

# Mark Scheme (Results)

## January 2007

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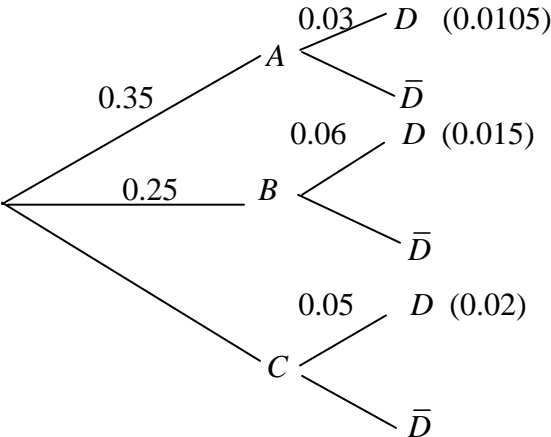
GCE

GCE Mathematics

Statistics (6683)

**January 2007  
6683 Statistics S1  
Mark Scheme**

Question number	Scheme	Marks
1. (a)	(£) 17	Just <b>17</b>
(b)	$\sum t = 212$ and $\sum m = 61$ (Accept as totals under each column in qu.)	B1, B1
	$S_m = 2485 - \frac{61 \times 212}{10}, = 1191.8$	awrt <b>1190</b> or 119 (3sf)
	$S_n = 983.6$ (awrt <b>984</b> ) and $S_{mm} = 1728.9$ (awrt <b>1730</b> )	(or 98.4 and 173)
(c)	$r = \frac{1191.8}{\sqrt{983.6 \times 1728.9}}$ $= 0.913922\dots$	M1, A1 A1, A1 (6) M1, A1f.t. awrt <b>0.914</b>
(d)	0.914 (Must be the same as (c) or awrt 0.914)	B1f.t. ( $ r  < 1$ )
	e.g. linear transformation, coding does not affect coefficient (or recalculate)	dB1 (2)
(e)	0.914 suggests longer spent shopping the more spent. (Idea more time, more spent)	B1
	0.178 different amounts spent for same time.	B1 (2)
(f)	e.g. might spend short time buying 1 expensive item <u>OR</u> might spend a long time checking for bargains, talking, buying lots of cheap items.	B1g (1)
<b>15 marks</b>		
(b)	M1 for one correct formula seen, f.t. their $\sum t, \sum m$ [Use 1 <sup>st</sup> A1 for 1 correct, 2 <sup>nd</sup> A1 for 2 etc]	
(c)	M1 for attempt at correct formula, $\frac{2485}{\sqrt{2101 \times 5478}}$ scores M1A0A0 A1ft f.t. their values for $S_n$ etc from (b) but don't give for $S_n = 5478$ etc (see above) Answer only (awrt 0.914) scores 3/3, 0.913 (i.e. truncation) can score M1A1ft by implication.	
(d)	2 <sup>nd</sup> B1 dependent on 1 <sup>st</sup> B1 Accept $\sum m = 261, \sum m^2 = 8541, \sum tm = 6725 \rightarrow 0.914$	
(e)	One mark for a sensible comment relating to each coefficient For 0.178 allow "little or no link between time and amount spent". Must be in context. Just saying 0.914 is strong +ve correlation between amount spent and time shopping and 0.178 is weak correlation ...scores B0B0.	
(f)	B1g for a sensible, practical suggestion showing that other factors might affect the amount spent. E.g. different day (weekend vs weekday) or time of day (time spent queuing if busy)	

