac{2}{6} = \dfrac{1}{3}$	A1 (2)
	(b)	$f(x) \qquad = \dfrac{dF(x)}{dx}$	M1
		$f(x) = \begin{cases} \dfrac{1}{6} & -2 \le x \le 4 \\ 0 & \text{otherwise} \end{cases}$	A1 B1 (3)
	(c)	Continuous Uniform (Rectangular) distribution	B1 (1)
	(d)	Mean $= 1$	B1
		Variance is $\dfrac{(4--2)^2}{12} = 3$	M1 A1 (3)
	(e)	$P(X = 1) = 0$	B1 (1)
			Total [10]
Q2	(a)	**Notes**	
		M1 for attempting to find F(0) by a correct method eg subst 0 into F(x) or $\displaystyle\int_{-2}^{0} \dfrac{1}{6} dx$	
		Do **NOT** award M1 for $\displaystyle\int_{-2}^{0} \dfrac{x+2}{6} dx$ or $\dfrac{1}{2} \times \dfrac{1}{3} \times 2$ both of which give the correct answer by using F(x) as the pdf	
		A1 1/3 o.e or awrt 0.333	
		Correct answer only with no incorrect working gets M1 A1	
	(b)	**M1** for attempting to differentiate F(x). (for attempt it must have no xs in)	
		A1 for the first line. Condone $<$ signs	
		B1 for the second line. – They must have 0 $x < -2$ and $x > 4$ only.	
	(c)	**B1** must have "continuous" and "uniform" **or** "Rectangular"	
	(d)	**B1** for mean $= 1$	
		M1 for attempt to use $\dfrac{[\pm(b-a)]^2}{12}$, they must subst in values and not just quote the formula, or using $\displaystyle\int_{-2}^{4} x^2 \,(their\, f(x)) - (their\, mean)^2$, including limits. Must get x^3 **when they integrate.**	
		A1 cao .	
	(e)	**B1** cao	

Question Number		Scheme	Marks
Q3	(a)	$Y \sim \mathrm{Po}(0.25)$	B1
		$\mathrm{P}(Y{=}0) \quad = \mathrm{e}^{-0.25}$	M1
		$\qquad\qquad\quad = 0.7788$	A1
			(3)
	(b)	$X \sim \mathrm{Po}(0.4)$	B1
		$\mathrm{P}(\text{Robot will break down}) \quad = 1 - \mathrm{P}(X = 0)$	
		$\qquad\qquad\qquad\qquad\qquad = 1 - e^{-0.4}$	M1
		$\qquad\qquad\qquad\qquad\qquad = 1 - 0.067032$	
		$\qquad\qquad\qquad\qquad\qquad = 0.3297$	A1
			(3)
	(c)	$\mathrm{P}(X = 2) \quad = \dfrac{e^{-0.4}(0.4)^2}{2}$	M1
		$\qquad\qquad\quad = 0.0536$	A1
			(2)
	(d)	0.3297 or answer to part (b)	B1ft
		as Poisson events are <u>independent</u>	B1 dep
			(2)
			Total [10]
		<u>Notes</u>	
Q3	(a)	**B1** for seeing or using Po(0.25)	
		M1 for finding P($Y{=}0$) either by e^{-a}, where a is positive (a needn't equal their λ) or using tables if their value of λ is in them	
		Beware common Binomial error using, $p = 0.05$ gives 0.7738 but scores B0 M0 A0	
		A1 awrt 0.779	
	(b)	**B1** for **stating or a clear use of** Po(0.4) in part (b) or (c)	
		M1 for writing or finding $1 - \mathrm{P}(X{=}0)$	
		A1 awrt 0.33	
	(c)	**M1** for finding P($X{=}2$) e.g $\dfrac{\mathrm{e}^{-\lambda}\lambda^2}{2!}$ with their value of λ in	
		$\qquad\qquad\qquad$ or if their λ is in the table for writing $\mathrm{P}(X \le 2) - \mathrm{P}(X \le 1)$	
		A1 awrt 0.0536	
	(d)	**1st B1** their answer to part(b) correct to 2 sf or awrt 0.33	
		2nd B1 need the word independent. This is dependent on them gaining the first B1	
		SC	
		Use of Binomial.	
		Mark parts a and b as scheme. They could get (a) B0,M0,A0 (b) B0 M1 A0	
		In part c allow M1 for $^{n}C_{2}\,(p)^2(1\text{-}p)^{n\text{-}2}$ with "their n" and "their p". They could get (c) M1,A0	
		DO NOT GIVE for $p(x \le 2) - p(x \le 1)$	
		In (d) they can get the first B1 only. They could get (d) B1B0	

