# Mark Scheme 4732 June 2006

#### 4732

#### Mark Scheme

Penalise	2 sfs only once in paper.			
1(i)	Negative, because (grad or coeff of $x$ in $1^{st}$			Neg because x incr & y decr
	equn or x-value or reg coeff or B or $-0.6$ ) is			
	negative	B1	1	
(ii)	$x = -1.6 \ge 7.0 + 21$	M1		Sub $y=7.0$ in $2^{nd}$ eqn. Allow 1 sign error
~ /	x = 9.8			If sub in both must choose 2nd
		A1	2	
			-	
(iii)	y = -0.6(-1.6y + 21) + 13 or similar	M1		Obtain correct eqn in 1 variable.
(111)	y = -0.0(-1.0y + 21) + 15 of similar	1111		Allow 1 num'l error
	$\overline{x} = 5, \ \overline{y} = 10$	A1A1	3	Allow without bars
	x = 3, y = 10	AIAI	3	Allow without bars
Total		6		
	In qus 2 & 3 "prod" means		of tw	vo probabilities"
2(i)	$^{4}/_{7}$ or 0.571 (3 sfs)	B1	1	
(ii)	$\frac{5}{8} \times \frac{4}{7} + \frac{3}{8} \times \frac{5}{8}$	M1M1		M1: one correct prod or add any two prods
				M1: all correct
	$=\frac{265}{448}$ or 0.592 (3 sfs)	A1	3	
(iii)	$^{3}/_{8} \times ^{5}/_{8} + ^{5}/_{8} \times ^{3}/_{7}$	M1M1		M1: one correct prod or add any two prods
(111)				M1: all correct
	$=\frac{225}{448}$ or 0.502 (3 sfs)	A1	3	
Total		7	-	
I otul		-		
3(i)	7!	M1M1		M1: 7!/(a factorial); or $ \div (3! \times 2(!))$
5(1)	$\frac{1}{3! \times 2(!)}$			M1: all correct
	= 420	A1	3	
	- 120	111	5	
(ii)	51	M1		M1: 5! seen (not part of a C) or 5 x 4!
(ii)	$\frac{5!}{2(1)}$	1411		or 120 seen or $\dots \div 2(!)$ alone
	2(!) = 60	Δ 1	2	of 120 seen of $\dots \pm 2(!)$ atome
	- 00	A1	4	
(;;;)	$1 - \frac{4}{7} \frac{x^3}{6}$ or $1 - \frac{4}{C_2} \frac{7}{7} C_2$ or $1 - \frac{4}{P_2} \frac{7}{7} P_2$	N/1N/1		M1.1 prod on 1 $\frac{\pi}{2}$ on 1 $\frac{4}{2}$
(iii)		M1M1		M1:1- prod or 1/ $^{7}C_{2}$ or 1- $^{4}C_{2}$ / (or Ps)
	or $\frac{3}{7}x^{2/6} + \frac{3}{7}x^{4/6} + \frac{4}{7}x^{3/6}$ oe			or add 3 prods or add 2 correct prods $r^{3}C$ $\sqrt{7}C$ $r^{3}C$ $r^{4}C$ $\sqrt{7}C$
	or ${}^{3}C_{2} / {}^{7}C_{2} + {}^{3}C_{1}x^{4}C_{1} / {}^{7}C_{2}$			or ${}^{3}C_{2} / {}^{7}C_{2}$ or ${}^{3}C_{1}x^{4}C_{1} / {}^{7}C_{2}$
				or add $\geq$ 5 out of 7 correct prods
				M1: all correct
	5/ 0.714/0.65		_	
	$= \frac{5}{7}$ or 0.714 (3 sfs)	Al	3	
Total		8		

Note: "(3 sfs)" means "answer which rounds to ... to 3 sfs". If correct ans seen to  $\geq$  3sfs, ISW for later rounding Penalise 2 sfs only once in paper.

