

Version 1.0



**General Certificate of Education (A-level)
January 2012**

Mathematics

MS/SS1B

(Specification 6360)

Statistics 1B

Final

Mark Scheme

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

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Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
✓ or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
-x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MS/SS1B

Q	Solution	Marks	Total	Comments
1 (a)	Median = 10 Upper quartile = 11 Lower quartile = 9 Interquartile range = 2	B1 B1 B1	3	CAO CAO; either May be implied by IQR = 2 CAO; do not award if seen to be not based on 11 and 9
(b)	Do not group results Illustrations for B1: Use all values Replace ≤ 6 by or use (0), 1, ..., 6 Replace ≥ 12 by or use 12, 13, ... Record exact values/frequencies	B1	1	OE statement that implies non grouping or recording of all separate observed values Illustrations for B0: Record max and/or min values Construct frequency table Use 1, 2 or 12, 13
		Total	4	

Q	Solution	Marks	Total	Comments
2 (a)	Probably correct	B1	3	CAO; accept minimum of PC or Pc or pC or pc
(b)	Definitely incorrect	B1		CAO; accept minimum of DI or Di or dI or di
(c)	Probably incorrect	B1		CAO; accept minimum of PI or Pi or pI or pi
	Notes: Ignore reasoning in all parts, unless it includes 2 of the 4 statements in which case \Rightarrow B0 If answers not labelled, then assume above order			Definitely wrong, etc \Rightarrow B0 Likely correct, etc \Rightarrow B0
		Total	3	

MS/SS1B (cont)

Q	Solution	Marks	Total	Comments
3(a) (i)	<p>Volume, $X \sim N(32, 10^2)$</p> $P(X < 40) = P\left(Z < \frac{40-32}{10}\right)$ $= P(Z < 0.8)$ $= 0.788$	M1 A1 A1	3	<p>Standardising 40 with 32 and 10; allow (32 – 40)</p> <p>CAO; ignore inequality and sign May be implied by a correct answer</p> <p>AWRT (0.78814)</p>
(ii)	$P(X > 25) = P(Z > -0.7)$ $= P(Z < +0.7)$ $= 0.758$	M1 A1	2	<p>Area change May be implied by a correct answer or an answer > 0.5</p> <p>AWRT (0.75804)</p>
(iii)	$P(25 < X < 40) = \quad (i) - (1 - (ii))$ $= 0.78814 - (1 - 0.75804) = 0.546$ <p>Note: If (ii) is 0.242, then $(0.788 - 0.242) = 0.546 \Rightarrow$ M0 A0</p>	M1 A1	2	<p>OE; allow new start ignoring (i) & (ii) Allow even if incorrect standardising providing $0 < \text{answer} < 1$ May be implied by a correct answer</p> <p>AWRT (0.54618)</p>
(b)	$P(B > \text{£}65) =$ $P\left(Z > \frac{48.5-32}{10}\right)$ <p>or</p> $P\left(Z > \frac{65-42.88}{13.4}\right)$ $= P(Z > 1.65) = 1 - P(Z < 1.65)$ $= 1 - 0.95053 = 0.049 \text{ to } 0.05(0)$	M1 m1 A1	3	<p>Attempt to change from B to X using (48 to 49), 32 and 10 or Attempt to work with distribution of B using 65, (42.8 to 42.9) and 13.4</p> <p>Area change May be implied by a correct answer or an answer < 0.5</p> <p>AWFW (0.04947)</p>
(c)	<p>Other fuels Other vehicles with an example (not other cars) Other types of customer Minimum purchase (policy) Purchases in integer/fixed £s Customers filling fuel cans</p>	B2,1	2	<p>Size of car/engine/fuel tank \Rightarrow B0 Price of fuel \Rightarrow B0 Customer paying capacity \Rightarrow B0 Must be two clearly different valid reasons for award of B2 Drivers and vehicles related \Rightarrow B1 eg lorry drivers & lorries</p>
		Total	12	

