

<b>1</b>	$X \sim B(18, 0.1)$		
<b>(i)</b>	<p>(A) <math>P(2 \text{ faulty tiles}) = \binom{18}{2} \times 0.1^2 \times 0.9^{16} = 0.2835</math></p> <p>OR from tables <math>0.7338 - 0.4503 = 0.2835</math></p> <p>(B) <math>P(\text{More than 2 faulty tiles}) = 1 - 0.7338 = 0.2662</math></p>	<p>M1 <math>0.1^2 \times 0.9^{16}</math>  M1 <math>\binom{18}{2} \times p^2 q^{16}</math>  A1 CAO</p> <p>OR: M2 for <math>0.7338 - 0.4503</math> A1 CAO</p> <p>M1 <math>P(X \leq 2)</math>  M1 <i>dep</i> for <math>1 - P(X \leq 2)</math>  A1 CAO</p>	<b>3</b>
	(C) $E(X) = np = 18 \times 0.1 = 1.8$	M1 for product $18 \times 0.1$ A1 CAO	<b>2</b>
<b>(ii)</b>	<p>(A) Let <math>p</math> = probability that a randomly selected tile is faulty</p> <p><math>H_0: p = 0.1</math>  <math>H_1: p &gt; 0.1</math></p>	<p>B1 for definition of <math>p</math> in context</p> <p>B1 for <math>H_0</math>  B1 for <math>H_1</math></p>	<b>3</b>
	(B) $H_1$ has this form as the manufacturer believes that the number of faulty tiles may <u>increase</u> .	E1	<b>1</b>
<b>(iii)</b>	<p>Let <math>X \sim B(18, 0.1)</math></p> <p><math>P(X \geq 4) = 1 - P(X \leq 3) = 1 - 0.9018 = 0.0982 &gt; 5\%</math>  <math>P(X \geq 5) = 1 - P(X \leq 4) = 1 - 0.9718 = 0.0282 &lt; 5\%</math></p> <p>So critical region is <math>\{5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18\}</math></p>	<p>B1 for 0.0982  B1 for 0.0282  M1 for at least one comparison with 5%  A1 CAO for critical region <i>dep</i> on M1 and at least one B1</p>	<b>4</b>
<b>(iv)</b>	4 does not lie in the critical region, (so there is insufficient evidence to reject the null hypothesis and we conclude that there is not enough evidence to suggest that the number of faulty tiles has increased.	M1 for comparison A1 for conclusion <b>in context</b>	<b>2</b>
		<b>TOTAL</b>	<b>18</b>

2	(i)	$P(20 \text{ correct}) = \binom{30}{20} \times 0.6^{20} \times 0.4^{10} = 0.1152$	M1 $0.6^{20} \times 0.4^{10}$ M1 $\binom{30}{20} \times p^{20} q^{10}$ A1 CAO	[3]
(ii)		Expected number = $100 \times 0.1152 = 11.52$	M1 A1 FT (Must not round to whole number)	[2]
			<b>TOTAL</b>	<b>[5]</b>

<b>3</b>	Median = 3370 Q <sub>1</sub> = 3050    Q <sub>3</sub> = 3700	B1	
<b>(i)</b>	Inter-quartile range = 3700 – 3050 = 650	B1 for Q <sub>3</sub> or Q <sub>1</sub> B1 for IQR	<b>3</b>
<b>(ii)</b>	Lower limit 3050 – 1.5 × 650 = 2075 Upper limit 3700 + 1.5 × 650 = 4675 Approx 40 babies below 2075 and 5 above 4675 so total 45	B1 B1  M1 (for either) A1	<b>4</b>
<b>(iii)</b>	Decision based on convincing argument: eg 'no, because there is nothing to suggest that they are not genuine data items and these data may influence health care provision'	E2 for convincing argument	<b>2</b>
<b>(iv)</b>	All babies below 2600 grams in weight	B2 CAO	<b>2</b>
<b>(v)</b>	(A) $X \sim B(17, 0.12)$ $P(X = 2) = \binom{17}{2} \times 0.12^2 \times 0.88^{15} = 0.2878$  (B) $P(X > 2)$ $= 1 - (0.2878 + \binom{17}{1} \times 0.12 \times 0.88^{16} + 0.8^{17})$ $= 1 - (0.2878 + 0.2638 + 0.1138) = 0.335$	M1 $\binom{17}{2} \times p^2 \times q^{15}$  M1 indep $0.12^2 \times 0.88^{15}$ A1 CAO  M1 for $P(X=1) + P(X=0)$  M1 for $1 - P(X \leq 2)$ A1 CAO	<b>3</b>     <b>3</b>
<b>(vi)</b>	Expected number of occasions is 33.5	B1 FT	<b>1</b>
		<b>TOTAL</b>	<b>18</b>

