

Version 1.0



**General Certificate of Education (A-level)  
June 2011**

**Mathematics**

**MS2B**

**(Specification 6360)**

**Statistics 2B**

**Final**

***Mark Scheme***

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## Key to mark scheme abbreviations

|              |  |
|--------------|--|
| M            | mark is for method   |
| m or dM      | mark is dependent on one or more M marks and is for method         |
| A            | mark is dependent on M or m marks and is for accuracy              |
| B            | mark is independent of M or m marks and is for method and accuracy |
| E            | mark is for explanation  |
| ✓ or ft or F | follow through from previous incorrect result                      |
| CAO          | correct answer only  |
| CSO          | correct solution only  |
| AWFW         | anything which falls within  |
| AWRT         | anything which rounds to   |
| ACF          | any correct form   |
| AG           | answer given   |
| SC           | special case   |
| OE           | or equivalent  |
| A2,1         | 2 or 1 (or 0) accuracy marks                                       |
| -x EE        | deduct x marks for each error                                      |
| NMS          | no method shown  |
| PI           | possibly implied   |
| SCA          | substantially correct approach                                     |
| c            | candidate  |
| sf           | significant figure(s)  |
| dp           | decimal place(s)   |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

**Otherwise we require evidence of a correct method for any marks to be awarded.**

## MS2B

| Q       | Solution  | Marks                        | Total     | Comments   |
|---------|---|------------------------------|-----------|--|
| 1(a)(i) | $X \sim \text{Po}(13)$  | B1                           | 1         | Both Poisson and $\lambda = 13$  |
| (ii)    | $P(X = 20) = P(X \leq 20) - P(X \leq 19)$ $= 0.975(0) - 0.957(3)$ [allow 0.975 – 0.957 ]<br>$= 0.0177 \text{ (3sf)}$  | M1<br><br>A1                 | 2         | Must use $\lambda = 13$ otherwise M0A0<br><br>AFWW 0.0176 to 0.018<br><b>or</b> $P(X = 20) = \frac{e^{-13} \times 13^{20}}{20!}$ M1<br>$= 0.0177$ A1   |
| (iii)   | $P(6 \leq X \leq 18) = P(X \leq 18) - P(X \leq 5)$ $= 0.930(2)$ $- (0.0107 \text{ or } 0.0259)$ $= 0.920 \text{ (3sf)}$   | M1<br><br>M1<br>A1           | 3         | AWFW 0.919 to 0.92   |
| (b)     | Cars not random<br>Cars not independent<br>Mean and Variance of cars different / not equal<br><br>Mean / Average / $\lambda$ / 2.6<br><br>greater / less / smaller / different / variable / not constant / too small / too large<br><br>Any contextual reason that suggests a change in traffic flow, eg due to:<br>rush hour / congestion / traffic jams / accidents / work traffic / school traffic / peak time | B1<br><br><br><br><br><br>B1 | 2         | Allow (number of) cars not random / not independent<br><br>B1 for any one of these 3 statements<br>Must indicate a reference to <b>cars</b><br><br>Correct comment about value of $\lambda \neq 2.6$<br><br>Any combination (one from each group):<br><br>eg<br>mean greater <i>due to</i> rush hour, <b>or</b><br>$\lambda$ smaller <i>due to</i> congestion, <b>or</b><br>2.6 too small <i>due to</i> school traffic |
| (c)     | $Y \sim \text{Bin}(20, 0.2)$<br>$P(Y \geq 5) = 1 - P(Y \leq 4)$<br><br>$= 1 - 0.6296$<br><br>$= 0.37(0) \text{ (3sf)}$  | M1<br><br>A1                 | 2         | <b>or:</b><br>$1 - \left( \begin{array}{l} 0.01153 + 0.05765 + 0.13691 \\ + 0.20536 + 0.21820 \end{array} \right)$<br>$1 - 0.6296$<br>(Allow $1 - 0.8042$ seen for M1)   |
| (d)     | $X$ and $Y$ independent<br><br>$p = 0.0177 \times 0.3704$<br>$= 0.00656 \text{ (3sf)}$  | B1<br><br>M1<br>A1           | 3         | Any statement which indicates two / both events are independent<br><br>[their (c)] $\times$ [their (a)(ii)]<br>AFWW 0.0065 and 0.0067  |
|         |   |                              | <b>13</b> |  |

