

1. Express $\frac{(x-7)(x-2)}{(x+2)(x-1)^2}$ in partial fractions.

[5]

2. Express $\frac{9x^2 + 43x + 8}{(3+x)(1-x)(2x+1)}$ in partial fractions.

[4]

END OF QUESTION paper

Mark scheme

Question	Answer/Indicative content	Marks	Part marks and guidance
1	$\frac{(x-7)(x-2)}{(x+2)(x-1)^2} \equiv \frac{A}{x+2} + \frac{B}{x-1} + \frac{C}{(x-1)^2}$ <p>[If no partial fractions seen anywhere, B0]</p> <p>$(x-7)(x-2) \equiv A(x-1)^2 + B(x+2)(x-1) + C(x+2)$ [Allow careless minor error but not algebraic method error] or any equiv identity such as</p> $\frac{(x-7)(x-2)}{(x-1)^2} \equiv A + \frac{B(x+2)}{(x-1)} + \frac{C(x+2)}{(x-1)^2}$ <p>(or even the identity on the 1st line), in which values of x are substituted (or cfs compared)</p> $A = 4, B = -3, C = 2 \text{ or } \frac{4}{x+2} - \frac{3}{x-1} + \frac{2}{(x-1)^2} \text{ ISW}$ <p>The 3 @ A1 are dep on the used identity being correct.</p> <p>Cover-up: $A = 4, C = 2$ score B1, B1; $B = -3$ needs M1, then A1</p>	<p>B1</p> <p>M1</p> <p>A1,1,1</p>	^{SC} $\frac{(x-7)(x-2)}{(x+2)(x-1)^2} \equiv \frac{A}{x+2} + \frac{Bx+C}{(x-1)^2}$ <p>[If no partial fractions seen anywhere, B0]</p> <p>$(x-7)(x-2) \equiv A(x-1)^2 + (Bx+C)(x+2)$ [Allow careless minor error but not algebraic method error] or any equivalent identity (as in previous column) (or even the identity on the 1st line), in which values of x are substituted (or cfs compared)</p> $A = 4, B = -3, C = 5 \text{ or } \frac{4}{x+2} + \frac{-3x+5}{(x-1)^2}$ <p>A1</p> <p>This gives max 3/5 for easier case</p> <p>Examiner's Comments</p> <p>This was generally answered well though a few candidates did not show the format of the partial fractions and expected the examiner to know the meaning of the A, B and C in their solution.</p>
Total		5	
2	$\frac{A}{3+x} + \frac{B}{1-x} + \frac{C}{2x+1}$ <p>[$9x^2 + 43x + 8 \equiv$]</p> <p>$A(1-x)(2x+1) + B(3+x)(2x+1) + C(3+x)(1-x)$ soi</p> <p>$A = 2$ $B = 5$ $C = -3$ isw</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>if not seen here, may be awarded at end</p> <p>allow sign errors only</p> $\frac{2}{3+x} + \frac{5}{1-x} - \frac{3}{2x+1}$

				A1	
				[5]	
					Examiner's Comments
					Nearly all the candidates were familiar with this topic, and most went on to score full marks. A few slipped up with the arithmetic and obtained one or sometimes two incorrect coefficients. Those who attempted a solution by equating coefficients went astray more frequently.
			Total	5	