CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International Advanced Subsidiary and Advanced Level

MARK SCHEME for the May/June 2015 series

9709 MATHEMATICS

9709/63 Paper 6, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2015 series for most Cambridge IGCSE®, Cambridge International A and AS Level components and some Cambridge O Level components.

Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.

- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

  The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

The following abbreviations may be used in a mark scheme or used on the scripts:

AEF Any Equivalent Form (of answer is equally acceptable)

AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)

BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)

CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)

CWO Correct Working Only – often written by a 'fortuitous' answer

ISW Ignore Subsequent Working

MR Misread

PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)

SOS See Other Solution (the candidate makes a better attempt at the same question)

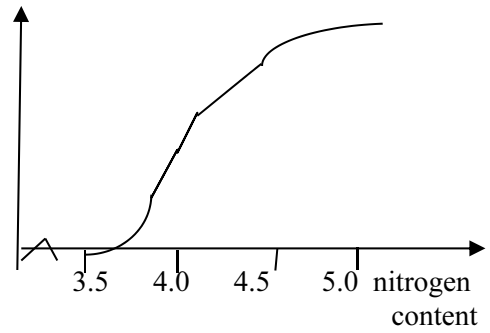
SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

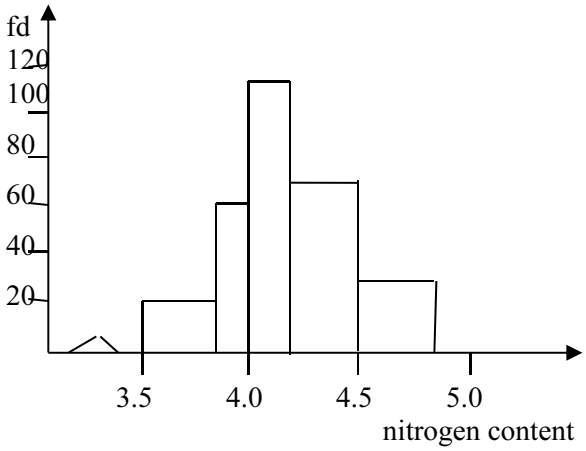
MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR –2 penalty may be applied in particular cases if agreed at the coordination meeting.

PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

1	$z = 1.136$ $1.136 = \frac{195 - \mu}{22}$ $\mu = 170$	B1 M1 A1 **[3]**	± 1.136 seen, not ±1.14, Standardising, no cc no sq rt, equated to their z not 0.128 or 0.872 Correct answer, nfww
2	**(i)**		All values may be decimals or %
		B1	2 probabilities correct
		B1	2 further probabilities correct
		B1 **[3]**	2 further probabilities correct
	(ii) P(not on time given kitchen mess) $= \frac{1/2}{3/5}$ $= 5/6$ o.e.	M1 A1 **[2]**	A cond prob fraction seen (using corresponding combined outcomes and total) FT from their values, 3sf or better, <1, 3/5ft<1
3	$\mu = 300\times0.072 = 21.6,\ \sigma^2 = 20.0448$ $P(x < 18) = P\left(z < \frac{17.5 - 21.6}{\sqrt{20.0448}}\right)$ $=P(z < -0.9157)$ $= 1 - 0.8201$ $= 0.180$	B1 M1 M1 M1 A1 **[5]**	300×0.072 seen and $300\times0.072\times0.928$ seen or implied ($\sigma = 4.4771, \sigma^2 = 20(.0)$) oe ±Standardising, their mean/var, with sq root Cont corr 17.5 or 18.5 Correct area 1 - Φ Answer wrt 0.180, nfww
4	**(i)** P(1 W) = 6/9×3/8 + 3/9×6/8 = ½ AG OR $\frac{{}^6C_1 \times {}^3C_1}{{}^9C_2}$ = ½ AG	M1 A1 **[2]** M1 A1	summing 2 two-factor probs (condone replacement) not ½×½ + ½×½ Correct answer, fully justified Using combinations consistent, correct format Correct answer, fully justified
	(ii) $P(\overline{W},\overline{W}) = 3/9\times2/8 = 6/72$ (1/12) $P(W,W) = 6/9\times5/8 = 30/72$ (5/12) x: 0, 1, 2 Prob: 1/12, 1/2, 5/12	B1 B1 B1√ **[3]**	Distribution table with 0,1,2 only $P(W,W)$ or $P(\overline{W},\overline{W})$ correct $P(W,W) + P(\overline{W},\overline{W}) = 0.5$
	(iii) E(X) = 16/12 (4/3) (1.33) isw	B1 **[1]**	Condone 1(.3) if correct working seen, nfww