Question Number	Scheme	Marks
Q4 (a)	$\int_0^3 k(x^2 - 2x + 2)\mathrm{d}x + \int_3^4 3k\,\mathrm{d}x \;\; = 1$	M1
	$k\left[\dfrac{1}{3}x^3 - x^2 + 2x\right]_0^3 + \left[3kx\right]_3^4$ (=1) or $k\left[\dfrac{1}{3}x^3 - x^2 + 2x\right]_0^3 + 3k$ (=1)	A1 M1 dep
	$\qquad\qquad 9k \quad = 1$	
	$\qquad\qquad k \quad = \dfrac{1}{9}$ **given** $\qquad\qquad$ cso	A1 (4)
(b)	For $0 < x \le 3$, $\;\mathrm{F}(x) \;= \int_0^x \dfrac{1}{9}(t^2 - 2t + 2)\mathrm{d}t$	M1
	$\qquad\qquad\qquad = \dfrac{1}{9}\left(\dfrac{1}{3}x^3 - x^2 + 2x\right)$	A1
	For $3 < x \le 4$, $\;\mathrm{F}(x) \;= \int_3^x 3k\,\mathrm{d}t + \dfrac{2}{3}$	M1
	$\qquad\qquad\qquad = \dfrac{x}{3} - \dfrac{1}{3}$	A1
	$\mathrm{F}(x) = \begin{cases} 0 & x \le 0 \\[2mm] \dfrac{1}{27}(x^3 - 3x^2 + 6x) & 0 < x \le 3 \\[2mm] \dfrac{x}{3} - \dfrac{1}{3} & 3 < x \le 4 \\[2mm] 1 & x > 4 \end{cases}$	B1 ft B1 (6)
(c)	$\mathrm{E}(X) \;= \int_0^3 \dfrac{x}{9}(x^2 - 2x + 2)\mathrm{d}t + \int_3^4 \dfrac{x}{3}\mathrm{d}x$	M1
	$\qquad = \dfrac{1}{9}\left[\dfrac{1}{4}x^4 - \dfrac{2}{3}x^3 + x^2\right]_0^3 + \left[\dfrac{1}{6}x^2\right]_3^4$	A1
	$\qquad = \dfrac{29}{12}$ or 2.416 or awrt 2.42	A1 (3)
(d)	$\mathrm{F}(m) = 0.5$	M1
	$\mathrm{F}(2.6) = \dfrac{1}{27}(2.6^3 - 3 \times 2.6^2 + 6 \times 2.6) = $ awrt 0.48	M1
	$\mathrm{F}(2.7) = \dfrac{1}{27}(2.7^3 - 3 \times 2.7^2 + 6 \times 2.7) = $ awrt 0.52	A1
	Hence median lies between 2.6 and 2.7	A1 dA (4)
		Total [17]

Notes

Q4 (a) **1st M1** attempting to integrate **at least one** part (at least one $x^n \to x^{n+1}$) (ignore limits)

1st A1 Correct integration. Limits not needed.

2nd M1 dependent on the previous M being awarded. Adding the two answers together, putting equal to 1 and have the correct limits.

2nd A1 cso

(b) **1st M1** Att to integrate $\frac{1}{9}\left(t^2 - 2t + 2\right)$ (at least one $x^n \to x^{n+1}$). Ignore limits for method mark

1st A1 $\frac{1}{9}\left(\frac{x^3}{3} - x^2 + 2x\right)$ allow use of *t*. Must have used/implied use of limit of 0.

