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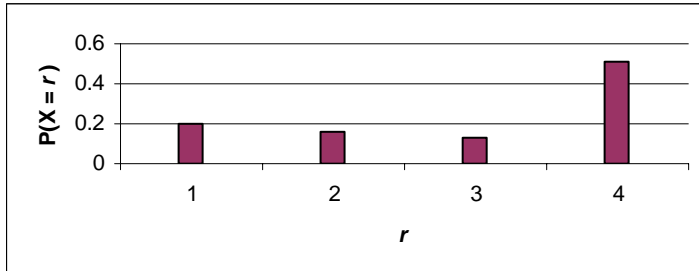
Mark Scheme

January 2008

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Statistics 1

Q1 (i)	Mode = 7 Median = 12.5	B1 cao B1 cao	2
(ii)	Positive or positively skewed	E1	1
(iii)	(A) Median (B) There is a large outlier or possible outlier of 58 / figure of 58. Just 'outlier' on its own without reference to either 58 or large scores E0 Accept the large outlier affects the mean (more) E1	E1 cao E1indep	2
(iv)	There are $14.75 \times 28 = 413$ messages So total cost = 413×10 pence = £41.30	M1 for 14.75×28 but 413 can also imply the mark A1cao	2
		TOTAL	7
Q2 (i)	$\binom{4}{3} \times 3! = 4 \times 6 = 24$ codes or ${}^4P_3 = 24$ (M2 for 4P_3) Or $4 \times 3 \times 2 = 24$	M1 for 4 M1 for $\times 6$ A1	3
(ii)	$4^3 = 64$ codes	M1 for 4^3 A1 cao	2
		TOTAL	5
Q3 (i)	Probability = $0.3 \times 0.8 = 0.24$	M1 for 0.8 from (1-0.2) A1	2
(ii)	Either: $P(A \cup B) = P(A) + P(B) - P(A \cap B)$ $= 0.3 + 0.2 - 0.3 \times 0.2$ $= 0.5 - 0.06 = 0.44$ Or: $P(A \cup B) = 0.7 \times 0.2 + 0.3 \times 0.8 + 0.3 \times 0.2$ $= 0.14 + 0.24 + 0.06 = 0.44$ Or: $P(A \cup B) = 1 - P(A' \cap B')$ $= 1 - 0.7 \times 0.8 = 1 - 0.56 = 0.44$	M1 for adding 0.3 and 0.2 M1 for subtraction of (0.3 \times 0.2) A1 cao M1 either of first terms M1 for last term A1 M1 for 0.7 \times 0.8 or 0.56 M1 for complete method as seen A1	3
(iii)	$P(A B) = \frac{P(A \cap B)}{P(B)} = \frac{0.06}{0.44} = \frac{6}{44} = 0.136$	M1 for numerator of their 0.06 only M1 for 'their 0.44' in denominator A1 FT (must be valid p)	3
		TOTAL	8

Q4 (i)	$E(X) = 1 \times 0.2 + 2 \times 0.16 + 3 \times 0.128 + 4 \times 0.512 = 2.952$ Division by 4 or other spurious value at end loses A mark $E(X^2) = 1 \times 0.2 + 4 \times 0.16 + 9 \times 0.128 + 16 \times 0.512 = 10.184$ $\text{Var}(X) = 10.184 - 2.952^2 = 1.47$ (to 3 s.f.)	M1 for $\sum rp$ (at least 3 terms correct) A1 cao M1 for $\sum x^2p$ at least 3 terms correct M1 for $E(X^2) - E(X)^2$ Provided ans > 0 A1 FT their $E(X)$ but not a wrong $E(X^2)$	5
(ii)	Expected cost = $2.952 \times \text{£}45000 = \text{£}133000$ (3sf)	B1 FT (no extra multiples / divisors introduced at this stage)	1
(iii)		G1 labelled linear scales G1 height of lines	2
		TOTAL	8
Q5 (i)	Impossible because the competition would have finished as soon as Sophie had won the first 2 matches	E1	1
(ii)	SS, JSS, JSJSS	B1, B1, B1 (-1 each error or omission)	3
(iii)	$0.7^2 + 0.3 \times 0.7^2 + 0.7 \times 0.3 \times 0.7^2 = 0.7399$ or $0.74(0)$ $\{ 0.49 + 0.147 + 0.1029 = 0.7399 \}$	M1 for any correct term M1 for any other correct term M1 for sum of all three correct terms A1 cao	4
		TOTAL	8