#### 4732

#### Mark Scheme

June 2006

4(i)	$\begin{array}{cccc} 0.4207 & \text{or} & 0.421 \ (3 \ \text{sfs}) \\ \text{or} & 0.8^{25} + 25 x 0.8^{24} x 0.2 + \\ \end{array} \\ \end{array}$		B1		or 1 – 0.6167 or 0.3833 (3 sfs)		
	or 0.8 <sup>-2</sup> +25x0.8 <sup>-3</sup> 0.579(3)	B1	2	or 1- (6 correct terms, 0 to 5)			
(ii)	$^{10}C_3 x (1-0.27)^7 x 0.27^3$ = 0.261 (3 sfs)		M1 A1	2			
(iii)	$0.73^9 = 0.059$ $0.73^{10} = 0.043$ n =	Allow "=" thro'out $1 - 0.73^n > 0.95$ or $0.73^n < 0.05$ $n\log 0.73 < \log 0.05$ oe 10	M1 M1 A1	3	or $1 - {}^{n}C_{0} \ge 0.27^{0} \ge 0.73^{n} > 0.95$ oe allow incorrect sign M1 must be correct ft (1 - 0.27) from (ii) for M1M1 10 with incorrect sign in wking: SCB2 10 with just 0.73 <sup>9</sup> = 0.059: M1M1A1		
Total			7				
5(i)	${}^{1}_{/_{3}} + {}^{1}_{/_{4}} + p + q = 1$ oe 0 x ${}^{1}_{/_{3}} + 1$ x ${}^{1}_{/_{4}} + 2p + 3q = 1{}^{1}_{/_{4}}$ oe		B1 B1				
	equalize coeffs, eg mult eqn (i) by 2 or 3 Or make <i>p</i> or <i>q</i> subject of (i) or (ii) $p = \frac{1}{4}, q = \frac{1}{6}$ oe		M1 A1A1	5	allow one error. ft their equns subst or subtr not nec'y		
(ii)	$\sum x^2 p \text{ (not } /4 \text{ or } /3 \text{ etc}) \qquad (= 2^3/_4) \\ - (1^1/_4)^2 \qquad \qquad$		M1 M1		$\geq 2 \text{ non-zero terms correct. dep +ve result}$ indep if +ve result or $x \cdot 1^{1/4} p$ $(\geq 2 \text{ (non-0) terms correct): M2}$ ft (i) $(0 \leq p, q < 1)$ or letters $p, q$ both M1s		
	= $1.1875$ or $1^{3}/_{16}$ oe sd = $\sqrt{(\text{their } 1.1875)}$ = $1.09 (3 \text{ sfs})$		A1 D1f	4	cao den let M1 $\%$ ((192 no.) en /2.75 - 1.66		
Total	$su = \sqrt{(\text{their } 1.18)}$	B1f 9	4	dep 1st M1 & $(+ve no.)$ eg $\sqrt{2.75} = 1.66$			
Total			9				

#### 4732

# Mark Scheme

June 2006

6(i)(a)	Ranks: 2 4 7 5 3 1 6 6 4 1 3 5 7 2	M1		$\geq$ 5 ranks correct in each set
	7 1 6 3 2 5 4 1 7 2 5 6 3 4	A1		all correct
	$\sum d^2$	M1		dep ranks attempted even if opp orders,
	(= 60)			allow arith errors
	$r_{\rm s} = 1 - \frac{6 \times 60}{7 \times 48}$	M1		Correct formula with $n = 7$ , dep $2^{nd}$ M1
	3 7×48			
				calc <i>r</i> for ranks:
				$S_{xx} = S_{yy} = 140 - 28^2/7.$ $S_{xy} = 110 - 28^2/7$
				(= 28) (= -2)
				corr subst in one corr <i>S</i> (any version):M1
	$= -\frac{1}{14}$ or -0.071 (3 dps)	. 1	_	corr subst in $r = S_{xy} / \sqrt{(S_{xx}S_{yy})}$ :M1
	= -714 or $-0.071$ (5 ups)	A1	5	-0.07 without wking: M1A1M2A0
				-0.07 without wking. WIAIW2A0
				No mks unless $ r_s  \leq 1$
(b)	Little (or no) connection (agreement,			ft their $r_s$
	rel'nship) between dist and commission			Must refer to context.
	Allow disagreement			Not "little corr'n between dist and
		B1ft	1	com"
				not "strong disagreement"
				Ignore other comment
(c)	Unchanged. No change in rank	B1B1	2	Ignore other comment
(ii)(a)	= -1	B1	1	indep
(b)	Close to $-1$ or, eg $\approx -0.9$	B1		cao
				not referring to "corr'n" rather than r
				allow "neg", not neg corr'n or neg skew
Total		10		
Total		10		