This must be on its own without anything else added

2nd M1 attempting to find $\int_3^x 3k + \ldots$ (must get $3kt$ or $3kx$)

and they must use the correct limits and add $\int_0^3 \frac{1}{9}\left(t^2 - 2t + 2\right)$ or $\frac{2}{3}$

or use $+ C$ and use F(4) = 1

2nd A1 $\frac{x}{3} - \frac{1}{3}$ must be correct

1st B1 middle pair followed through from their answers. condone them using < or $\leq$ incorrectly they do not need to match up

2nd B1 end pairs. condone them using < or $\leq$. They do not need to match up

NB if they show no working and just write down the distribution. If it is correct they get full marks. If it is incorrect then they cannot get marks for any incorrect part. So if $0 < x \leq 3$ is correct they can get M1 A1 otherwise M0 A0. If $3 < x \leq 4$ is correct they can get M1 A1 otherwise M0 A0. you cannot award B1ft if they show no working unless the middle parts are correct.

(c) **1st M1** attempting to use integral of x f(x) on one part

1st A1 Correct Integration for both parts added together. Ignore limits.

2nd A1 cao or awrt 2.42

(d) **1st M1** for using F(X) = 0.5. This may be implied by subst into F(X) and comparing answers with 0.5.

2nd M1 for substituting both 2.6 and 2.7 into "their F(X)" – 0.5 or "their F(X)"

1st A1 awrt 0.48 and 0.52 if using "their F(X)" .

and awrt -0.02 and 0.02 or if using "their F(X)" 0.5

Other values possible. You may need to check their values for their **correct** equation

NB these last two marks are B1 B1 on ePEN but mark as M1 A1

2nd A1 for conclusion but only award if it follows from their numbers. Dependent on previous A mark being awarded

SC using calculators

M1 for sign of a suitable equation

M1 A1 for awrt 2.66 provided equation is correct

A1 correct comment

Question Number	Scheme	Marks
Q5 (a)	$X \sim \text{Po}(10)$ $P(X < 9) \qquad = P(X \leq 8)$ $\qquad\qquad\qquad = 0.3328$	B1 M1 A1 (3)
(b)	$Y \sim \text{Po}(40)$ Y is approximately N(40,40) $P(Y > 50) \qquad = 1 - P(Y \leq 50)$ $\qquad\qquad = 1 - P\left(Z < \dfrac{50.5 - 40}{\sqrt{40}} \right)$ $\qquad\qquad = 1 - P(Z < 1.660..)$ $\qquad\qquad = 1 - 0.9515$ $\qquad\qquad = 0.0485$ N.B. Calculator gives 0.048437. Poisson gives 0.0526 (but scores nothing)	 M1 A1 M1 M1 A1 A1 (6) Total [9]
Q5 (a)	**Notes** **B1** for using Po(10) **M1** for attempting to find $P(X \leq 8)$: useful values $P(X \leq 9)$ is 0.4579(M0), using Po(6) gives 0.8472, (M1). **A1** awrt 0.333 but do not accept $\dfrac{1}{3}$	
(b)	**1$^{\text{st}}$ M1** for identifying the normal approximation **1$^{\text{st}}$ A1** for [mean = 40] and [sd = $\sqrt{40}$ or var = 40] **NB These two marks are B1 M1 on ePEN** These first two marks may be given if the following are seen in the standardisation formula : 40 and $\sqrt{40}$ or awrt 6.32 **2$^{\text{nd}}$ M1** for attempting a continuity correction (50 or 30 $\pm$ 0.5 is acceptable) **3$^{\text{rd}}$ M1** for standardising using their mean and their standard deviation and using either 49.5, 50 or 50.5. (29.5, 30, 30.5) accept $\pm$ **2$^{\text{nd}}$ A1** correct z value awrt $\pm$1.66 **or** this may be awarded if see $\pm\dfrac{50.5 - 40}{\sqrt{40}}$ or $\pm\dfrac{29.5 - 40}{\sqrt{40}}$ **3$^{\text{rd}}$ A1** awrt 3 sig fig in range 0.0484 – 0.0485	

