1.

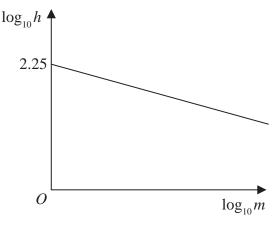


Figure 2

The resting heart rate, h, of a mammal, measured in beats per minute, is modelled by the equation

$$h = pm^q$$

where p and q are constants and m is the mass of the mammal measured in kg.

Figure 2 illustrates the linear relationship between  $\log_{10} h$  and  $\log_{10} m$ 

The line meets the vertical  $\log_{10} h$  axis at 2.25 and has a gradient of -0.235

(a) Find, to 3 significant figures, the value of p and the value of q.

**(3)** 

A particular mammal has a mass of 5kg and a resting heart rate of 119 beats per minute.

(b) Comment on the suitability of the model for this mammal.

**(3)** 

(c) With reference to the model, interpret the value of the constant p.

**(1)** 


2.	The mass,	A kg,	of algae	in a small	pond, is	modelled by	the equation
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$$A = pq^t$$

where p and q are constants and t is the number of weeks after the mass of algae was first recorded.

Data recorded indicates that there is a linear relationship between t and  $\log_{10} A$  given by the equation

$$\log_{10} A = 0.03t + 0.5$$

(a) Use this relationship to find a complete equation for the model in the form

$$A = pq^t$$

giving the value of p and the value of q each to 4 significant figures.

**(4)** 

- (b) With reference to the model, interpret
  - (i) the value of the constant p,
  - (ii) the value of the constant q.

**(2)** 

- (c) Find, according to the model,
  - (i) the mass of algae in the pond when t = 8, giving your answer to the nearest 0.5 kg,
  - (ii) the number of weeks it takes for the mass of algae in the pond to reach 4kg.

**(3)** 

(d) State one reason why this may not be a realistic model in the long term.

**(1)** 

- **3.** (a) Given that  $p = \log_3 x$ , where x > 0, find in simplest form in terms of p,
  - (i)  $\log_3\left(\frac{x}{9}\right)$
  - (ii)  $\log_3(\sqrt{x})$
  - (b) Hence, or otherwise, solve

$$2\log_3\left(\frac{x}{9}\right) + 3\log_3\left(\sqrt{x}\right) = -11$$

giving your answer as a simplified fraction.

Solut	ions relying on o	calculator technolo	gy are not accept	able.	
	, 3		1		<b>(4)</b>

	Using the laws of logarithms, solve the equation	
	$2\log_5(3x-2) - \log_5 x = 2$	
		(5)
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$\log_3(12y+5) - \log_3(1-3y) = 2 \tag{3}$

**6.** The time, T seconds, that a pendulum takes to complete one swing is modelled by the formula

$$T = al^b$$

where l metres is the length of the pendulum and a and b are constants.

(a) Show that this relationship can be written in the form

$$\log_{10} T = b \log_{10} l + \log_{10} a$$
 (2)

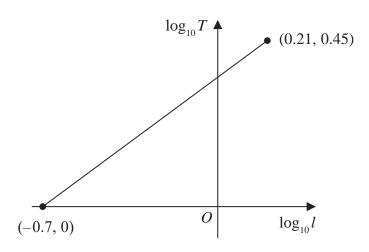


Figure 3

A student carried out an experiment to find the values of the constants a and b.

The student recorded the value of *T* for different values of *l*.

Figure 3 shows the linear relationship between  $\log_{10} l$  and  $\log_{10} T$  for the student's data. The straight line passes through the points (-0.7, 0) and (0.21, 0.45)

Using this information,

(b) find a complete equation for the model in the form

$$T = al^b$$

giving the value of a and the value of b, each to 3 significant figures.

**(3)** 

(c) With reference to the model, interpret the value of the constant a.

**(1)** 

7. (a) Sketch the curve with equation

$$y = 4^x$$

stating any points of intersection with the coordinate axes.

**(2)** 

(b) Solve

$$4^{x} = 100$$

giving your answer to 2 decimal places.

**(2)** 

8.  $a = \log_2 x$   $b = \log_2(x+8)$ 

Express in terms of a and/or b

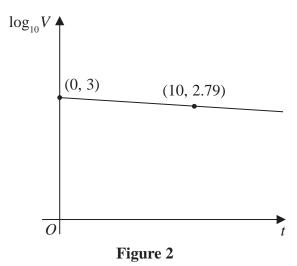
(a) 
$$\log_2 \sqrt{x}$$
 (1)

(b) 
$$\log_2(x^2 + 8x)$$
 (2)

(c) 
$$\log_2\left(8 + \frac{64}{x}\right)$$

Give your answer in simplest form. (3)

9.



The value, V pounds, of a mobile phone, t months after it was bought, is modelled by

$$V = ab^t$$

where a and b are constants.

Figure 2 shows the linear relationship between  $\log_{10} V$  and t.

The line passes through the points (0, 3) and (10, 2.79) as shown.

Using these points,

(a) find the initial value of the phone,

**(2)** 

(b) find a complete equation for *V* in terms of *t*, giving the exact value of *a* and giving the value of *b* to 3 significant figures.

**(3)** 

Exactly 2 years after it was bought, the value of the phone was £320

(c) Use this information to evaluate the reliability of the model.

**(2)** 

**(3)** 

10. Given that

$$\log_2(x+3) + \log_2(x+10) = 2 + 2\log_2 x$$

(a) show that

$$3x^2 - 13x - 30 = 0$$

(b) (i) Write down the roots of the equation

$$3x^2 - 13x - 30 = 0$$

(ii) Hence state which of the roots in part (b)(i) is not a solution of

$$\log_2(x+3) + \log_2(x+10) = 2 + 2\log_2 x$$

giving a reason for your answer. **(2)**