## MS2B (cont)

| Q            | Solution   | Marks   | Total     | Comments   |
|--------------|--|---------|-----------|--|
| 2(a)(i)      | Area / $F(x) = 10u \times 0.01\pi$ (OE)  | B1      | 2         | Shown by any correct method<br><br><b>Alternatives:</b><br>$f = \frac{1}{10u}$ B1<br>Show $u = \frac{10}{\pi}$ or show $\frac{1}{10u} = 0.01\pi$<br>Bdep1  |
|              | $= 1 \Rightarrow u = \frac{10}{\pi}$   | Bdep1   |           |  |
| (ii)         | or<br>$u = \frac{10}{\pi} \Rightarrow F(x) = 1$  | (Bdep1) | 1         | Must be in terms of $\pi$ (eg $60\pi^{-1}$ )<br><br><b>Alternatives:</b><br>$\frac{10000}{12\pi^2} = \frac{5000}{6\pi^2} = \frac{2500}{3\pi^2} = \left(\frac{50}{\pi\sqrt{3}}\right)^2 = \frac{(AWRT\ 833)}{\pi^2}$<br>Must be in terms of $\pi$   |
|              | $E(X) = \frac{1}{2}(11u + u) = 6u = 6 \times \frac{10}{\pi} = \frac{60}{\pi}$  | B1      |           |  |
| (iii)        | $\text{Var}(X) = \frac{1}{12}(b-a)^2$  | B1      | 1         | Must be in terms of $\pi$  |
|              | $\text{Var}(X) = \frac{1}{12}(11u - u)^2$  |         |           |  |
|              | $= \frac{1}{12} \times 100 \times \frac{100}{\pi^2} = \frac{100^2}{12\pi^2}$   |         |           |  |
|              |  |         |           |  |
| (iii)        | $C = \pi \left( X + \frac{10}{\pi} \right)$  | M1      | 4         | Their <b>numerical</b> value of $E(X)$ used correctly<br>Must have a multiplier of $\pi$ or $2\pi$<br><br>CAO<br><br>$\pi^2 \times [\text{their } \text{Var}(X) > 0]$<br>Must have a multiplier of $\pi^2$ or $4\pi^2$<br><br><b>Alternatives:</b><br>$\frac{10000}{12} = \frac{5000}{6} = \frac{2500}{3}$<br>Must be exact: 833.3 gets A0 |
|              | $E(C) = \left. \begin{array}{l} \pi \times [\text{their } E(X)] + 10 \\ \pi \times \frac{60}{\pi} + 10 \end{array} \right\}$             |         |           |  |
|              | $= 70$   |         |           |  |
|              | $\text{Var}(C) = \pi^2 \times \frac{100^2}{12\pi^2} = \frac{100^2}{12}$  |         |           |  |
| (b)          | $n = 100$ and $\bar{a} = 40.5$   | B1      | 3         | For $z = 1.96$<br><br>$z = 1.96$ or 1.64 to 1.65 only<br><br>AWRT  |
|              | $95\% \text{ CI for } \mu = \left. \begin{array}{l} 40.5 \pm z \times \frac{\sqrt{25}}{\sqrt{100}} \\ 40.5 \pm 1.0 \end{array} \right\}$ |         |           |  |
|              | $= (39.5, 41.5)$   |         |           |  |
| <b>Total</b> |  |         | <b>11</b> |  |