MS/SS1B (cont)

Q	Solution	Marks	Total	Comments
4(a)	$U \sim B(40, 0.15)$	M1		Used somewhere in (a)
(i)	$P(U = 6) = 0.6067 - 0.4325$ or $= \binom{40}{6} (0.15)^6 (0.85)^{34}$ $= 0.174$	M1 A1	3	Accept 3 dp rounding or truncation Can be implied by a correct answer AWRT (0.1742)
(ii)	$P(U \leq 5) = 0.432$ to 0.433	B1	1	AWFW (0.4325)
(iii)	See supplementary sheet for individual probabilities			
	$P(5 < U < 10) = 0.9328$ or 0.9701 (p_1) MINUS 0.4325 or 0.2633 (p_2) $= 0.5(00)$ to 0.501	M1 M1 A1	3	Accept 3 dp rounding or truncation but allow 0.97 $p_2 - p_1 \Rightarrow$ M0 M0 A0 $(1 - p_2) - p_1 \Rightarrow$ M0 M0 A0 $p_1 - (1 - p_2) \Rightarrow$ M1 M0 A0 $(1 - p_2) - (1 - p_1) \Rightarrow$ M1 M1 (A1) only providing result > 0 Accept 3 dp rounding or truncation AWFW (0.5003)
(b)	Mean or $\mu = 32 \times 0.15 = 4.8$ (V or $\sigma^2 \Rightarrow$) $\frac{32 \times 0.15 \times 0.85}{}$ or (SD or $\sigma \Rightarrow$) $\sqrt{32 \times 0.15 \times 0.85}$ (SD or $\sigma) = 2.02$	B1 M1 A1	3	CAO Either numerical expression; ignore terminology May be implied by 4.08 CAO seen or 2.02 AWRT seen AWRT (2.0199) Do not award if labelled V or σ^2
(c)	Mean = 7.7 SD = 1.26 to 1.34 (Sample) mean is bigger / greater / different or $7.7/32 = 0.24 > 0.15$ and (Sample) SD is smaller / less / different So model appears unsuitable	B1 B1 Bdep1 Bdep1	4	CAO ($\sum x = 77$) AWFW ($\sum x^2 = 609$) Both; dependent on all previous 5 marks of B1 M1 A1 B1 B1 Can be scored for incorrect (b) re-done correctly in (c) Means & SDs different \Rightarrow Bdep0 OE; dependent on Bdep1
		Total	14	

MS/SS1B (cont)

Q	Solution	Marks	Total	Comments
5	See supplementary sheet for alternative solutions and additional guidelines to parts (b), (d) and (e)			
	(a) Calorific value depends upon moisture content Moisture (content) is set/are fixed values	B1	1	Must be in context; not "it", etc Use of x and $y \Rightarrow$ B0
(b)	b (gradient) = -0.076 b (gradient) = -0.07 to -0.08 a (intercept) = 5.35 to 5.36 a (intercept) = 5.1 to 5.6 Thus $y = (5.35 \text{ to } 5.36) - 0.076x$	B2 (B1) B2 (B1) BF1	5	AWRT; including $-ve$ sign (-0.07582) AWFW; including $-ve$ sign <i>Treat rounding of correct answers as ISW</i> AWFW (5.35385) AWFW F on a and b even if rounded
(c)	a : calorific value of wood with zero/no moisture or dry maximum calorific value b : each 1(%) rise in moisture content reduces calorific value by 0.076 MWh/tonne As x increases y decreases	B1 B2 (B1)	3	OE; $a \leq 0 \Rightarrow$ B0 In context and with values; F on b $b \geq 0 \Rightarrow$ B0 Negative relationship/correlation
(d)	$y_{27} = 3.28$ to 3.32 $= 2.5$ to 3.5	B2 (B1)	2	AWFW (3.30659) AWFW; even if by interpolation from original data giving likely values of 3 or 3.04
(e)	$r(35, 2.5) = -0.21$ to -0.19 $= 0.1$ to 0.3	B2 (B1)	2	AWFW; including $-ve$ sign (-0.20000) AWFW; ignore sign
(f)	Good/reasonable/accurate/correct/etc Accept more positive qualifying adjectives	B1	1	OE; ignore reasoning Very good (B1) Not good (B0)
(g)(i)	Extrapolation/outside (observed) range (of x)	B1	1	OE
(ii)	$y_{80} = -0.5$ to -1 Negative value for calorific value is impossible or More energy needed than is generated	B1 Bdep1	2	AWFW (-0.71209) OE; dependent on B1 Must be in context; negative value impossible \Rightarrow Bdep0
		Total	17	

