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# A-LEVEL

# Mathematics

Statistics 2B – MS2B

Mark scheme

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6360  
June 2014

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Version/Stage: Final

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Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from [aqa.org.uk](http://aqa.org.uk)

### Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
✓ or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
-x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

**Otherwise we require evidence of a correct method for any marks to be awarded.**

## A-level Mathematics June 2014 MS2B

Q1	Solution	Marks	Total	Comments
(a)	Sample mean = $1904 \div 5 = 380.8$ $s = 4.38$ or $s^2 = 19.2$ $t_4 = 2.132$ C.I. = $380.8 \pm 2.132 \times \frac{4.38}{\sqrt{5}}$ or $\sqrt{(19.2/5)}$ $= (377, 385)$	B1 B1 B1 M1 m1 A1	          <b>6</b>	CAO AWR AWR 2.13 Use of their $4.38/\sqrt{5}$ or $\sqrt{(19.2/5)}$ Rest of formula (using $t_4$ or $t_5$ (2.015)) AWR
(b)	3	B1	<b>1</b>	CAO
			<b>7</b>	

Q2	Solution					Marks	Total	Comments
(a)		<b>E</b>	<b>S</b>	<b>W</b>	<b>NI</b>	<b>Total</b>	B2,1	B2 all correct, B1 one slip.
	<b>Male</b>	57	44	27	17	145		
	<b>Female</b>	39	43	19	4	105		
	<b>Total</b>	96	87	46	21	250		
						<b>2</b>		
(b)	Expected	<b>E</b>	<b>S</b>	<b>W</b>	<b>NI</b>		M1	Expected attempted, at least 2 correct to 3 s.f.
	<b>Male</b>	55.68	50.46	26.68	12.18			
	<b>Female</b>	40.32	36.54	19.32	8.82			
							M1	(O – E) <sup>2</sup> /E attempted, at least 1 correct to 3 s.f.
		0.03129..	0.82702..	0.00383..	1.90742..			
		0.04321..	1.14207..	0.00530..	2.63405..		A1	AWFW 6.58 – 6.60
							B1	CAO
							B1	AWRT 6.25 B2 for just 6.25 seen
							B1	At least 1 correct – must be in context.
							A1	Comparison of 6.59 with 6.251
							Dep on 6.59 A1 and 6.251 B1 and on hypotheses B1	
						E1	Conclusion in context Dep on previous A1 and B1	
						<b>8</b>		
(c)	More females than expected from Scotland Fewer females than expected from N.I. About the right number of females from England and/or Wales					B1		For any one of these
						<b>1</b>		
						<b>11</b>		

If they combine Wales and Northern Ireland

Q2	Solution			Marks	Total	Comments	
(b)	Expected	<b>E</b>	<b>S</b>	<b>W + NI</b>		M1	Expected attempted, at least 2 correct to 3 s.f.
	<b>Male</b>	55.68	50.46	38.86			
	<b>Female</b>	40.32	36.54	28.14			
						M1	(O – E) <sup>2</sup> /E attempted, at least 1 correct to 3 s.f.
		0.03129..	0.82702..	0.67986..			
		0.04321..	1.14207..	0.93886		A0	
						B1F	AWFW 4.60 to 4.61
						B1F	B2F for just 4.60 or 4.61 seen
						B1	At least 1 correct – must be in context
						A0	
					E0		
						A maximum of 5 out of 8	

Q3	Solution	Marks	Total	Comments
(a)	$P(X \leq 4) = 0.3$ So $P(\text{Both} \leq 4) = 0.3^2 = 0.09$	M1 A1	2	CAO
(b)(i)	$0.1 + 0.2 + a + 0.3 + b = 1$ so $a + b = 0.4$ $3 \times 0.1 + 4 \times 0.2 + 5a + 6 \times 0.3 + 7b = 5.1$ $5a + 7b = 2.2$ and $5a + 5b = 2.0$ or substitution of $b = 0.4 - a$ or $a = 0.4 - b$ leading to $a = 0.3, b = 0.1$	B1 M1  m1 A1	4	Correct treatment of simultaneous equations, starting with correctly simplified $5a + 7b = 2.2$ CAO
(ii)	$E(X^2) = 0.1 \times 3^2 + 0.2 \times 4^2 + 0.3 \times 5^2 + 0.3 \times 6^2 + 0.1 \times 7^2$ (= 27.3) $\text{Var}(X) = E(X^2) - E(X)^2 = 27.3 - 5.1^2 = 1.29$	M1 A1	2	Not simply $E(X^2) = 27.3$ AG
(iii)	Using $N = 2X - 5$ $E(N) = 2E(X) - 5 = 5.2$ $\text{Var}(N) = 2^2 \text{Var}(X) = 5.16$ so $\sigma_N = 2.27$	M1 A1 A1	3	Or by use of 1, 3, 5, 7, 9 AWRT Or $2 \times \sqrt{1.29}$
			11	

Q4	Solution	Marks	Total	Comments
(a)(i)	Area of rectangle = 1 (or total probability) $= \frac{1}{k} \times (b - a) \rightarrow (b - a) = k$	M1 A1	2	AG
(ii)	$E(X) = \frac{1}{2}(a + b)$ (or $a + \frac{1}{2}k$ )	B1	1	
(iii)	$E(X^2) = \int_a^b \frac{x^2}{k} dx$ $= \left[ \frac{1}{3k} x^3 \right]_a^b$ $= \frac{(b^3 - a^3)}{3(b - a)} = \frac{1}{3}(b^2 + ab + a^2)$	M1  m1 A1	3	$k$ or $(b - a)$ For integration. Ignore limits Use of correct limits AG
(iv)	$\text{Var}(X) = E(X^2) - [E(X)]^2$ $= \frac{1}{12}(b^2 + ab + a^2) - \frac{3}{12}(a + b)^2$ $= \frac{1}{12}(b^2 - 2ab + a^2) = \frac{1}{12}(b - a)^2$	M1 A1	2	Applied to this case (their mean) Either form or continued to $\frac{1}{12}k^2$
(b)	$\frac{1}{12}(b - a)^2 = 3 \rightarrow (b - a) = 6$ $b = 10$ $E(X) = \frac{1}{2}(a + b) = 7$	M1 A1 A1	3	
			11	

