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| 1 (i) | $X \sim B(10,0.2)$ $P(X < 4) = P(X \leq 3) = 0.8791$ OR attempt to sum $P(X = 0,1,2,3)$ using $X \sim B(10,0.2)$ can score M1, A1 | M1 for $X \leq 3$ A1 | 2 |
| (ii) | Let $p =$ the probability that a bowl is imperfect $H_0 : p = 0.2 \quad H_1 : p < 0.2$ $X \sim B(20,0.2)$ $P(X \leq 3) = 0.2061$ $0.2061 > 5\%$ Cannot reject H_0 and so insufficient evidence to claim a reduction. OR using critical region method: CR is $\{0\}$ B1, 2 not in CR M1, A1 as above | B1 Definition of p B1, B1 B1 for 0.2061 seen M1 for this comparison A1 <i>dep</i> for comment <u>in context</u> | 3 |
| | | TOTAL | 8 |

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| 2 (i) | $X \sim B\left(15, \frac{1}{6}\right)$ $P(X = 0) = \left(\frac{5}{6}\right)^{15} = 0.065$ | M1 A1 cao | $\left(\frac{5}{6}\right)^{15}$ |
| (ii) | $P(X = 4) = \binom{15}{4} \times \left(\frac{1}{6}\right)^4 \times \left(\frac{5}{6}\right)^{11}$ $= 0.142$ (or 0.9102-0.7685) | M1 M1 A1 cao | $\left(\frac{1}{6}\right)^4 \left(\frac{5}{6}\right)^{11}$ multiply by $\binom{15}{4}$ |

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| (iii) | $P(X > 3) = 1 - P(X \leq 3)$ $= 1 - 0.7685 = 0.232$ | M1 A1 | |
| (iv) | Let p = probability of a six on any throw | B1 | Definition of p |
| (A) | $H_0 : p = \frac{1}{6} \quad H_1 : p < \frac{1}{6}$ $X \sim B\left(15, \frac{1}{6}\right)$ $P(X = 0) = 0.065$ <p>$0.065 < 0.1$ and so reject H_0</p> <p>Conclude that there is sufficient evidence at the 10% level that the dice are biased against sixes.</p> | B1 M1 M1 dep E1 dep | Both hypotheses 0.065 Comparison |
| (B) | Let p = probability of a six on any throw | B1 | Both hypotheses |
| | $H_0 : p = \frac{1}{6} \quad H_1 : p > \frac{1}{6}$ $X \sim B\left(15, \frac{1}{6}\right)$ $P(X \geq 5) = 1 - P(X \leq 4) = 1 - 0.910 = 0.09$ <p>$0.09 < 0.1$ and so reject H_0</p> <p>Conclude that there is sufficient evidence at the 10% level that the dice are biased in favour of sixes.</p> | M1 M1 dep E1 dep | 0.09 Comparison |
| (v) | <p>Conclusions contradictory.</p> <p>Even if null hypothesis is true, it will be rejected 10% of the time purely by chance.</p> <p>Or other sensible comments.</p> | E1 E1 | Contradictory By chance |

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| 3 | Number not turning up $X \sim B(16, 0.2)$ | | |
| (i) | $P(X = 0) = 0.8^{16} = 0.0281$ | M1 A1 | 0.8^{16} or tables |
| (ii) | $P(X > 3) = 1 - P(X \leq 3)$ or $P(X \leq 12)$ $= 1 - 0.5981 = 0.4019$ | M1 M1 A1 | Manipulation Use of tables |
| (iii) | $X \sim B(17, 0.2) \rightarrow P(X \geq 1) = 0.9775$ Greater than 0.9 so acceptable | M1 A1 E1 | B(17, 0.2) 0.9775 |
| (iv) | $X \sim B(18, 0.2) \rightarrow P(X \geq 2) = 0.9009$ Can make 18 appointments $X \sim B(19, 0.2) \rightarrow P(X \geq 3) = 0.7631$ | M1 A1 A1 M1 | 18 and ≥ 2 0.9009 18 ok 19 and ≥ 3 |
| (v) | Now $X \sim B(20, p)$ Let p be probability of not turning up. $H_0: p = 0.2$ $H_1: p \neq 0.2$ $P(X \leq 1) = 0.0692 > 2.5\%$ cannot reject H_0 conclude that the proportion of patients not turning up is unchanged. | B1 B1 B1 M1 M1 A1 E1 | 0.0692 correct comparison cannot reject H_0 |