MS/SS1B (cont)

Q	Solution	Marks	Total	Comments															
6	See supplementary sheet for alternative solutions to parts (a)(i) and (b)(ii)																		
	<p>(a)(i) Table Method (2- way with either R or C totals)</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th></th> <th>A</th> <th>A'</th> <th>Total</th> </tr> </thead> <tbody> <tr> <th>E</th> <td>0.55</td> <td>0.05</td> <td>0.60</td> </tr> <tr> <th>E'</th> <td>0.30</td> <td>0.10</td> <td>0.40</td> </tr> <tr> <th>Total</th> <td>0.85</td> <td>0.15</td> <td>1.00</td> </tr> </tbody> </table>		A	A'	Total	E	0.55	0.05	0.60	E'	0.30	0.10	0.40	Total	0.85	0.15	1.00	B1 B1 Bdep1	3
	A	A'	Total																
E	0.55	0.05	0.60																
E'	0.30	0.10	0.40																
Total	0.85	0.15	1.00																
(ii)	$P(\geq 1) = 0.9$ or $9/10$	B1	1	CAO															
(iii)	$P(1) = 0.3 + 0.05 = 1 - (0.55 + 0.10)$ $= 0.35$ or $35/100$ or $7/20$	B1	1	CAO															
(b)(i)	$P(3) = 0.55 \times 0.30$ $= 0.165$ or $165/1000$ or $33/200$	B1		OE; implied by correct answer															
		B1	2	CAO															
(ii)	$0.55 \times (1 - 0.3)$ or 0.385 or (0.3×0.75) or 0.225 or (0.05×0.75) or 0.0375 or (0.35×0.75) or 0.2625 $(0.385 + 0.2625) + 0.165$ $= 0.812$ to 0.813 or $\frac{8125}{10000}$ or $\frac{1625}{2000}$ or $\frac{325}{400}$ or $\frac{65}{80}$ or $\frac{13}{16}$	M1																	
		M1		At least one of these expressions or values															
		B1		OE; implied by correct answer															
		A1	4	AWFW (0.8125) CAO															
		Total	11																

MS/SS1B (cont)