Question Number		Scheme	Marks
Q6	(a)	The set of values of the test statistic for which the null hypothesis is rejected in a hypothesis test.	B1 B1 (2)
	(b)	X~B(30,0.3)	M1
		$P(X \leq 3) = 0.0093$	
		$P(X \leq 2) = 0.0021$	A1
		$P(X \geq 16) = 1 - 0.9936 = 0.0064$	
		$P(X \geq 17) = 1 - 0.9979 = 0.0021$	A1
		Critical region is $(0 \leq)x \leq 2$ or $16 \leq x(\leq 30)$	A1A1 (5)
	(c)	Actual significance level 0.0021+0.0064=0.0085 or 0.85%	B1 (1)
	(d)	15 (it) is not in the critical region not significant No significant evidence of a change in $p = 0.3$ accept H_0, (reject H_1) $P(x \geq 15) = 0.0169$	Bft 2, 1, 0 (2) Total [10]

Notes

Q6 (a) **1st B1** for "**values/ numbers**"
2nd B1 for "reject the null hypothesis" o.e or the test is significant

(b) **M1** for using B(30,0.3)
1st A1 $P(x \leq 2) = 0.0021$
2nd A1 0.0064

3rd A1 for $(X) \leq 2$ or $(X) < 3$ They get **A0** if they write $P(X \leq 2/ X < 3)$
4th A1 $(X) \geq 16$ or $(X) > 15$ They get **A0** if they write $P(X \geq 16 X > 15$
NB these are B1 B1 but mark as A1 A1

$16 \leq X \leq 2$ etc is accepted
To describe the critical regions they can use any letter or no letter at all. It does not have to be X.

(c) **B1**   correct answer only

(d) Follow through 15 and their critical region
B1 for any one of the 5 correct statements up to a maximum of B2
– **B1** for any incorrect statements

Question Number	Scheme	Marks
Q7 (a)		

(a)

x	1p	2p
P($X = x$)	$\dfrac{1}{4}$	$\dfrac{3}{4}$

$\mu = 1 \times \dfrac{1}{4} + 2 \times \dfrac{3}{4} = \dfrac{7}{4}$ or $1\dfrac{3}{4}$ or 1.75   **B1**

$\sigma^2 \quad = 1^2 \times \dfrac{1}{4} + 2^2 \times \dfrac{3}{4} - \left(\dfrac{7}{4}\right)^2$ **M1**

$\qquad = \dfrac{3}{16}$ or 0.1875   **A1**

     (3)

(b) (1,1,1) , (1,1,2) any order, (1,2,2) any order, (2,2,2)   **B1**

    (1,2,1) (2,1,1) (2,1,2) (2,2,1)   all 8 cases considered.   **B1**

                        May be implied by 3 * (1,1,2) and 3*(1,2,2)

     (2)

(c)

$\bar{x}$	1	$\dfrac{4}{3}$	$\dfrac{5}{3}$	2
P($\bar{X} = \bar{x}$)	$\dfrac{1}{4} \times \dfrac{1}{4} \times \dfrac{1}{4} = \dfrac{1}{64}$	$3 \times \dfrac{1}{4} \times \dfrac{1}{4} \times \dfrac{3}{4} = \dfrac{9}{64}$	$3 \times \dfrac{1}{4} \times \dfrac{3}{4} \times \dfrac{3}{4} = \dfrac{27}{64}$	$\dfrac{3}{4} \times \dfrac{3}{4} \times \dfrac{3}{4} = \dfrac{27}{64}$

B1
M1 A1
M1 A1A1

     (6)

Total [11]

Notes

Q7 (a) B1 1.75 oe

M1 for using $\sum (x^2 p) - \mu^2$

A1 0.1875 oe

(b) ignore repeats

(c) 1st B1 4 correct means (allow repeats)

1st M1 for p^3 for either of the ends

1st A1 for 1/64 or awrt 0.016 **and** 27/64 or awrt 0.422

2nd M1 $3 \times p^2(1-p)$ for either of the middle two $0 < p < 1$

May be awarded for finding the probability of the 3 samples with mean of either 4/3 or 5/3 .

2nd A1 for 9/64 (or 3/64 three times) and 27/64 (or 9/64 three times) accept awrt 3dp.

3rd A1 fully correct table, accept awrt 3dp.