Section B																			
Q6																			
(i)	$\text{Mean} = \frac{180.6}{12} = 15.05 \text{ or } 15.1$ $S_{xx} = 3107.56 - \frac{180.6^2}{12} \text{ or } 3107.56 - 12(\text{their } 15.05)^2 = (389.53)$ $s = \sqrt{\frac{389.53}{11}} = 5.95 \text{ or better}$ NB Accept answers seen without working (from calculator)	B1 for mean M1 for attempt at S_{xx} A1 cao	3																
(ii)	$\bar{x} + 2s = 15.05 + 2 \times 5.95 = 26.95$ $\bar{x} - 2s = 15.05 - 2 \times 5.95 = 3.15$ So no outliers	M1 for attempt at either M1 for both A1 for limits and conclusion FT their mean and sd	3																
(iii)	New mean = $1.8 \times 15.05 + 32 = 59.1$ New s = $1.8 \times 5.95 = 10.7$	B1FT M1 A1FT	3																
(iv)	New York has a higher mean or 'is on average' higher (oe) New York has greater spread /range /variation or SD (oe)	E1FT using $^{\circ}F$ (\bar{x} dep) E1FT using $^{\circ}F$ (σ dep)	2																
(v)	<table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td style="padding: 2px;">Upper bound</td> <td style="padding: 2px;">(70)</td> <td style="padding: 2px;">100</td> <td style="padding: 2px;">110</td> <td style="padding: 2px;">120</td> <td style="padding: 2px;">150</td> <td style="padding: 2px;">170</td> <td style="padding: 2px;">190</td> </tr> <tr> <td style="padding: 2px;">Cumulative frequency</td> <td style="padding: 2px;">(0)</td> <td style="padding: 2px;">6</td> <td style="padding: 2px;">14</td> <td style="padding: 2px;">24</td> <td style="padding: 2px;">35</td> <td style="padding: 2px;">45</td> <td style="padding: 2px;">48</td> </tr> </table> 	Upper bound	(70)	100	110	120	150	170	190	Cumulative frequency	(0)	6	14	24	35	45	48	B1 for all correct cumulative frequencies (may be implied from graph). <u>Ignore cf of 0 at this stage</u> G1 for linear scales (linear from 70 to 190) ignore $x < 70$ vertical: 0 to 50 but not beyond 100 (no inequality scales) G1 for labels G1 for points plotted as (UCB, their cf). <u>Ignore (70,0)</u> at this stage. No mid – point or LCB plots.	5
Upper bound	(70)	100	110	120	150	170	190												
Cumulative frequency	(0)	6	14	24	35	45	48												
(vi)	NB all G marks dep on attempt at cumulative frequencies. NB All G marks dep on attempt at cumulative frequencies Line on graph at cf = 43.2(soi) or used 90th percentile = 166	G1 for joining all of 'their points'(line or smooth curve) AND now including (70,0) M1 for use of 43.2 A1FT but dep on 3rd G mark earned	2																
		TOTAL	18																

<p>Q7 (i)</p>	<p>$X \sim B(12, 0.05)$</p> <p>(A) $P(X = 1) = \binom{12}{1} \times 0.05 \times 0.95^{11} = 0.3413$</p> <p>OR from tables $0.8816 - 0.5404 = 0.3412$</p> <p>(B) $P(X \geq 2) = 1 - 0.8816 = 0.1184$</p> <p>(C) Expected number $E(X) = np = 12 \times 0.05 = 0.6$</p>	<p>M1 0.05×0.95^{11}</p> <p>M1 $\binom{12}{1} \times pq^{11} (p+q) = 1$</p> <p>A1 cao</p> <p>OR: M1 for 0.8816 seen and M1 for subtraction of 0.5404</p> <p>A1 cao</p> <p>M1 for $1 - P(X \leq 1)$</p> <p>A1 cao</p> <p>M1 for 12×0.05</p> <p>A1 cao (= 0.6 seen)</p>	<p>3</p> <p>2</p> <p>2</p>
<p>(ii)</p> <p>(iii)</p>	<p><i>Either:</i> $1 - 0.95^n \leq \frac{1}{3}$ $0.95^n \geq \frac{2}{3}$ $n \leq \log \frac{2}{3} / \log 0.95$, so $n \leq 7.90$ Maximum $n = 7$</p> <p><i>Or:</i> (using tables with $p = 0.05$): $n = 7$ leads to $P(X \geq 1) = 1 - P(X = 0) = 1 - 0.6983 = 0.3017 (< \frac{1}{3})$ or $0.6983 (> \frac{2}{3})$ $n = 8$ leads to $P(X \geq 1) = 1 - P(X = 0) = 1 - 0.6634 = 0.3366 (> \frac{1}{3})$ or $0.6634 (< \frac{2}{3})$ Maximum $n = 7$ (total accuracy needed for tables)</p> <p><i>Or:</i> (using trial and improvement): $1 - 0.95^7 = 0.3017 (< \frac{1}{3})$ or $0.95^7 = 0.6983 (> \frac{2}{3})$ $1 - 0.95^8 = 0.3366 (> \frac{1}{3})$ or $0.95^8 = 0.6634 (< \frac{2}{3})$ Maximum $n = 7$ (3 sf accuracy for calculations)</p> <p>NOTE: $n = 7$ unsupported scores SC1 only</p> <p>Let $X \sim B(60, p)$ Let $p =$ probability of a bag being faulty $H_0: p = 0.05$ $H_1: p < 0.05$</p> <p>$P(X \leq 1) = 0.95^{60} + 60 \times 0.05 \times 0.95^{59} = 0.1916 > 10\%$</p> <p>So not enough evidence to reject H_0</p> <p>Conclude that there is not enough evidence to indicate that the new process reduces the failure rate or scientist incorrect/wrong.</p>	<p>M1 for equation in n</p> <p>M1 for use of logs</p> <p>A1 cao</p> <p>M1 indep</p> <p>M1 indep</p> <p>A1 cao dep on both M's</p> <p>M1 indep (as above)</p> <p>M1 indep (as above)</p> <p>A1 cao dep on both M's</p> <p>B1 for definition of p</p> <p>B1 for H_0</p> <p>B1 for H_1</p> <p>M1 A1 for probability</p> <p>M1 for comparison</p> <p>A1</p> <p>E1</p>	<p>3</p> <p>8</p>
TOTAL			18