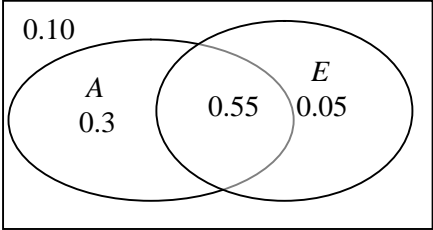
Q	Solution	Marks	Total	Comments
7(a) (i)	$\bar{x} = \frac{2290}{50} = 45.8 \text{ or } 45800$ $(s^2 =) \frac{28225.5}{49 \text{ or } 50} \quad \text{or} \quad (s =) \sqrt{\frac{28225.5}{49 \text{ or } 50}}$ $s = 24(.0) \text{ or } 24000 \text{ to } 24001$ SCs: (for no seen working) M1 A1 for 24.0 or 24000 to 24001 M1 A0 for 24 or 23700 to 23800	B1 M1 A1	3	CAO Ignore notation AWRT/AFWW (24.00064) ($\sigma = 23.75942$)
(ii)	See supplementary sheet for alternative solutions $\bar{x} - ns = (45.8 - n \times 24.0) < 0$ SC: Accept quoted values of (-4 to -1) ($n = 2$) or (-28.5 to -23.5) ($n = 3$) (both AFWW) and negative salaries are impossible	M1 A1	2	Allow (45 to 47) and any multiple of (23.5 to 24.5) which gives value < 0 Must clearly state the value of a numerical expression OE; must be in context Negative values impossible \Rightarrow A0
(b)(i)	Large sample or $n > 25$ or 30 or $n = 50$ so CLT applies	B1 Bdep1	2	OE Must indicate CLT; dependent on B1 Indication that other than sample mean is normally distributed \Rightarrow Bdep0
(ii)	$99\% (0.99) \Rightarrow z = 2.57 \text{ to } 2.58$ CI for μ is $\bar{x} \pm z \times \frac{s}{\sqrt{n}}$ Thus $45.8 \pm 2.5758 \times \frac{24.0}{\sqrt{50}}$ Hence $45.8 \pm (8.7 \text{ to } 8.8)$ or $45800 \pm (8700 \text{ to } 8800)$ OR $(37(.0) \text{ to } 37.1, 54.5 \text{ to } 54.6)$ or $(37000 \text{ to } 37100, 54500 \text{ to } 54600)$	B1 M1 AF1 A1	4	AFWW (2.5758) Used with (\bar{x} & s) from (a)(i) and $z(1.64 \text{ to } 2.58)$ & $\div \sqrt{n}$ with $n > 1$ F on (\bar{x} & s) with $\div \sqrt{50}$ or 49 & $z(1.64 \text{ to } 1.65 \text{ or } 2.32 \text{ to } 2.33 \text{ or } 2.57 \text{ to } 2.58)$ CAO/AFWW (8.74) Ignore (absence of) quoted units AFWW
(c)	See supplementary sheet for additional illustrations Clear correct comparison of 55 or 55000 with c's UCL or CI $(6/50 \text{ or } 0.12 \text{ or } 12\%) < / \neq 0.25 \text{ or } 25\%$ Reject both/each of the two claims	B1 B1 Bdep1	3	Accept 55000 compared with c's 54.5 to 54.6 (ie different units) OE; correct comparison mentioning both 12% and 25% Dependent on B1 B1
		Total	14	

MS/SS1B (cont)

Q	Solution	Marks	Total	Comments														
4	Alternative solution																	
	(a)(iii) B(40, 0.15) expressions stated for at least 3 terms within $5 \leq U \leq 10$ gives probability = 0.5(00) to 0.501	M2 A1		Can be implied by a correct answer AWFW (0.5003)														
	<table border="1"> <tr> <td>u</td> <td>(5)</td> <td>6</td> <td>7</td> <td>8</td> <td>9</td> <td>(10)</td> </tr> <tr> <td>$P(U = u)$</td> <td>(0.1692)</td> <td>0.1742</td> <td>0.1492</td> <td>0.1087</td> <td>0.0682</td> <td>(0.0373)</td> </tr> </table>	u	(5)	6	7	8	9	(10)	$P(U = u)$	(0.1692)	0.1742	0.1492	0.1087	0.0682	(0.0373)			
u	(5)	6	7	8	9	(10)												
$P(U = u)$	(0.1692)	0.1742	0.1492	0.1087	0.0682	(0.0373)												
			3															