## MS2B (cont)

| Q    | Solution   | Marks | Total     | Comments  |
|------|--|-------|-----------|---|
| 3(a) | H <sub>0</sub> : no association (between type of school and performance of 16 year olds in their GCSEs)  | B1    | 1         | H <sub>0</sub> : type of school and performance of 16 year olds in their GCSEs independent  |
| (b)  | $\frac{(O-E)^2}{E}$ 0.195819311<br>0.482160711<br>0.003569447<br>1.080536181<br><br>0.062507172<br>1.269422099<br>0.785491128<br>0.183802623<br><br>0.541856652<br>0.044011976<br>3.274102564<br>4.096492891 | M1    |           | Attempt at $\frac{(O-E)^2}{E}$<br>(≥ 4 correct values seen to 2dp)  |
|      | $X^2 = \sum \frac{(O-E)^2}{E}$<br>$= 12.01977275$ $= 12.0 \text{ (1dp)}$   | m1    |           | Attempt to add ≥ 8 terms  |
|      |  | A1    | 3         | Allow $11.9 \leq X^2 \leq 12.1 \Rightarrow M1m1$<br>CAO   |
| (c)  | $\nu = 6 \Rightarrow \chi_{1\%}^2 = 16.8(12)$  | B1,B1 |           | $\nu = 6$ can be implied by $\chi_{1\%}^2 = 16.8(12)$   |
|      | <b>No</b> (significant evidence to suggest an <b>association between</b> (type of) <b>school and</b> (GCSE) <b>performance</b> (of 16 year olds))  | Adep1 | 3         | Insufficient/no evidence to support Emily's belief.<br>School and performance are independent.<br>Correct conclusion <b>in context</b><br>Dep on B1M1m1B1B1 given in (a), (b), (c) <b>and</b> $11.9 \leq X^2 \leq 12.1$ |
| (d)  | More than expected gained at least / more than 5 GCSEs<br>Fewer than expected gained at least / more than 1 GCSE but less than 5 GCSEs<br>Fewer than expected gained no GCSEs                                | B1    | 1         | Since conclusion of <b>no association</b> between school and GCSE performance, it may be misleading to look at individual differences in any great detail<br>Any one of these 4 comments seen                           |
| (e)  | $\chi_{10\%}^2 = 10.6(45)$   | B1    |           | Correct value of $\chi^2$ only  |
|      | Reject H <sub>0</sub> at 10% level of significance. (Evidence to suggest) an <b>association between</b> (type of) <b>school and</b> (GCSE) <b>performance</b>  | Bdep1 | 2         | Evidence to support Emily's (Joanne's) belief. (Type of) school + (GCSE) performance dependent.<br>Dep on B1M1m1 <b>and</b> $11.9 \leq X^2 \leq 12.1$ <b>and</b> B1 in (e)  |
|      | <b>Total</b>   |       | <b>10</b> |   |

