

## COORDINATE GEOMETRY

- 1 Write down an equation of the circle with the given centre and radius in each case.
 

**a** centre (0, 0) radius 5    **b** centre (1, 3) radius 2    **c** centre (4, -6) radius 1  
**d** centre (-1, -8) radius 3    **e** centre  $(-\frac{1}{2}, \frac{1}{2})$  radius  $\frac{1}{2}$     **f** centre (-3, 9) radius  $2\sqrt{3}$
- 2 Write down the coordinates of the centre and the radius of each of the following circles.
 

**a**  $x^2 + y^2 = 16$                                   **b**  $(x - 6)^2 + (y - 1)^2 = 81$                   **c**  $(x + 1)^2 + (y - 4)^2 = 121$   
**d**  $(x - 7)^2 + y^2 = 0.09$                           **e**  $(x + 2)^2 + (y + 5)^2 = 32$                   **f**  $(x - 8)^2 + (y + 9)^2 = 108$
- 3 Find the coordinates of the centre and the radius of each of the following circles.
 

**a**  $x^2 + y^2 - 4y + 3 = 0$                                   **b**  $x^2 + y^2 - 2x - 10y - 23 = 0$   
**c**  $x^2 + y^2 + 12x - 8y + 36 = 0$                           **d**  $x^2 + y^2 - 2x + 16y = 35$   
**e**  $x^2 + y^2 = 8x - 6y$     **f**  $x^2 + y^2 + 10x - 2y - 19 = 0$   
**g**  $4x^2 + 4y^2 - 4x - 24y + 1 = 0$                           **h**  $9x^2 + 9y^2 + 6x - 24y + 8 = 0$
- 4 Find an equation of the circle
 

**a** with centre (1, -2) which passes through the point (4, 2),  
**b** with centre (-5, 7) which passes through the point (0, 5).
- 5 Find an equation of the circle in which  $AB$  is a diameter in each case.
 

**a**  $A(1, -2)$      $B(3, -2)$                   **b**  $A(-7, 2)$      $B(1, 8)$                   **c**  $A(1, 1)$      $B(4, 0)$
- 6 The points  $P(0, 1)$ ,  $Q(3, 10)$  and  $R(6, 9)$  all lie on circle  $C$ .
 

**a** Show that  $\angle PQR$  is a right-angle.  
**b** Hence, show that  $C$  has the equation  $x^2 + y^2 - 6x - 10y + 9 = 0$ .
- 7 Find in each case whether the given point lies inside, outside or on the given circle.
 

**a** (0, -9)     $x^2 + y^2 = 64$                                   **b** (4, 7)     $x^2 + y^2 - 2x - 6y - 26 = 0$   
**c** (7, -3)     $x^2 + y^2 + 10x - 4y = 140$                           **d** (-4, 1)     $x^2 + y^2 + 2x + 8y - 13 = 0$
- 8 The point  $P$  lies on the circle with equation  $x^2 + y^2 + 12x - 6y + 27 = 0$  and the point  $Q$  has coordinates (8, 1). Find the minimum length of  $PQ$  giving your answer in the form  $k\sqrt{2}$ .
- 9 Find an equation of the circle which crosses the  $x$ -axis at the points (2, 0) and (8, 0) and touches the  $y$ -axis at the point (0, 4).
- 10 Given that the circle with equation  $x^2 + y^2 + 8x - 12y + k = 0$  does not touch or cross either of the coordinate axes, find the set of possible values of the constant  $k$ .
- 11 The circle  $C$  passes through the points  $P$ ,  $Q$  and  $R$  with coordinates (-2, -2), (2, -4) and (7, 1) respectively.
 

**a** Find an equation of the perpendicular bisector of the points  $P$  and  $Q$ .  
**b** Find the coordinates of the centre of  $C$ .  
**c** Find an equation of  $C$ .

<b>COORDINATE GEOMETRY</b>	<i>continued</i>
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- 12** The circle  $C$  has the equation  $x^2 + y^2 - 4x - 4y - 28 = 0$ .
- a** Find the distance of the point  $A(10, 8)$  from the centre of  $C$ .  
The tangent to  $C$  at the point  $B$  passes through  $A$ .
- b** Find the length  $AB$ .
- 13** A circle has the equation  $x^2 + y^2 + 6x - 2y = 0$  and passes through the point  $P$ .  
Given that the tangent to the circle at  $P$  passes through the point  $Q(2, 6)$ , find the exact length  $PQ$  in its simplest form.
- 14** The circle  $C$  has the equation  $x^2 + y^2 - 6x - 10y + 16 = 0$  and passes through the point  $A(6, 2)$ .
- a** Find the coordinates of the centre of  $C$ .
- b** Find the gradient of the normal to the circle at  $A$ .
- c** Find an equation of the normal to the circle at  $A$ .
- 15** Find an equation of
- a** the normal to the circle with equation  $x^2 + y^2 + 4x = 13$  at the point  $(-1, 4)$ ,
- b** the tangent to the circle with equation  $x^2 + y^2 + 2x + 4y - 40 = 0$  at the point  $(5, 1)$ ,
- c** the tangent to the circle with equation  $x^2 + y^2 - 10x + 4y + 4 = 0$  at the point  $(2, 2)$ .
- 16** Find the coordinates of the points where the circle with equation  $x^2 + y^2 - 6x + 6y - 16 = 0$  intersects the coordinate axes.
- 17** Find in each case the coordinates of the points where the line  $l$  intersects the circle  $C$ .
- a**  $l: y = x - 4$        $C: x^2 + y^2 = 10$
- b**  $l: 3x + y = 17$        $C: x^2 + y^2 - 4x - 2y - 15 = 0$
- c**  $l: y = 2x + 2$        $C: 4x^2 + 4y^2 + 4x - 8y - 15 = 0$
- 18** The line with equation  $y = 1 - x$  intersects the circle with equation  $x^2 + y^2 + 6x + 2y = 27$  at the points  $A$  and  $B$ .  
Find the length of the chord  $AB$ , giving your answer in the form  $k\sqrt{2}$ .
- 19** Show that the line with equation  $y = 2x + 1$  is a tangent to the circle with equation  $x^2 + y^2 - 8x - 8y + 27 = 0$  and find the coordinates of the point where they touch.
- 20** The line with equation  $y = x + k$  is a tangent to the circle with equation  $x^2 + y^2 + 6x - 8y + 17 = 0$ .  
Find the two possible values of  $k$ .
- 21** The line with equation  $y = mx$  is a tangent to the circle with equation  $x^2 + y^2 - 8x - 16y + 72 = 0$ .  
Find the two possible values of  $m$ .
- 22** The line with equation  $2x + 3y = k$  is a tangent to the circle with equation  $x^2 + y^2 + 6x + 4y = 0$ .  
Find the two possible values of  $k$ .
- 23** The circle with equation  $x^2 + y^2 - 4x - 6y = 7$  crosses the  $y$ -axis at the points  $A$  and  $B$ .
- a** Find the coordinates of the points  $A$  and  $B$ .
- b** Find the coordinates of the point where the tangent to the circle at  $A$  intersects the tangent to the circle at  $B$ .