Q	Solution	Marks	Total	Comments
5	Alternative solutions and additional guidelines			
	(b) Attempt at $\sum x$ $\sum x^2$ $\sum y$ & $\sum xy$ ($\sum y^2$) or Attempt at S_{xx} & S_{yy} (S_{yy}) Attempt at correct formula for b (gradient) b (gradient) = -0.076 a (intercept) = 5.35 to 5.36 Thus $y = (5.35 \text{ to } 5.36) - 0.076x$ Notes: 1 If a and b interchanged and equation $y = ax + b$ used \Rightarrow max of 5 marks 2 If a and b interchanged and equation $y = a + bx$ used \Rightarrow maximum of BF1 3 Marks lost here cannot be gained from subsequent work in parts (d) and/or (e)	M1 m1 A1 A1 BF1		455 20475 35.1 & 883.5 (121.33) (all 4 attempted) 4550 & -345 (26.56) (both attempted) AWRT AWFW F on a and b even if rounded If a and b are not identified anywhere in equation, then: -0.07 to $-0.08 \Rightarrow$ B1 5.1 to $5.6 \Rightarrow$ B1
(d)	$y_{27} = (5.35 \text{ to } 5.36) - 0.076 \times 27$ $= 3.28 \text{ to } 3.32$	M1 A1	2	Clear evidence of correct use of c 's equation with $x = 27$ AWFW (3.30659)
(e)	$r(35, 2.5) = 2.5 - y_{35}$ $= 2.5 - \{(5.35 \text{ to } 5.36) - 0.076 \times 35\}$ $= -0.21 \text{ to } -0.19$	M1 A1	2	Used; allow $y_{35} - 2.5$ AWFW (-0.20000)

MS/SS1B (cont)

Q	Solution	Marks	Total	Comments
6 (a)(i)	Alternative solutions			
	Venn Diagram Method	B1		0.55; CAO
		B1 Bdep1	3	0.3 and 0.05; CAO 0.1; AG so dependent on B1 B1
(a)(i)	Formula Method $P(\geq 1) = 0.85 + 0.60 - 0.55$ OR $0.85 + 0.60 - 0.55 + p = 1$ OR $0.15 + 0.40 - 0.45$ $P(0) = 1 - P(\geq 1)$ OR $= 1 - 0.9 = 0.1$ $0.9 + p = 1$ OR $= 0.1$	M2 (M1) A1	3	Full justification for numerical expression Insufficient justification or numerical expression only AG; gained from M2 or M1
(b)(ii)	$0.1 \times (1 - 0.4)$ or 0.06 (0.3×0.25) or 0.075 or (0.05×0.25) or 0.0125 or (0.35×0.25) or 0.0875 or (0.1×0.4) or 0.04 $1 - (0.1875)$ $= 0.812$ to 0.813	M1 M1 B1 A1	4	At least one of these expressions or values OE; implied by correct answer AWFW (0.8125) CAO for equivalent fraction
(b)(ii)	$(0.55 + p)$ where $0 < p < 0.45$ (0.3×0.75) or 0.225 or (0.05×0.75) or 0.0375 or (0.35×0.75) or 0.2625 $0.55 + 0.2625$ $= 0.812$ to 0.813	M1 M1 B1 A1	4	At least one of these expressions or values OE; implied by correct answer AWFW (0.8125) CAO for equivalent fraction

MS/SS1B (cont)

Q	Solution	Marks	Total	Comments
7 (a)(ii)	Alternative solutions			
	$P(X < 0 \mid N(45.8, 24.0^2)) = P(Z < -1.91)$ $= 0.027$ to 0.03	M1 A1	2	Standardising 0 using 45.8 & 24.0 In addition to probability within range, must state that negative salaries are impossible
	$P(X > 60 \mid N(45.8, 24.0^2)) = P(Z > 0.59)$ $= 0.27$ to 0.28	M1 A1	2	Standardising 60 using 45.8 & 24.0 In addition to probability within range, must compare calculated value to $6/50 = 0.12$ OE
(c)	Additional comment illustrations			
	It/(claimed) mean/(claimed) value > UCL/CI	B0		Must indicate 55 or 55000
	99% have (mean) weights between CLs so ...	B0		
	Any comparison of 60 (£60 000) with UCL/CI	B0		Value of 60 does not refer to mean
	$P(X > 60 \mid N(45.8, 24.0^2)) = P(Z > 0.59)$ $= (0.27 \text{ to } 0.28) > 6/50 = 0.12$	B0		Assumes salaries ~ N; cf (a)(ii)