## MS2B (cont)

| Q            | Solution  | Marks                   | Total           | Comments   |                 |   |   |     |    |    |                 |    |   |     |                |                |                |                 |                 |                |   |   |
|--------------|---|-------------------------|-----------------|--|-----------------|---|---|-----|----|----|-----------------|----|---|-----|----------------|----------------|----------------|-----------------|-----------------|----------------|---|---|
| 4(a)         | $E(X) = \sum xp$ $= \frac{3}{40} + \left(2 \times \frac{6}{40}\right) + \left(3 \times \frac{9}{40}\right) + \left(4 \times \frac{12}{40}\right) + \left(5 \times \frac{5}{20}\right) = 3.5$  | B2,1                    | 2               |  |                 |   |   |     |    |    |                 |    |   |     |                |                |                |                 |                 |                |   |   |
| (b)(i)       | $E\left(\frac{1}{X}\right) = \sum \frac{1}{x} \times p$ $= \left(1 \times \frac{3}{40}\right) + \left(\frac{1}{2} \times \frac{6}{40}\right) + \left(\frac{1}{3} \times \frac{9}{40}\right) + \left(\frac{1}{4} \times \frac{12}{40}\right) + \left(\frac{1}{5} \times \frac{5}{20}\right)$ $= \frac{7}{20}$  | M1<br>A1                | 2               | At least 4 of these terms added (accept decimal equivalents)<br>AG (allow 0.35 seen)   |                 |   |   |     |    |    |                 |    |   |     |                |                |                |                 |                 |                |   |   |
| (ii)         | $E\left(\frac{1}{X^2}\right) = \sum \frac{1}{x^2} \times p$ $= \left(1 \times \frac{3}{40}\right) + \left(\frac{1}{4} \times \frac{6}{40}\right) + \left(\frac{1}{9} \times \frac{9}{40}\right) + \left(\frac{1}{16} \times \frac{12}{40}\right) + \left(\frac{1}{25} \times \frac{5}{20}\right)$ $= \frac{133}{800} \quad (0.16625)$ $\text{Var}\left(\frac{1}{X}\right) = \frac{133}{800} - \frac{49}{400}$ $= \frac{7}{160}$   | M1<br>A1<br>m1<br>Adep1 | 4               | At least 4 of these terms added (accept decimal equivalents) (can be implied by $\frac{133}{800}$ seen with no other working shown)<br>$\left[ \text{their } E\left(\frac{1}{X^2}\right) \right] - \left(\frac{7}{20}\right)^2$<br>AG (allow 0.04375 seen) |                 |   |   |     |    |    |                 |    |   |     |                |                |                |                 |                 |                |   |   |
| (c)(i)       | <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td><math>x</math></td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td><math>y</math></td> <td>40</td> <td>20</td> <td><math>13\frac{1}{3}</math></td> <td>10</td> <td>8</td> </tr> <tr> <td><math>p</math></td> <td><math>\frac{3}{40}</math></td> <td><math>\frac{6}{40}</math></td> <td><math>\frac{9}{40}</math></td> <td><math>\frac{12}{40}</math></td> <td><math>\frac{10}{40}</math></td> </tr> </table> <p>Identifying <math>X = (2), 3, 4, 5</math> <b>or</b><br/> <math>Y = (20), 13\frac{1}{3}, 10, 8</math></p> $P(X > 2) = \frac{9}{40} + \frac{12}{40} + \frac{5}{20}$ $= P(Y < 20)$ $= \frac{31}{40} \quad (0.775)$ | $x$                     | 1               | 2  | 3               | 4 | 5 | $y$ | 40 | 20 | $13\frac{1}{3}$ | 10 | 8 | $p$ | $\frac{3}{40}$ | $\frac{6}{40}$ | $\frac{9}{40}$ | $\frac{12}{40}$ | $\frac{10}{40}$ | M1<br>A1<br>A1 | 3 | <b>Alternative:</b><br>$Y < 20 \Rightarrow \frac{40}{X} < 20 \Rightarrow 40 < 20X \Rightarrow X > 2$<br>M1 (allow $<$ or $\leq$ <b>and</b> $>$ or $\geq$ in above)<br>$P(Y < 20) = P(X > 2)$<br>$= 1 - \left(\frac{3}{40} + \frac{6}{40}\right) \quad \text{A1}$<br>$= \frac{31}{40} \quad (0.775) \quad \text{A1}$ |
| $x$          | 1   | 2                       | 3               | 4  | 5               |   |   |     |    |    |                 |    |   |     |                |                |                |                 |                 |                |   |   |
| $y$          | 40  | 20                      | $13\frac{1}{3}$ | 10   | 8               |   |   |     |    |    |                 |    |   |     |                |                |                |                 |                 |                |   |   |
| $p$          | $\frac{3}{40}$  | $\frac{6}{40}$          | $\frac{9}{40}$  | $\frac{12}{40}$  | $\frac{10}{40}$ |   |   |     |    |    |                 |    |   |     |                |                |                |                 |                 |                |   |   |
| (ii)         | $\frac{9}{40}$ seen irrespective of labelling<br>$P(X < 4   Y < 20) = \frac{\frac{9}{40}}{\frac{31}{40}} = \frac{0.225}{0.775}$ $= \frac{9}{31} \quad (0.290)$  | B1<br>M1<br>A1          | 3               | As numerator <b>or</b> final answer (0.225)<br>$= \frac{9}{40}$<br>(their (c)(i)) (or correct use of table)<br>AWFW 0.29 to 0.2904   |                 |   |   |     |    |    |                 |    |   |     |                |                |                |                 |                 |                |   |   |
| <b>Total</b> |   |                         | <b>14</b>       |  |                 |   |   |     |    |    |                 |    |   |     |                |                |                |                 |                 |                |   |   |