Q5	Solution	Marks	Total	Comments
(a)	$\mu = 128 \div 40 = 3.2$ as required for $\lambda$ $s^2 = 3.2410\dots$ (Condone $\sigma^2 = 3.16$ ) which is close to $\lambda$ , as required for Poisson	B1 B1 E1	<b>3</b>	AWRT 3.24 or 3.16 Clearly stated (for either $s^2$ or $\sigma^2$ )
(b)(i)	$1 - P(X \leq 5) = 1 - 0.8946$ $= 0.105(4)$	M1 A1	<b>2</b>	For attempt to subtract $P(X \leq 5)$ AWRT
(ii)	$P(X \leq 7) - P(X \leq 2)$ $0.9832 - 0.3799$ $= 0.603(3)$	M1 B1 A1	<b>3</b>	Attempt to use these two For either. AWFW 0.603 to 0.604
(iii)	$P(X = 0) = 0.0408$ or $e^{-3.2}$ or $P(X \geq 0) = 0.9592$ $1 - 0.9592^2$ (or $0.0408^2 + 2 \times 0.0408 \times 0.9592$ ) $= 0.0799$	B1 M1 A1	<b>3</b>	For any of these seen to 3 d.p. AWFW 0.079 to 0.081
(c)	Using Po(8.2) $e^{-8.2} \times 8.2^9 \div 9! + e^{-8.2} \times 8.2^{10} \div 10!$ $= 0.231$	M1 m1 A1	<b>3</b>	Stated or use in formula or either of figures below seen Or Calc $P(\leq 10) - P(\leq 8)$ $= 0.79555 - 0.56465$ AWRT
			<b>14</b>	

Q6	Solution	Marks	Total	Comments
(a)	$H_0: \mu = 20, H_1: \mu \neq 20$ $\bar{x} = 22.625$ $s = 4.5650066$ (or $\sigma = 4.27$ ) test stat = $\frac{22.625 - 20}{(4.5650066 \div \sqrt{8})}$ = 1.626 $t_7 = \pm 1.895$ Test statistic not in critical region, accept $H_0$ There is insufficient evidence that Gary does not take a mean time of 20 minutes for an annual service.  Alternative: If the boundaries of the critical region are calculated, marks as above except $20 \pm 1.895 \times (4.5650066 \div \sqrt{8})$ M1 ((16.94), 23.06) A1 (AWRT)	B1 B1 B1 M1 A1 B1 A1 E1	8	Both CAO AWFW 4.56 – 4.57 (or AWRT 4.27)  Or $\sqrt{7}$ if $\sigma = 4.27$ used  AWRT 1.63  Comparison of test stat with $t_7$ In context. These last two marks dep on both A1s and hypotheses B1. E1 also dep on previous A1.
(b)	5% sig gives $z = 1.64$ to $1.65$ $20 + 1.6449 \times (4.6 \div \sqrt{100})$ = $20 + 0.754$ to $0.759$ So to not support suspicion need $\bar{x} \leq 20.75$  SC 20.76 using this method scores B1, M1, A1, A0	B1 M1 A1 A1	4	AWFW OE AWFW
			12	



Q7	Solution	Marks	Total	Comments
(a)	$P(X < 1) = \int_0^1 \frac{4x}{5} dx \quad \text{or } \frac{1}{2} \times 1 \times \frac{4}{5}$ $= \left[ \frac{2}{5} x^2 \right]_0^1 = \frac{2}{5}$	M1 A1	2	Including limits
(b)(i)	$\int_1^x \frac{1}{20}(3t^2 - 20t + 33) dt$ $= \left[ \frac{1}{20}(t^3 - 10t^2 + 33t) \right]_1^x$ $= \frac{1}{20}(x^3 - 10x^2 + 33x) - \frac{1}{20}(1 - 10 + 33)$ $F(x) = \frac{2}{5} + \frac{1}{20}(x^3 - 10x^2 + 33x) - \frac{24}{20}$ $= \frac{1}{20}(x^3 - 10x^2 + 33x - 16)$	M1 A1 m1 A1	4	Accept x integral Correct integration with limits Use of limits With $\frac{2}{5}$ included AG
(ii)	<p> <math>F(1.13) = 0.49819\dots</math>  <math>F(1.14) = 0.50527\dots</math>            Median requires <math>F(x) = 0.5</math>  <math>0.49819\dots &lt; 0.5 &lt; 0.50527\dots</math>            So <math>1.13 &lt; \text{median} &lt; 1.14</math> </p> <p>           Alternative scheme for (b)(ii)            If a calculator, or trial and improvement, has been used to solve the cubic equation directly:  <math>\frac{1}{20}(x^3 - 10x^2 + 33x - 16) = 0.5</math>            median = AFWW 1.132 to 1.133            which lies between 1.13 and 1.14         </p>	B1 B1  E1  M1 A1 E1	3	At least 3 s.f. At least 3 s.f.  Must clearly indicate that median requires $F(x) = 0.5$
			9	