#### Mark Scheme

June 2006

7(i)				Correct (149.5)	With 150	Tot =
	Midpoints attempted $\geq 2$ classes	M1		<u>concer (11) io j</u>	<u></u>	2000
	$\sum xf / 100 \text{ or } \sum xf / \sum f \text{ attempted } \ge 2 \text{ terms}$	M1				
	x within class, not class width $27.2(1+2)$			2720.5/100	2725/100	Allow
	Mean = 27.2 (to 3 sfs) (not 27.25) art 27.2 from fully correct wking	A1				Ms
	art 27.2 from fully confect wking	AI				
	$\sum x^2 f$ or $\sum x - \overline{x}^2 f$ > 2 terms	M1				& poss
	$\sum x^2 f  \text{or}  \sum x - \overline{x}  )^2 f \ge 2 \text{ terms} \\ \sqrt{(\sum x^2 f / 100 - \overline{x}^2)} \text{ or } \sqrt{((\sum x - \overline{x})^2 f / 100)} \text{ or} $					As
	$\sum f$	M1		27.2	07.05	
	fully corr method, not $\sqrt{neg}$			27.2	27.25	
	= 40.5 to 41.1 (3 sfs)	A1	6	240702.25 40.82	242050 40.96	
	- +0.5 (0 +1.1 (5 515)			allow class widths		nly
(ii)	Recog LQ in $1^{st}$ class <u>&amp;</u> UQ in $3^{rd}$ class	B1		and the clubb when b to 2nd har only		
	Graph: Interp:					
	Attempt $25(.25)^{th}$ value LQ = 3.0 to 4.3   Attempt $75(.75)^{th}$ value UQ = 27 to 29	M1		both nec'y		
	Autompt $75(.75)$ value $6Q = 2710 25$	1111		both nec y		
	Subtract	<b>M</b> 1		dep B1or M1		
	IQR = 23 or 24 or 25	A1	4	integer. dep M2		
(iii)(a)	Increase	B1	1			
(b)	Increase	B1	1	Ignore "probably" etc		
(c) Total	No change	B1	1 13			
10001			15			
8(i)	Geometric.	B1				
	Each attempt (or result or try) indep	B1	2	In context. Not "events,. trials, outcomes". Ignore		
				extra		
(ii)(a)	$(^{2}/_{3})^{3} x^{1}/_{3}$	M2		$({}^{2}/_{3})^{2}x^{1}/_{3}$ or $({}^{2}/_{3})^{4}x^{1}/_{3}$ :		
	$= \frac{8}{81}$ or 0.0988 (3 sfs)	A1	3	allow other numerical " $p$ " (0-		( <i>p</i> <1):M1
			5			
(b)	$\binom{2}{3}^{3}$	<b>M</b> 1		not $(^{2}/_{3})^{3}$ x		
	$\binom{\binom{2}{3}^{3}}{1-\binom{2}{3}^{3}}$	M1		or $\frac{1}{3} + \frac{2}{3}x^{1}/_{3} + \frac{2}{3}x^{2}/_{3}$	$(3)^{2}x^{1}/3$	M2
				$1 - (^2/_3)^4$ or $1 - (^{(*)}_3)^4$		M1
				or 3 terms, with 2 or 3 correct terms		M1 M1
				or " $p$ " + " $qp$ " + " $q$		M1
				or $1 - \text{sum of } 3 \text{ co}$	orrect terms	M1
	$= \frac{19}{27}$ or 0.704 (3sfs)	A1	3	<i>"p"</i> r	neans num val	ue, not $^{1}/_{3}$
	2	D16				
(iii)	3	B1f	1	or $1/p$ .		
(iv)	$1 - \frac{19}{27}$   (1 - 0.7037) or 0.2963	M1		ft (b) for M1M1 m	nust see metho	d if ft
()	$\begin{array}{c c} 1 - \frac{^{19}\!\!/_{27}}{\binom{^{8}\!\!/_{27}}{2} x^{^{19}\!\!/_{27}}} & (1 - 0.7037) \text{ or } 0.2963 \\ 0.2963^2 x \ 0.7037 \end{array}$	M1		Allow figs rounde		
	$= \frac{1216}{19683} = 0.0618 (3 \text{ sfs})$			-		
	$= \frac{1210}{19683}$ = 0.0618 (3 sfs)	A1	3	cao. allow art 0.06	518 or 0.0617	
Total			12			
Total	otal 72 marks	<u> </u>	14			

Total 72 marks