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ASSESSMENT and QUALIFICATIONS ALLIANCE

General Certificate of Education

Mathematics 6360

MS2B Statistics 2B

Mark Scheme

2008 examination – June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Key to mark scheme and abbreviations used in marking

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation

√or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
–*x* EE	deduct *x* marks for each error	G	graph
NMS	no method shown	c	candidate
PI	possibly implied	sf	significant figure(s)
SCA	substantially correct approach	dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

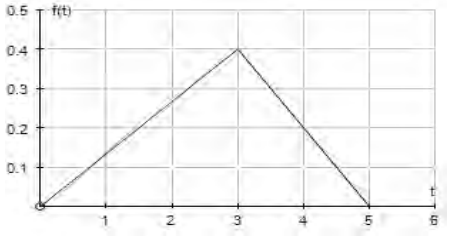
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MS2B

Q	Solution	Marks	Total	Comments
1(a)	O_i | E_i | $\lvert O_i - E_i \rvert - 0.5$ | $\frac{7.5^2}{E_i}$ 52 | 44 | 7.5 | 1.2784 58 | 66 | 7.5 | 0.8523 28 | 36 | 7.5 | 1.5625 62 | 54 | 7.5 | 1.0417 4.7349	M1 M1 M1 A1		E attempted Yates' correction attempted χ^2 attempted AWFW 4.73 to 4.74
	H_0: No association between incidence of asthma and volume of traffic H_1: Association	B1		at least H_0 stated correctly
	$\nu = 1$ $\chi^2_{\text{crit}} = 3.841 < 4.7349$	B1		critical value
	Reject H_0 at 5% level	A1ft		
	Evidence to suggest an association between the incidence of asthma in children and the volume of traffic where they live	E1ft	8	
(b)	More than expected had asthma	E1	1	dep on statement of association
	Total		**9**	
2(a)	$P(X = 8) = P(X \le 8) - P(X \le 7)$ $= 0.8472 - 0.7440$	M1		$P(X = 8) = \frac{e^{-6}(6^8)}{8!}$
	$= 0.103$	A1	2	
(b)(i)	$\lambda = 9$	B1	1	
(ii)	$P(Y > 9) = 1 - P(Y \le 9)$ $= 1 - 0.5874$	M1		
	$= 0.4126$	A1ft	2	AWFW 0.412 to 0.413
(c)(i)	$T \sim \text{Po}(15)$	B1ft	1	
(ii)	$P(T \le 20) = 0.917$	B1ft	1	
(iii)	$P(T \text{ at least } 21) = 0.083$	B1ft		
	$p = 15 \times (0.083)^4 (0.917)^2$	M1		B(6, (iii)) used
	$= 0.000599$	A1	3	CAO; AWFW 0.000598 to 0.0006
	Total		**10**	

MS2B (cont)

Q	Solution	Marks	Total	Comments
3	$H_0: \mu = 34.5$ $H_1: \mu \neq 34.5$	B1		
	$z_{crit} = \pm 1.96$	B1		
	$z = \dfrac{35.1 - 34.5}{2.5/\sqrt{50}} = 1.70$	M1A1		(1.697)
	Accept H_0	A1		
	Insufficient evidence, at 5% level of significance, to suggest that the mean weight has changed	E1	6	or … to confirm Alan's belief
	Total		**6**	
4(a)		B1 B1 B1	3	line segment on 0 – 3 line segment on 3 – 5 scales (0 – 0.4 vertical; 0 – 5 horizontal)
(b)(i)	$P(T \leq 2) = \dfrac{1}{2} \times 2 \times \dfrac{4}{15}$ $= \dfrac{4}{15}$	M1 A1	2	(0.267)
(ii)	$P(2 < T < 4) = 1 - (P(T < 2) + P(T > 4))$ $= 1 - \left(\dfrac{4}{15} + \dfrac{1}{2} \times \dfrac{1}{5}\right)$ $= 1 - \dfrac{4}{15} - \dfrac{1}{10}$ $= \dfrac{19}{30}$	M1 A1 A1	3	for $P(T > 4) = \dfrac{1}{10}$ $\dfrac{1}{2} d\left[(f_2 + f_4) + 2f_3\right]$ $f_2 = \dfrac{4}{15};\ f_4 = \dfrac{1}{5};\ f_3 = \dfrac{2}{5};\ d = 1$ (0.633)
(c)	$E(T) = \int_0^3 \dfrac{2}{15} t^2 \, dt + \int_3^5 t\left(1 - \dfrac{1}{5}t\right) dt$ $= \left[\dfrac{2}{45}t^3\right]_0^3 + \left[\dfrac{1}{2}t^2 - \dfrac{1}{15}t^3\right]_3^5$ $= \dfrac{6}{5} + \dfrac{25}{6} - \dfrac{27}{10}$ $= 2\dfrac{2}{3}$	M1 B1B1 A1	4	both integrals seen OE
	Total		**12**	

