

# ALGEBRA

- 1** Express in the form  $(x + a)^2 + b$
- |                            |                                  |                                   |   |
|----------------------------|----------------------------------|-----------------------------------|---|
| <b>a</b> $x^2 + 2x + 4$    | <b>b</b> $x^2 - 2x + 4$          | <b>c</b> $x^2 - 4x + 1$           | <b>d</b> $x^2 + 6x$                         |
| <b>e</b> $x^2 + 4x + 8$    | <b>f</b> $x^2 - 8x - 5$          | <b>g</b> $x^2 + 12x + 30$         | <b>h</b> $x^2 - 10x + 25$                   |
| <b>i</b> $x^2 + 6x - 9$    | <b>j</b> $18 - 4x + x^2$         | <b>k</b> $x^2 + 3x + 3$           | <b>l</b> $x^2 + x - 1$                      |
| <b>m</b> $x^2 - 18x + 100$ | <b>n</b> $x^2 - x - \frac{1}{2}$ | <b>o</b> $20 + 9x + x^2$          | <b>p</b> $x^2 - 7x - 2$                     |
| <b>q</b> $5 - 3x + x^2$    | <b>r</b> $x^2 - 11x + 37$        | <b>s</b> $x^2 + \frac{2}{3}x + 1$ | <b>t</b> $x^2 - \frac{1}{2}x - \frac{1}{4}$ |
- 2** Express in the form  $a(x + b)^2 + c$
- |                            |                           |                            |  |
|----------------------------|---------------------------|----------------------------|--|
| <b>a</b> $2x^2 + 4x + 3$   | <b>b</b> $2x^2 - 8x - 7$  | <b>c</b> $3 - 6x + 3x^2$   | <b>d</b> $4x^2 + 24x + 11$                             |
| <b>e</b> $-x^2 - 2x - 5$   | <b>f</b> $1 + 10x - x^2$  | <b>g</b> $2x^2 + 2x - 1$   | <b>h</b> $3x^2 - 9x + 5$                               |
| <b>i</b> $3x^2 - 24x + 48$ | <b>j</b> $3x^2 - 15x$     | <b>k</b> $70 + 40x + 5x^2$ | <b>l</b> $2x^2 + 5x + 2$                               |
| <b>m</b> $4x^2 + 6x - 7$   | <b>n</b> $-2x^2 + 4x - 1$ | <b>o</b> $4 - 2x - 3x^2$   | <b>p</b> $\frac{1}{3}x^2 + \frac{1}{2}x - \frac{1}{4}$ |
- 3** Solve each equation by completing the square, giving your answers as simply as possible in terms of surds where appropriate.
- |                             |                               |                             |                              |
|-----------------------------|-------------------------------|-----------------------------|------------------------------|
| <b>a</b> $y^2 - 4y + 2 = 0$ | <b>b</b> $p^2 + 2p - 2 = 0$   | <b>c</b> $x^2 - 6x + 4 = 0$ | <b>d</b> $7 + 10r + r^2 = 0$ |
| <b>e</b> $x^2 - 2x = 11$    | <b>f</b> $a^2 - 12a - 18 = 0$ | <b>g</b> $m^2 - 3m + 1 = 0$ | <b>h</b> $9 - 7t + t^2 = 0$  |
| <b>i</b> $u^2 + 7u = 44$    | <b>j</b> $2y^2 - 4y + 1 = 0$  | <b>k</b> $3p^2 + 18p = -23$ | <b>l</b> $2x^2 + 12x = 9$    |
| <b>m</b> $-m^2 + m + 1 = 0$ | <b>n</b> $4x^2 + 49 = 28x$    | <b>o</b> $1 - t - 3t^2 = 0$ | <b>p</b> $2a^2 - 7a + 4 = 0$ |
- 4** By completing the square, find the maximum or minimum value of  $y$  and the value of  $x$  for which this occurs. State whether your value of  $y$  is a maximum or a minimum in each case.
- |                               |                               |                               |
|-------------------------------|-------------------------------|-------------------------------|
| <b>a</b> $y = x^2 - 2x + 7$   | <b>b</b> $y = x^2 + 2x - 3$   | <b>c</b> $y = 1 - 6x + x^2$   |
| <b>d</b> $y = x^2 + 10x + 35$ | <b>e</b> $y = -x^2 + 4x + 4$  | <b>f</b> $y = x^2 + 3x - 2$   |
| <b>g</b> $y = 2x^2 + 8x + 5$  | <b>h</b> $y = -3x^2 + 6x$     | <b>i</b> $y = 7 - 5x - x^2$   |
| <b>j</b> $y = 4x^2 - 12x + 9$ | <b>k</b> $y = 4x^2 + 20x - 8$ | <b>l</b> $y = 17 - 2x - 2x^2$ |
- 5** Sketch each curve showing the exact coordinates of its turning point and the point where it crosses the  $y$ -axis.
- |                              |                                |                                |
|------------------------------|--------------------------------|--------------------------------|
| <b>a</b> $y = x^2 - 4x + 3$  | <b>b</b> $y = x^2 + 2x - 24$   | <b>c</b> $y = x^2 - 2x + 5$    |
| <b>d</b> $y = 30 + 8x + x^2$ | <b>e</b> $y = x^2 + 2x + 1$    | <b>f</b> $y = 8 + 2x - x^2$    |
| <b>g</b> $y = -x^2 + 8x - 7$ | <b>h</b> $y = -x^2 - 4x - 7$   | <b>i</b> $y = x^2 - 5x + 4$    |
| <b>j</b> $y = x^2 + 3x + 3$  | <b>k</b> $y = 3 + 8x + 4x^2$   | <b>l</b> $y = -2x^2 + 8x - 15$ |
| <b>m</b> $y = 1 - x - 2x^2$  | <b>n</b> $y = 25 - 20x + 4x^2$ | <b>o</b> $y = 3x^2 - 4x + 2$   |
- 6** **a** Express  $x^2 - 4\sqrt{2}x + 5$  in the form  $a(x + b)^2 + c$ .  
**b** Write down an equation of the line of symmetry of the curve  $y = x^2 + 4\sqrt{2}x + 5$ .
- 7**  $f(x) \equiv x^2 + 2kx - 3$ .  
 By completing the square, find the roots of the equation  $f(x) = 0$  in terms of the constant  $k$ .