5	**(i)**	P(large) = 1 - $\Phi\left(\frac{29-21.7}{6.5}\right)$ = 1 – Φ(1.123) = 1 – 0.8692 = 0.1308 P(0,1) = $(0.8692)^{8\backslash}$ + $^8C_1(0.1308)(0.8692)^7$ = 0.718	M1 M1 A1 M1 M1 A1	**[6]**	Standardising no cc no sq rt Correct area 1 – Φ Rounding to 0.13 Any bin term with $^8C_x p^x(1-p)^{8-x}$ $0 < p < 1$ Summing bin P(0) + P(1) only with $n = 8$, oe Correct ans
	(ii)	$= 1 - (0.8692)^n > 0.98$ $(0.8692)^n < 0.02$ Least number = 28	M1 M1 A1	**[3]**	eq/ineq involving their $(0.8692)^n$ or $(0.1308)^n$, 0.02 or 0.98 oe with or without a 1 solving attempt (could be trial and error) – may be implied by their answer correct answer
6	**(i)**	cf  	B1 M1 A1	**[3]**	Uniform axes cf and nitrogen content labelled, at least 0 to 70 and 3.5 to 4.8 seen 5 points plotted correctly on graph paper All points correct and a reasonable curve (condone 1 missed point) or line segments.
	(ii)	70 – their 55 = 15 = 21.4%	M1 A1	**[2]**	Subt a value > 41 from 70 (or n/70, n<29) Correct ans, accept 18.5 – 22
	(iii)	median = 4.15	B1	**[1]**	Accept 4.1< median < 4.2, nfww

3.5	3.8	4.0	4.2	4.5	4.8
0	6	18	41	62	70

	(iv)	<table><tr><td>nit cont</td><td>3.5– 3.8</td><td>3.8– 4.0</td><td>4.0– 4.2</td><td>4.2– 4.5</td><td>4.5– 4.8</td></tr><tr><td>fr</td><td>6</td><td>12</td><td>23</td><td>21</td><td>8</td></tr><tr><td>fd</td><td>20</td><td>60</td><td>115</td><td>70</td><td>26.7</td></tr></table> 	M1 M1 A1 B1 B1 **[5]**	Attempt at freqs, at least 3 correct, ignore labelling Attempt at fd as f/cw only at least 3 correct FT (Accept f/cw × k) Correct heights seen on graph (plot at 4.8,27 A0) Graph paper must be used (3 correct relative heights implies M1M1) Correct bar ends seen on graph – graph paper used Correct linear scale and labels.
7	**(i)**	W S D 1 1 $3 = 6\times4\times{}^3C_3 = 24$ 1 3 $1 = 6\times{}^4C_3\times3 = 72$ 3 1 $1 = {}^6C_3\times4\times3 = 240$ 1 2 $2 = 6\times{}^4C_2\times{}^3C_2 = 108$ 2 1 $2 = {}^6C_2\times4\times{}^3C_2 = 180$ 2 2 $1 = {}^6C_2\times{}^4C_2\times3 = 270$ Total = 894	M1 M1 M1 B1 A1 **[5]**	Listing at least 4 different options Mult 3 (combs) together assume $6 = {}^6C_1$, $\Sigma r=5$ Summing at least 4 different evaluated/unsimplified options >1 At least 3 correct unsimplified options Correct answer
	(ii)	${}^3P_2 \times {}^{10}P_8$ = 10886400	B1 B1 B1 **[3]**	${}^3P_2$ oe seen multiplied either here or in (iii) $k^{10}P_x$ seen or k^yP_8 with no addition, $k\geqslant1$, $y>8$, $x<10$ Correct answer, nfww
	(iii)	DSWSWSWSWD or DWSWSWSWSD D in ${}^3P_2$ ways = 6 S in ${}^4P_4$ ways = 24 W in ${}^6P_4 = 360$ Swap SW in 2 ways Total = 103680 ways	 B1 B1 B1 **[3]**	If ${}^3P_2$ has not gained credit in (ii) may be awarded ${}^4P_4$ or ${}^6P_4$ oe seen multiplied or common in all terms (no division) Mult by 2 (condone 2!) Correct answer, 3sf or better, nfww