## MS2B (cont)

| Q      | Solution   | Marks  | Total     | Comments  |
|--------|--|--|-----------|---|
| 5(a)   | $Y \sim N(\mu_y, 640^2)$<br>$n = 25$ and $\bar{y} = 19700$<br><br>$H_0: \mu_y = 20000$<br>$H_1: \mu_y \neq 20000$ (both)<br><br>$\bar{Y} \sim N\left(20000, \frac{640^2}{25}\right)$<br><br>$z = \frac{19700 - 20000}{640/\sqrt{25}}$<br>$= -2.34375$<br><br>$z_{\text{crit}} = \pm 2.5758$<br><br>Accept $H_0$<br><br><b>Insufficient / no evidence</b> (to suggest) that the <b>mean</b> (lifetime) has <b>changed</b> (from 20000 hours)<br><br><b>Mean</b> (lifetime) has <b>not</b> changed at 1% level (of significance) | B1<br><br><br>M1<br>A1<br>B1<br>Adep1<br><br>Edep1 | 6         | <b>Alternative:</b><br>$P(\bar{Y} < 19700) = P(Z < -2.34375)$<br>$= 1 - 0.99036$<br>$= 0.00964 \geq 0.005$ Accept $H_0$<br><br>( - 2.35 to - 2.34)<br>( ± 2.57 to ± 2.58)<br><br>Use of $t \Rightarrow$ max B1M1A1<br><br>dep on B1M1B1<br><br>dep on Adep1<br><br>If incorrect hypotheses then B0<br>$\Rightarrow$ max M1A1B1<br>ie final Adep1Edep1 not available |
| (b)(i) | $\mu < 10000$  | B1   | 1         |   |
| (ii)   | $n = 16$ and $s = 500$ ; $t_{\text{crit}} = 1.753$<br>$\text{sd}(\bar{X}) = \frac{500}{\sqrt{16}}$ (125)<br>Critical value is one of:<br>$10000 \pm 1.753 \times \frac{500}{\sqrt{16}}$ (considered)<br><br>Choose 9780 (3sf)<br><br>( $\Rightarrow$ critical region: $\bar{x} < 9780$ )<br><br>$\therefore$ Range of values for $\bar{x}$ which leads Christine <b>not</b> to reject $H_0: \mu = 10000$ is:<br>$\bar{x} > 9780$   | B1<br>B1<br>M1<br>A1<br><br>A1                     | 5         | For $t_{\text{crit}}$ (ignore signs)<br><br>Ignore notation<br><br>M0 if only considered upper value<br>No ft on incorrect $t$ value<br><br>AFWW 9780 to 9781 (ignore inequality)<br><br>If $z$ used then max B0B1M0A0A0<br><br>Allow $\bar{x} \geq 9780$ to 9781   |
| (iii)  | No error   | B1   | 1         | Ignore any subsequent statements  |
|        | <b>Total</b>   |  | <b>13</b> |   |



## MS2B (cont)

| Q   | Solution  | Marks  | Total | Comments   |   |
|---|---|--|-------|--|---|
| 6(a)  | $F(x) = \int \frac{3}{8}(x^2 + 1) dx$   | M1   |       | Ignore limits  |   |
|   | $= \frac{3}{8} \left[ \frac{x^3}{3} + x \right]$ or $= \frac{1}{8}x^3 + \frac{3}{8}x$ | A1   |       | Either   |   |
|   | $= \frac{1}{8}x(x^2 + 3)$   | A1   | 3     | (including use of correct limits 0 and $x$ or $+c$ used and evaluated) (AG)              |   |
| (b)   | $F(m) = \frac{1}{2}$  | B1   |       |  |   |
|   | $F(1) = \frac{1}{8} \times 1 \times 4 = \frac{1}{2}$                                  | B1   | 2     | AG   |   |
| (c)   | Upper quartile lies in range $1 < x < 2$<br>such that $F(q) = \frac{3}{4}$            |  |       | $\frac{1}{2} + \int_1^q \frac{1}{4}(5 - 2x) dx = \frac{3}{4}$                            |   |
|   | $\int_1^q \frac{1}{4}(5 - 2x) dx = \frac{1}{4}$                                       | M1   |       | <b>Alternative:</b> $\int_q^2 \frac{1}{4}(5 - 2x) dx = \frac{1}{4}$                      |   |
|   | $[5x - x^2]_1^q = 1$  |  |       | $[5x - x^2]_q^2 = 1$   |   |
|   | $5q - q^2 - 4 = 1$  |  |       | $(10 - 4) - (5q - q^2) = 1$  |   |
|   | $q^2 - 5q + 5 = 0$  | A1   |       | $6 - 5q + q^2 = 1$<br>$q^2 - 5q + 5 = 0$   |   |
|   | $q = \frac{5 \pm \sqrt{25 - 20}}{2}$ or $\frac{1}{2}(5 \pm \sqrt{5})$                 | M1   |       | Correct use of formula (OE) to give the two surd answers to given quadratic equation     |   |
|   | but $1 < q < 2$ [or ( $q < 2$ )]  | m1   |       |  |   |
|   | $\therefore q = \frac{1}{2}(5 - \sqrt{5})$  | A1   | 5     | Must qualify with a numerical comparison, not just quote the given answer; dep on M1; AG |   |
|   | (d)   | $P(X > 1.5) = \frac{1}{2} \left[ \frac{1}{2} + \frac{1}{4} \right] \times \frac{1}{2}$ | M1    |  | $P(X < 1.5) = 0.5 + \frac{1}{2} \left[ \frac{3}{4} + \frac{1}{2} \right] \times \frac{1}{2}$ (M1) |
|   |   | $= \frac{3}{16}$ (0.1875)  | A1    |  | $= \frac{1}{2} + \frac{1}{2} \times \frac{5}{4} \times \frac{1}{2}$                               |
| $P(X > q) = \frac{1}{4}$ (0.25)               |   | B1   |       | $= \frac{1}{2} + \frac{5}{16} = \frac{13}{16}$ (A1)                                      |   |
| $P(q < X < 1.5) = \frac{1}{4} - \frac{3}{16}$ |   |  |       | $P(X < q) = \frac{3}{4}$ (0.75) (B1)   |   |
| $= \frac{1}{16}$ (0.0625)                     |   | A1   | 4     | $P(q < X < 1.5) = \frac{13}{16} - \frac{3}{4} = \frac{1}{16}$ (A1)<br>(0.0625)           |   |