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2. (a)	 <p style="text-align: right;">Correct tree shape</p> <p><math>A, B</math> and <math>C</math> and 0.35 and 0.25</p> <p><math>D</math> (x3) and 0.03, 0.06, 0.05 (May be implied by seeing <math>P(A \cap D)</math> etc at the ends)</p>	<p>M1</p> <p>A1</p> <p>A1 (3)</p>
(b)(i)	$P(A \cap D) = 0.35 \times 0.03, = \underline{\mathbf{0.0105}}$ or $\frac{21}{2000}$	<p>M1, A1</p>
	<p><math>P(C) = 0.4</math> (anywhere)</p>	<p>B1</p>
(ii)	$P(D) = (i) + 0.25 \times 0.06 + (0.4 \times 0.05)$ $= \underline{\mathbf{0.0455}}$ or $\frac{91}{2000}$	<p>M1</p> <p>A1 (5)</p>
(c)	$P(C D) = \frac{P(C \cap D)}{P(D)}, = \frac{0.4 \times 0.05}{(ii)}$ $= 0.43956... \text{ or } \frac{40}{91}$	<p>M1, A1ft</p> <p><math>\underline{\mathbf{0.44}}</math> or awrt <math>\underline{\mathbf{0.440}}</math> A1 (3)</p>
[Correct answers only score full marks in each part]		<b>11 marks</b>
(a)	<p>M1 for tree diagram, 3 branches and then two from each. At least one probability attempted.</p>	
(b)	<p>1<sup>st</sup> M1 for <math>0.35 \times 0.03</math>. Allow for equivalent from <u>their</u> tree diagram.</p> <p>B1 for <math>P(C) = 0.4</math>, can be in correct place on tree diagram or implied by <math>0.4 \times 0.05</math> in <math>P(D)</math>.</p> <p>2<sup>nd</sup> M1 for all 3 cases attempted and <u>some</u> correct probabilities seen, including +. Can ft their tree. Condone poor use of notation if correct calculations seen. E.g. <math>P(C D)</math> for <math>P(C \cap D)</math>.</p>	
(c)	<p>M1 for attempting correct ratio of probabilities. There must be an attempt to substitute some values in a correct formula. If no correct formula and ration not correct ft score M0. Writing <math>P(D C)</math> and attempting to find this is M0. Writing <math>P(D C)</math> but calculating correct ratio – ignore notation and mark ratios.</p> <p>A1ft must have their <math>0.4 \times 0.05</math> divided by their (ii). If ratio is incorrect ft (0/3) unless correct formula seen and part of ratio is correct then M1.</p>	

Question number	Scheme	Marks														
3. (a)	<p>N.B. Part (a) doesn't have to be in a table, could be a list <math>P(X = 1) = \dots</math>etc</p> <table border="1" data-bbox="293 349 968 510"> <tr> <td><math>x</math></td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> <tr> <td><math>P(X = x)</math></td> <td><math>\frac{1}{36}</math></td> <td><math>\frac{3}{36}</math></td> <td><math>\frac{5}{36}</math></td> <td><math>\frac{7}{36}</math></td> <td><math>\frac{9}{36}</math></td> <td><math>\frac{11}{36}</math></td> </tr> </table> <p>0.0278, 0.0833, 0.139, 0.194, 0.25, 0.306 (Accept awrt 3 s.f)</p> <p>(b) <math>P(3) + P(4) + P(5) = \frac{21}{36}</math> or <math>\frac{7}{12}</math> or awrt 0.583</p> <p>(c) <math>E(X) = \frac{1}{36} + 2 \times \frac{3}{36} + \dots = \frac{161}{36}</math> or 4.472 or <math>4\frac{17}{36}</math></p> <p>(d) <math>E(X^2) = \frac{1}{36} + 2^2 \times \frac{3}{36} + \dots = \frac{791}{36}</math> or full expression or <math>21\frac{35}{36}</math> or awrt 21.97</p> <p><math>\text{Var}(X) = \frac{791}{36} - \left(\frac{161}{36}\right)^2</math>, = <b><u>1.9714...</u></b> *</p> <p>(e) <math>\text{Var}(2 - 3X) = 9 \times 1.97</math> or <math>(-3)^2 \times 1.97</math>, = 17.73 awrt <b><u>17.7</u></b> or <math>\frac{2555}{144}</math></p>	$x$	1	2	3	4	5	6	$P(X = x)$	$\frac{1}{36}$	$\frac{3}{36}$	$\frac{5}{36}$	$\frac{7}{36}$	$\frac{9}{36}$	$\frac{11}{36}$	<p>B1, B1, B1 (3)</p> <p>M1, A1 (2)</p> <p>M1, A1 (2)</p> <p>M1, A1 (4)</p> <p>M1, A1c.s.o. (4)</p> <p>M1, A1 (2)</p> <p><b>13 marks</b></p>
$x$	1	2	3	4	5	6										
$P(X = x)$	$\frac{1}{36}$	$\frac{3}{36}$	$\frac{5}{36}$	$\frac{7}{36}$	$\frac{9}{36}$	$\frac{11}{36}$										
	<p>(a) 1<sup>st</sup> B1 for <math>x = 1, \dots, 6</math> and at least one correct probability N.B. <math>\frac{3}{36} = \frac{1}{12}</math> and <math>\frac{9}{36} = \frac{1}{4}</math>                  2<sup>nd</sup> B1 for at least 3 correct probabilities                  3<sup>rd</sup> B1 for a fully correct probability distribution.</p> <p>(b) M1 for attempt to add the correct three probabilities, ft their probability distribution</p> <p>(c) M1 for a correct attempt at <math>E(X)</math>. Minimum is as printed. Exact answer only scores M1A1.                  [Division by 6 at any point scores M0, no ISW. Non-exact answers with no working score M0.]</p> <p>(d) 1<sup>st</sup> M1 for a correct attempt at <math>E(X^2)</math>. Minimum as printed. <math>\frac{791}{36}</math> or awrt 21.97 scores M1A1.                  2<sup>nd</sup> M1 for their <math>E(X^2) - (\text{their } E(X))^2</math>.                  2<sup>nd</sup> A1 cso needs awrt 1.97 <u>and</u> <math>\frac{791}{36} - \left(\frac{161}{36}\right)^2</math> or <math>\frac{2555}{1296}</math> or any fully correct expression seen.                  Can accept <u>at least 4 sf</u> for both. i.e. 21.97 for <math>\frac{791}{36}</math>, 4.472 for <math>\frac{161}{36}</math>, 20.00 for <math>\left(\frac{161}{36}\right)^2</math>.</p> <p>(e) M1 for correct use of <math>\text{Var}(aX + b)</math> formula or a <u>full</u> method.                  NB <math>-3^2 \times 1.97</math> followed by awrt 17.7 scores M1A1 <u>BUT</u> <math>-3^2 \times 1.97</math> alone, or followed by <math>-17.7</math>, scores M0A0.</p>															

