

1 (i)	$P(A \cap B) = 0.4$	B1 CAO	1
(ii)	$P(C \cup D) = 0.6$	B1 CAO	1
(iii)	Events B and C are mutually exclusive.	B1 CAO	1
(iv)	$P(B) = 0.6$, $P(D) = 0.4$ and $P(B \cap D) = 0.2$	B1 for $P(B \cap D) = 0.2$ soi	
	$0.6 \times 0.4 \neq 0.2$ (so B and D not independent)	E1	2
		TOTAL	5

2 (i)	$P(\text{all jam})$ $= \frac{5}{12} \times \frac{4}{11} \times \frac{3}{10}$ $= \frac{1}{22} = 0.04545$	M1 $5 \times 4 \times 3$ or $\binom{5}{3}$ in numerator M1 $12 \times 11 \times 10$ or $\binom{12}{3}$ in denominator A1 CAO	3
(ii)	$P(\text{all same})$ $= \frac{5}{12} \times \frac{4}{11} \times \frac{3}{10} + \frac{4}{12} \times \frac{3}{11} \times \frac{2}{10} + \frac{3}{12} \times \frac{2}{11} \times \frac{1}{10}$ $= \frac{1}{22} + \frac{1}{55} + \frac{1}{220} = \frac{3}{44} = 0.06818$	M1 Sum of 3 reasonable triples or combinations M1 Triples or combinations correct A1 CAO	3
(iii)	$P(\text{all different})$ $= 6 \times \frac{5}{12} \times \frac{4}{11} \times \frac{3}{10}$ $= \frac{3}{11} = 0.2727$	M1 5,4,3 M1 $6 \times$ three fractions or $\binom{12}{3}$ denom. A1 CAO	3
(iv)	$P(\text{all jam given all same}) = \frac{\frac{1}{22}}{\frac{3}{44}} = \frac{2}{3}$	M1 Their (i) in numerator M1 Their (ii) in denominator A1 CAO	3
(v)	$P(\text{all jam exactly twice})$ $= \binom{5}{2} \times \left(\frac{1}{22}\right)^2 \times \left(\frac{21}{22}\right)^3 = 0.01797$	M1 for $\binom{5}{2} \times \dots$ M1 for their $p^2 q^3$ A1 CAO	3
(vi)	$P(\text{all jam at least once})$ $= 1 - \left(\frac{21}{22}\right)^5 = 0.2075$	M1 for their q^5 M1 indep for $1 - 5^{\text{th}}$ power A1 CAO	3
TOTAL			18

3	<p>(i)</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td></td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> <tr> <td>1</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> <tr> <td>2</td> <td>2</td> <td>2</td> <td>6</td> <td>4</td> <td>10</td> <td>6</td> </tr> <tr> <td>3</td> <td>3</td> <td>6</td> <td>3</td> <td>12</td> <td>15</td> <td>6</td> </tr> <tr> <td>4</td> <td>4</td> <td>4</td> <td>12</td> <td>4</td> <td>20</td> <td>12</td> </tr> <tr> <td>5</td> <td>5</td> <td>10</td> <td>15</td> <td>20</td> <td>5</td> <td>30</td> </tr> <tr> <td>6</td> <td>6</td> <td>6</td> <td>6</td> <td>12</td> <td>30</td> <td>6</td> </tr> </table> <p>(ii)</p> <p>(A) $P(\text{LCM} > 6) = 1/$</p> <p>(B) $P(\text{LCM} = 5n) = 11/3$</p> <p>(C) $P(\text{LCM} > 6 \cap \text{LCM} = 5n) = 2/9$</p> <p>(iii)</p> <p>$\frac{1}{3} \times \frac{11}{36} \neq \frac{2}{9}$</p> <p>Hence events are not independent</p>		1	2	3	4	5	6	1	1	2	3	4	5	6	2	2	2	6	4	10	6	3	3	6	3	12	15	6	4	4	4	12	4	20	12	5	5	10	15	20	5	30	6	6	6	6	12	30	6	<p>B1</p> <p>B1</p> <p>B1</p> <p>M1 A1 cao</p> <p>M1</p> <p>E1</p>	<p>All correct</p> <p>Use of diagram</p> <p>Use of definition</p>
	1	2	3	4	5	6																																														
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4	<p>(i)</p> <p>(ii)</p>	<p>G1 G1</p> <p>M1</p>	<p>Probabilities Outcomes</p>
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4(A)	$P(\text{First team}) = 0.9^3 = 0.729$	A1	
(B)	$P(\text{Second team}) =$ $0.9 \times 0.9 \times 0.1 + 0.9 \times 0.1 \times 0.5 + 0.1 \times 0.9 \times 0.5$ $= 0.081 + 0.045 + 0.045 = 0.171$	M1 M1 A1	1 correct triple 3 correct triples added
(iii)	$P(\text{asked to leave}) = 1 - 0.729 - 0.171$ $= 0.1$	B1	
(iv)	$P(\text{Leave after two games given leaves})$ $= \frac{0.1 \times 0.5}{0.1} = \frac{1}{2}$	M1 ft A1 cao	Denominator
(v)	$P(\text{at least one is asked to leave})$ $= 1 - 0.9^3 = 0.271$	M1 ft M1 A1 cao	Calc'n of 0.9 $1 - ()^3$
(vi)	$P(\text{Pass a total of 7 games})$ $= P(\text{First, Second, Second}) + P(\text{First, First, Leave after three games})$ $= 3 \times 0.729 \times 0.171^2 + 3 \times 0.729^2 \times 0.05$ $= 0.064 + 0.080$ $= 0.144$	M1 M1 ft M1 ft M1 A1 cao	Attempts both $0.729(0.171)^2$ $0.05(0.729)^2$ multiply by 3

Qn	Answer	Mk	Comment
5	Let $P(B) = x$ Using $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ $0.9 = 2x + x - 0.3$ $x = 0.4$ $P(B) = 0.4$	 M1 M1 A1	 Correct set of equations Correct solution