## MS2B (cont)

| Q         | Solution  | Marks | Total     | Comments   |
|-----------|---|-------|-----------|--|
| 6(d) cont | <p><b>OR</b></p> $\int_{1.5}^2 \frac{1}{4}(5-2x) dx = \frac{3}{16} \text{ etc (M1A1)}$ <p><b>NB</b> statement <math>F(1.5) - \frac{3}{4} = \frac{1}{16}</math> (OE)<br/>scores 4 marks</p> <p><b>Alternative:</b></p> $\int_q^{1.5} \frac{1}{4}(5-2x) dx = \left[ -\frac{1}{16}(5-2x)^2 \right]_{\frac{5-\sqrt{5}}{2}}^{1.5}$ <p style="text-align: right;">(M1)</p> $= -\frac{1}{16}(4) - \left[ -\frac{1}{16}(\sqrt{5})^2 \right] \text{ (sub) (A1)}$ $= -\frac{4}{16} + \frac{5}{16} \text{ (A1)}$ $= \frac{1}{16} \text{ (A1)}$ |       |           | <p><b>OR</b></p> $\int_q^{1.5} \frac{1}{4}(5-2x) dx = \frac{1}{4} [5x - x^2]_q^{1.5} \text{ (M1)}$ <p>(correct integration and limits)<br/>Allow use of <math>q = 1.38</math> to <math>q = 1.382</math><br/>in limits for M1<br/>Whatever follows <b>must be exact</b></p> $= \frac{1}{4} [(7.5 - 2.25) - (5q - q^2)] \text{ (A1)}$ <p>for use of <math>5q - q^2 = 5</math> <b>or</b> showing<br/><math>5q - q^2 = 5</math> by substituting <math>q = \frac{1}{2}(5 - \sqrt{5})</math><br/>(A1)</p> $= \frac{1}{4} [5.25 - 5] = \frac{1}{16} \text{ (A1)}$ <p><b>Alternative using F(x):</b></p> <p>for <math>1 \leq x \leq 2</math><br/> <math display="block">F(x) = \frac{1}{2} + \int_1^x \frac{1}{4}(5-2x) dx</math> <math display="block">= \frac{1}{2} + \frac{1}{4} [5x - x^2]_1^x</math> <math display="block">= \frac{1}{2} + \frac{1}{4} [(5x - x^2) - (5 - 1)]</math> <math display="block">= \frac{1}{4} (2 + 5x - x^2 - 4)</math> <math display="block">= \frac{1}{4} (5x - x^2 - 2) \text{ (seen or used) (M1)}</math> <math display="block">F(1.5) = \frac{1}{4} (7.5 - 2.25 - 2) = \frac{3.25}{4}</math> <math display="block">= 0.8125 = \frac{13}{16} \text{ (A1)}</math> <math display="block">F(q) = \frac{1}{16} (50 - 10\sqrt{5} - (25 - 10\sqrt{5} + 5) - 8)</math> <math display="block">= \frac{12}{16} \text{ OE (B1)}</math> <math display="block">P(q &lt; X &lt; 1.5) = \frac{13}{16} - \frac{12}{16} = \frac{1}{16} \text{ (A1)}</math></p> |
|           | <b>Total</b>  |       | <b>14</b> |  |
|           | <b>TOTAL</b>  |       | <b>75</b> |  |