Question number	Scheme	Marks
4. (a)	Positive skew (both bits)	B1 (1)
(b)	$19.5 + \frac{(60-29)}{43} \times 10, = 26.7093\dots$ (N.B. Use of 60.5 gives 26.825... so allow awrt 26.8)	awrt <b>26.7</b> M1, A1 (2)
(c)	$\mu = \frac{3550}{120} = 29.5833\dots$ or $29\frac{7}{12}$ $\sigma^2 = \frac{138020}{120} - \mu^2$ or $\sigma = \sqrt{\frac{138020}{120} - \mu^2}$ $\sigma = 16.5829\dots$ or ( $s = 16.652\dots$ )	awrt <b>29.6</b> B1 M1 awrt <b>16.6</b> (or $s = 16.7$ ) A1 (3)
(d)	$\frac{3(29.6 - 26.7)}{16.6}$ $= 0.52\dots$ (N.B. 60.5 in (b) ...awrt 0.499[or with $s$ awrt 0.497])	M1A1ft awrt <b>0.520</b> (or with $s$ awrt 0.518) A1 (3)
(e)	0.520 > 0 So it is consistent with (a)	correct statement about their (d) being >0 or < 0 ft their (d) B1ft dB1ft (2)
(f)	Use <u>Median</u> Since the data is skewed <u>or</u> less affected by outliers/extreme values	B1 dB1 (2)
(g)	If the data are <u>symmetrical</u> or <u>skewness is zero</u> or <u>normal/uniform distribution</u> ("mean =median" or "no outliers" or "evenly distributed" all score B0)	B1 (1) <b>14 marks</b>
(b)	M1 for $(19.5 \text{ or } 20) + \frac{(60-29)}{43} \times 10$ or better. Allow 60.5 giving awrt 26.8 for M1A1 Allow their $0.5n$ [or $0.5(n+1)$ ] instead of 60 [or 60.5] for M1.	
(c)	M1 for a correct expression for $\sigma, \sigma^2, s$ or $s^2$ . NB $\sigma^2 = 274.99$ and $s^2 = 277.30$ Condone poor notation if answer is awrt 16.6 (or 16.7 for $s$ )	
(d)	M1 for attempt to use this formula using their values to any accuracy. Condone missing 3. 1 <sup>st</sup> A1ft for using their values to at least 3sf. Must have the 3. 2 <sup>nd</sup> A1 for using accurate enough values to get awrt 0.520 (or 0.518 if using $s$ ) NB Using only 3 sf gives 0.524 and scores M1A1A0	
(e)	1 <sup>st</sup> B1 for saying or implying correct sign for their (d). B1g and B1ft. Ignore "correlation" if seen. 2 <sup>nd</sup> B1 for a comment about consistency with their (d) and (a) being positive skew, ft their (d) only This is dependent on 1 <sup>st</sup> B1: so if (d)>0, they say yes, if (d)<0 they say no.	
(f)	2 <sup>nd</sup> B1 is dependent upon choosing median.	

