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SI Jan 07 - Solutions

1. a) 20-3 = 17

b)  $S_{tt} = \sum t^2 - \frac{(\sum t)^2}{n} = 5478 - \frac{(212)^2}{10} = \underline{983.6}$

$S_{mm} = \sum m^2 - \frac{(\sum m)^2}{n} = 2101 - \frac{(61)^2}{10} = \underline{1728.9}$

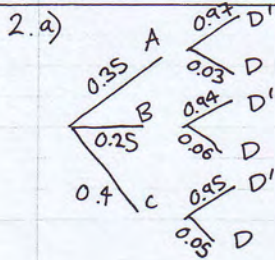
$S_{tm} = \sum tm - \frac{\sum t \sum m}{n} = 2485 - \frac{212 \times 61}{10} = \underline{1191.8}$

c)  $PMCC = r = \frac{S_{tm}}{\sqrt{S_{tt} S_{mm}}} = \frac{1191.8}{\sqrt{983.6 \times 1728.9}} = \underline{0.914}$  (3sf)

d) 0.914 coding does not effect the PMCC

- e) 0.914 implies the longer spent shopping the more money spent.
- 0.178 shows little or no correlation implying that the amount of time spent shopping had no bearing on the amount spent.

f) One could be measured during a sale.



b) i)  $P(A \cap D) = 0.35 \times 0.03 = \underline{0.0105}$

ii)  $P(D) = 0.0105 + 0.25 \times 0.06 + 0.4 \times 0.05 = \underline{0.0455}$

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c)  $P(C|D) = \frac{P(C \cap D)}{P(D)} = \frac{0.4 \times 0.05}{0.0455} = \underline{0.440}$  (3sf)

3. a)

X	1	2	3	4	5	6
P(X=x)	$\frac{1}{36}$	$\frac{2}{36}$	$\frac{5}{36}$	$\frac{7}{36}$	$\frac{9}{36}$	$\frac{10}{36}$

b)  $P(2 < X \leq 5) = P(X=3,4,5) = \frac{5+7+9}{36} = \underline{\frac{21}{36}}$

c)  $E(X) = \frac{1}{36} + \frac{6}{36} + \frac{15}{36} + \frac{28}{36} + \frac{45}{36} + \frac{66}{36} = \underline{\frac{161}{36}}$

d)  $Var(X) = E(X^2) - [E(X)]^2$

$E(X^2) = \frac{1}{36} + \frac{12}{36} + \frac{45}{36} + \frac{112}{36} + \frac{225}{36} + \frac{396}{36} = \underline{\frac{791}{36}}$

$\therefore Var(X) = \frac{791}{36} - \left(\frac{161}{36}\right)^2 = \underline{1.97}$  (3sf)

e)  $Var(2-3X) = (-3)^2 \times 1.97 = \underline{17.73}$

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4. a) Positive skew.

b)  $\frac{120}{2} = 60$  in 20-29 class

$Q_2 = 19.5 + \frac{(60-29) \times 10}{43} = \underline{26.7}$  (3sf)

c)  $\mu = \frac{\sum fx}{\sum f} = \frac{3550}{120} = \underline{29.6}$  (3sf)

$\sigma = \sqrt{\frac{\sum fx^2}{\sum f} - \mu^2} = \sqrt{\frac{138020}{120} - (29.6)^2} = \underline{16.6}$  (3sf)

d)  $\frac{3(29.6-26.7)}{16.6} = \underline{0.5}$

e) Yes as the coefficient is positive  $\Rightarrow$  positive skew.

f) median, as mean is effected by skew.

g) No skew.

5. a) continuous data.

b) Area represents frequency.

c) Area of Rectangle =  $3.6 \times 2 = 7.2 \text{ cm}^2$  Frequency = 9  
 $\therefore \frac{9}{7.2} = \underline{0.8 \text{ cm}^2}$

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d)  $\frac{24}{0.8} = 30$  pupils

- 6. a) Simplify complicated problems.
- Provide a quick and cheap solution.

b) Stage 3 Expected values are calculated  
Stage 4 Data is collected.

Stage 7 The model is revised and improved

7. a)  $IQ \sim N(100, 15^2)$

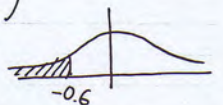
$P(IQ < 91) = P(Z < \frac{91-100}{15})$

$= P(Z < -0.6)$

$= P(Z > 0.6)$

$= 1 - P(Z < 0.6)$

$= 1 - \Phi(0.6) = 1 - 0.7257 = \underline{0.2743}$



b)  $P(IQ \geq 100+k) = 0.2090$

$P(Z > \frac{k}{15}) = 0.2090$

$P(Z < \frac{k}{15}) = 0.791$

$\Phi(\frac{k}{15}) = 0.791$

$\frac{k}{15} = 0.81 \quad k = 12.15$   
 $k = 12$