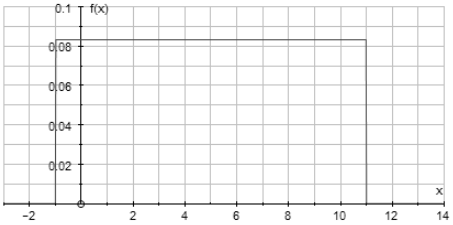
MS2B (cont)

Q	Solution	Marks	Total	Comments
5(a)(i)	$\bar{x} = 3.19$ and $s^2 = \frac{1.849}{9} = 0.2054$	B1		both (s = 0.453)
	$t_9 = 3.250$	B1		
	99% confidence interval: $3.19 \pm 3.250 \times \frac{\sqrt{0.2054}}{\sqrt{10}}$	M1		$3.19 \pm (\text{their } t_9) \times \frac{\sqrt{0.2054}}{\sqrt{10}}$
	$= 3.19 \pm 0.4658$	A1ft		
	$= (2.72, 3.66)$	A1	5	(2.72 to 2.73, 3.65 to 3.66)
(ii)	Reasonable claim, with 3.5 within the 99% confidence interval	B1 E1	2	dep on correct CI in (a)(i)
(b)	$0.01 \times 200 = 2$	B1	1	
	Total		**8**	
6	$\bar{x} = 4.1$ $s = 0.392$ $(s^2 = 0.153)$	B1		both
	$H_0: \mu = 3.8$ $H_1: \mu > 3.8$	B1		both
	$t = \frac{4.1 - 3.8}{0.392/\sqrt{7}} = 2.03$	M1A1		AWFW 2.02 to 2.03
	$t_{crit} = 1.943$	B1ft		
	Reject H_0	A1		
	Evidence at 5% level of significance to support the doctor's belief that the cholesterol level is higher than the management's claim of 3.8	E1		
	Cholesterol levels normally distributed	B1	8	
	Total		**8**	

MS2B (cont)

Q	Solution	Marks	Total	Comments
7(a)(i)	$\mathrm{E}(Y) = \sum y\ \mathrm{P}(Y = y)$ $= 5\times 0.1 + 15\times 0.2 + 25\times 0.3 + 35\times 0.4$ $= 25$	B1		
	$\mathrm{Var}(Y) = \mathrm{E}(Y^2) - [\mathrm{E}(Y)]^2$			
	$= 725 - 25^2$	M1		
	$= 100$	A1		CAO
	Standard deviation = 10	A1ft	4	ft on $\mathrm{Var}(Y) > 0$
(ii)	$C = 10Y + 5$ $\mathrm{E}(C) = 10\mathrm{E}(Y) + 5$ $= 10\times 25 + 5$ $= 255$ pence	B1	1	OE
(b)	$\mathrm{Var}(X) = \mathrm{E}(X^2) - [\mathrm{E}(X)]^2$			
	$= 75.25 - 8.35^2$	M1		
	$= 75.25 - 69.7225$ $= 5.5275$	A1		AWFW 5.52 to 5.53
	$T = 0.4X + 250$ $\mathrm{Var}(T) = \mathrm{Var}(0.4X + 250)$			
	$= 0.4^2 \times \mathrm{Var}(X)$	M1		$\mathrm{Var}(X) > 0$
	$= 0.16\times 5.5275$ $= 0.8844$	A1	4	AWFW 0.884 to 0.885
	Total		**9**	

MS2B (cont)

Q	Solution	Marks	Total	Comments
8(a)	$\mathrm{P}(X<0)=\mathrm{F}(0)$	M1		
	$=\dfrac{1}{k+1}$	A1	2	
(b)	$(q_1+1)\times\dfrac{1}{k+1}=\dfrac{1}{4}$	M1		alternative (from a sketch)
	$q_1+1=\dfrac{1}{4}(k+1)$	A1		
	$q_1=\dfrac{1}{4}(k+1)-1$	A1	3	OE
(c)	$\mathrm{f}(x)=\dfrac{\mathrm{d}}{\mathrm{d}x}(\mathrm{F}(x))$	M1		use of
	$=\dfrac{1}{k+1}\times\dfrac{\mathrm{d}}{\mathrm{d}x}(x+1)$ $=\dfrac{1}{k+1}\quad -1\le x\le k$ $=0\quad$ otherwise	A1	2	AG; $\dfrac{1}{k+1}$ clearly deduced
(d)(i)	$k=11\Rightarrow \mathrm{f}(x)=\begin{cases}\dfrac{1}{12} & -1\le x\le 11\\ 0 & \text{otherwise}\end{cases}$			
	Rectangular distribution:			
		B1		horizontal line on $[-1,11]$
		B1	2	at $\mathrm{f}=\dfrac{1}{12}$
(ii)	$\mathrm{E}(X)=\dfrac{1}{2}(-1+11)=5$	B1		
	$\mathrm{Var}(X)=\dfrac{1}{12}(11--1)^2=12$	B1	2	
(iii)	$\mathrm{P}(q_1<X<\mathrm{E}(X))=\mathrm{P}(2<X<5)$			
	$=(5-2)\times\dfrac{1}{12}$	M1		
	$=0.25$	A1	2	AG
	Total		**13**	
	TOTAL		**75**	