Question number	Scheme	Marks
5. (a)	Time is a <u>continuous</u> variable <u>or</u> data is in a <u>grouped</u> frequency table	B1 (1)
(b)	Area is proportional to frequency <u>or</u> $A \propto f$ <u>or</u> $A = kf$	B1 (1)
(c)	$3.6 \times 2 = 0.8 \times 9$ <p>1 child represented by 0.8</p>	M1 dM1 A1 cso (3)
(d)	$(\text{Total}) = \frac{24}{0.8}, = \underline{\underline{30}}$	M1, A1 (2)
<b>7 marks</b>		
(b)	<p>1<sup>st</sup> B1 for one of these correct statements.                      “Area proportional to frequency density” or “Area = frequency” is B0</p>	
(c)	<p>1<sup>st</sup> M1 for a correct combination of any 2 of the 4 numbers: 3.6, 2, 0.8 and 9                      e.g. <math>3.6 \times 2</math> or <math>\frac{3.6}{0.8}</math> or <math>\frac{0.8}{2}</math> etc BUT e.g. <math>\frac{3.6}{2}</math> is M0                      2<sup>nd</sup> M1 dependent on 1<sup>st</sup> M1 and for a correct combination of 3 numbers leading to 4<sup>th</sup>.                      May be in separate stages but must see all 4 numbers                      A1cso for fully correct solution. Both Ms scored, no false working seen and <u>comment required</u>.</p>	
(d)	M1 for $\frac{24}{0.8}$ seen or implied.	

Question number	Scheme	Marks
6. (a)	Used to simplify <u>or</u> represent a real world problem Cheaper <u>or</u> quicker <u>or</u> easier (than the real situation) <u>or</u> more easily modified To improve understanding of the real world problem Used to predict outcomes from a real world problem (idea of predictions)	(any two lines) B1 B1 (2)
(b)	(3 or 4) Model used to make predictions. (Idea of predicted values based on the model)	B1
	(4 or 3) (Experimental) data collected	B1
	(7) Model is refined.	B1 (3)
		<b>5 marks</b>
(a)	1 <sup>st</sup> B1 For one line 2 <sup>nd</sup> B1 For a second line Be generous for 1 <sup>st</sup> B1 but stricter for B1B1	
(b)	1 <sup>st</sup> & 2 <sup>nd</sup> B1 These two points can be interchanged. Idea of values from (experimental) data and predicted values based on the model. 1 <sup>st</sup> B1 for predicted values from model e.g. “model used to gain suitable data” 2 <sup>nd</sup> B1 for data collected. Idea of experimental data but “experiment” needn’t be explicitly seen  3 <sup>rd</sup> B1 This should be stage 7. Idea of refinement or revision or adjustment	

Question number	Scheme	Marks
7. (a)	$P(X < 91) = P\left(Z < \frac{91-100}{15}\right)$ $= P(Z < -0.6)$ $= 1 - 0.7257$ $= 0.2743$	Attempt standardisation M1 A1 M1 awrt <b>0.274</b> A1 (4)
(b)	$1 - 0.2090 = 0.7910$ $P(X > 100+k) = 0.2090 \quad \text{or} \quad P(X < 100+k) = 0.7910 \quad (\text{May be implied})$ $\frac{100+k-100}{15} = 0.81 \quad (\text{ft their } z = 0.81, \text{ but must be } z \text{ not prob.})$ $\underline{k = 12}$	0.791 B1 M1 B1 M1, A1ft A1 cao (6) <b>10 marks</b>
(a)	$\pm \frac{(91-\mu)}{\sigma \text{ or } \sigma^2}$ 1 <sup>st</sup> M1 for attempting standardisation. Can use of 109 instead of 91. Use of 90.5 etc is M0 1 <sup>st</sup> A1 for -0.6 (or +0.6 if using 109) 2 <sup>nd</sup> M1 for 1 - probability from tables. Probability should be > 0.5	
(b)	1 <sup>st</sup> B1 for 0.791 seen or implied. 1 <sup>st</sup> M1 for a correct probability statement, but must use X or Z correctly. Shown on diagram is OK 2 <sup>nd</sup> B1 for awrt 0.81 seen (or implied by correct answer - see below) (Calculator gives 0.80989...) 2 <sup>nd</sup> M1 for attempting to standardise e.g. $\frac{100+k-100}{15}$ or $\frac{k}{15}$ $\frac{X-100}{15}$ scores 2 <sup>nd</sup> M0 until the 100+ k is substituted to give k, but may imply 1 <sup>st</sup> M1 if k= 112.15 seen 1 <sup>st</sup> A1ft for correct equation for k (as written or better). Can be implied by k = 12.15 (or better) 2 <sup>nd</sup> A1 for k = 12 only. <u>Answers only</u> k = 112 or 112.15 or better scores 3/6 (on EPEN give first 3 marks) k = 12.15 or better (calculator gives 12.148438...) scores 5/6 (i.e loses last A1 only) k = 12 (no incorrect working seen) scores 6/6 NB Using 0.7910 instead of 0.81 gives 11.865 which might be rounded to 12. This should score no more than B1M1B0M1A0A0.	