<p><b>4</b></p> <p><b>(i)</b></p>	<p>(A) <math>P(\text{both}) = \left(\frac{2}{3}\right)^2 = \frac{4}{9}</math></p> <p>(B) <math>P(\text{one}) = 2 \times \frac{2}{3} \times \frac{1}{3} = \frac{4}{9}</math></p> <p>(C) <math>P(\text{neither}) = \left(\frac{1}{3}\right)^2 = \frac{1}{9}</math></p>	<p>B1 CAO</p> <p>B1 CAO</p> <p>B1 CAO</p>	<p><b>3</b></p>
<p><b>(ii)</b></p>	<p>Independence necessary because otherwise, the probability of one seed germinating would change according to whether or not the other one germinates. May not be valid as the two seeds would have similar growing conditions eg temperature, moisture, etc. <i>NB Allow valid alternatives</i></p>	<p>E1</p> <p>E1</p>	<p><b>2</b></p>
<p><b>(iii)</b></p>	<p>Expected number = <math>2 \times \frac{2}{3} = \frac{4}{3}</math> (= 1.33)</p> <p><math>E(X^2) = 0 \times \frac{1}{9} + 1 \times \frac{4}{9} + 4 \times \frac{4}{9} = \frac{20}{9}</math></p> <p><math>\text{Var}(X) = \frac{20}{9} - \left(\frac{4}{3}\right)^2 = \frac{4}{9} = 0.444</math></p> <p><i>NB use of npq scores M1 for product, A1CAO</i></p>	<p>B1 FT</p> <p>M1 for <math>E(X^2)</math></p> <p>A1 CAO</p>	<p><b>3</b></p>
<p><b>(iv)</b></p>	<p>Expect <math>200 \times \frac{8}{9} = 177.8</math> plants</p> <p>So expect <math>0.85 \times 177.8 = 151</math> onions</p>	<p>M1 for <math>200 \times \frac{8}{9}</math></p> <p>M1 dep for <math>\times 0.85</math></p> <p>A1 CAO</p>	<p><b>3</b></p>
<p><b>(v)</b></p>	<p>Let <math>X \sim B(18, p)</math> Let <math>p =</math> probability of germination (for population) <math>H_0: p = 0.90</math> <math>H_1: p &lt; 0.90</math></p> <p><math>P(X \leq 14) = 0.0982 &gt; 5\%</math> So not enough evidence to reject <math>H_0</math> Conclude that there is not enough evidence to indicate that the germination rate is below 90%.</p> <p>Note: use of critical region method scores M1 for region <math>\{0, 1, 2, \dots, 13\}</math> M1 for 14 does not lie in critical region then A1 E1 as per scheme</p>	<p>B1 for definition of <math>p</math></p> <p>B1 for <math>H_0</math></p> <p>B1 for <math>H_1</math></p> <p>M1 for probability</p> <p>M1 dep for comparison</p> <p>A1</p> <p>E1 for conclusion in context</p>	<p><b>7</b></p>
<p style="text-align: right;"><b>TOTAL</b></p>			<p><b>18</b></p>