

1. A random sample of 35 homeowners was taken from each of the villages Greenslax and Penville and their ages were recorded. The results are summarised in the back-to-back stem and leaf diagram below.

| Totals | Greenslax | | | | | | Penville | | | | | Totals | | | | | | | |
|--------|-----------|---|---|---|---|---|----------|---|-----|-----|---|--------|-----|-----|-----|---|---|---|------|
| (2) | | | 8 | 7 | 2 | | 5 | 5 | 6 | 7 | 8 | 8 | 9 | (7) | | | | | |
| (3) | | | 9 | 8 | 7 | | 3 | 1 | 1 | 1 | 2 | 3 | 4 | 4 | 5 | 6 | 7 | 9 | (11) |
| (4) | | | 4 | 4 | 4 | 0 | | 4 | 0 | 1 | 2 | 4 | 7 | (5) | | | | | |
| (5) | | | 6 | 6 | 5 | 2 | 2 | | 5 | 0 | 0 | 5 | 5 | 5 | (5) | | | | |
| (7) | 8 | 6 | 5 | 4 | 2 | 1 | 1 | | 6 | 2 | 5 | 6 | 6 | (4) | | | | | |
| (8) | 8 | 6 | 6 | 6 | 4 | 3 | 1 | 1 | | 7 | 0 | 5 | (2) | | | | | | |
| (5) | | | 9 | 8 | 4 | 3 | 2 | | 8 | (0) | | | | | | | | | |
| (1) | | | | | 4 | 9 | | 9 | (1) | | | | | | | | | | |

Key: 7 | 3 | 1 means 37 years for Greenslax and 31 years for Penville

Some of the quartiles for these two distributions are given in the table below.

| | Greenslax | Penville |
|-----------------------|-----------|----------|
| Lower quartile, Q_1 | a | 31 |
| Median, Q_2 | 64 | 39 |
| Upper quartile, Q_3 | b | 55 |

- (a) Find the value of a and the value of b . (2)

An outlier is a value that falls either

more than $1.5 \times (Q_3 - Q_1)$ above Q_3

or more than $1.5 \times (Q_3 - Q_1)$ below Q_1

- (b) On the graph paper opposite draw a box plot to represent the data from Penville. Show clearly any outliers. (4)

- (c) State the skewness of each distribution. Justify your answers. (3)



2. The mark, x , scored by each student who sat a statistics examination is coded using

$$y = 1.4x - 20$$

The coded marks have mean 60.8 and standard deviation 6.60

Find the mean and the standard deviation of x .

(4)

Q2

(Total 4 marks)



6. The times, in seconds, spent in a queue at a supermarket by 85 randomly selected customers, are summarised in the table below.

| Time (seconds) | Number of customers, f |
|----------------|--------------------------|
| 0 – 30 | 2 |
| 30 – 60 | 10 |
| 60 – 70 | 17 |
| 70 – 80 | 25 |
| 80 – 100 | 25 |
| 100 – 150 | 6 |

A histogram was drawn to represent these data. The 30 – 60 group was represented by a bar of width 1.5 cm and height 1 cm.

- (a) Find the width and the height of the 70 – 80 group. (3)
- (b) Use linear interpolation to estimate the median of this distribution. (2)

Given that x denotes the midpoint of each group in the table and

$$\sum fx = 6460 \quad \sum fx^2 = 529\,400$$

- (c) calculate an estimate for
- (i) the mean,
- (ii) the standard deviation,
- for the above data. (3)

One measure of skewness is given by

$$\text{coefficient of skewness} = \frac{3(\text{mean} - \text{median})}{\text{standard deviation}}$$

- (d) Evaluate this coefficient and comment on the skewness of these data. (3)



