



## AS Level Further Mathematics B (MEI) Y410 Core Pure

Sample Question Paper

# Date – Morning/Afternoon

Time allowed: 1 hour 15 minutes



#### OCR supplied materials:

- Printed Answer Booklet
- Formulae Further Mathematics B (MEI)

### You must have:

- Printed Answer Booklet
- Formulae Further Mathematics B (MEI)
- Scientific or graphical calculator



## INSTRUCTIONS

- Use black ink. HB pencil may be used for graphs and diagrams only.
- Complete the boxes provided on the Printed Answer Booklet with your name, centre number and candidate number.
- Answer **all** the questions.
- Write your answer to each question in the space provided in the Printed Answer Booklet.
- Additional paper may be used if necessary but you must clearly show your candidate number, centre number and question number(s).
- Do not write in the bar codes.
- You are permitted to use a scientific or graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

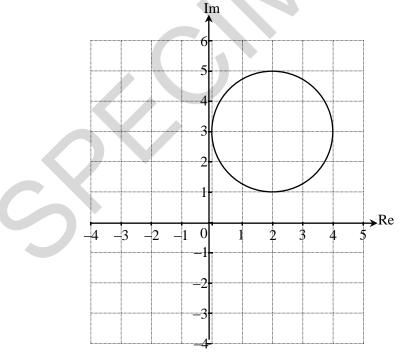
## INFORMATION

- The total number of marks for this paper is 60.
- The marks for each question or part question are shown in brackets [].
- You are advised that an answer may receive no marks unless you show sufficient detail of the working to indicate that a correct method is used. You should communicate your method with correct reasoning.
- The Printed Answer Booklet consists of **12** pages. The Question Paper consists of **4** pages.

#### Answer **all** the questions.

The complex number z<sub>1</sub> is 1+ i and the complex number z<sub>2</sub> has modulus 4 and argument π/3.
 (i) Express z<sub>2</sub> in the form a + bi, giving a and b in exact form.
 (ii) Express z<sub>2</sub>/z<sub>1</sub> in the form c + di, giving c and d in exact form.
 (i) Describe fully the transformation represented by the matrix (1 2)/(0 1).
 (ii) A triangle of area 5 square units undergoes the transformation represented by the matrix (1 2)/(0 1).
 (iii) A triangle of area 5 square units undergoes the transformation represented by the matrix (1 2)/(0 1).

3 (i) Write down, in complex form, the equation of the locus represented by the circle in the Argand diagram shown in Fig. 3. [2]





(ii) On the copy of Fig. 3 in the Printed Answer Booklet mark with a cross any point(s) on the circle for which  $\arg(z-2i) = \frac{\pi}{4}$ . [2]

[4]

[7]

4 (i) Find the coordinates of the point where the following three planes intersect. Give your answers in terms of *a*.

$$x-2y-z = 6$$
  

$$3x + y + 5z = -4$$
  

$$-4x + 2y - 3z = a$$

(ii) Determine whether the intersection of the three planes could be on the *z*-axis. [2]

5 The cubic equation 
$$x^3 - 4x^2 + px + q = 0$$
 has roots  $\alpha$ ,  $\frac{2}{\alpha}$  and  $\alpha + \frac{2}{\alpha}$ .

Find

- the values of the roots of the equation,
- the value of *p*.

6 (i) Show that, when 
$$n = 5$$
,  $\sum_{r=n+1}^{2n} r^2 = 330$ . [1]

- (ii) Find, in terms of *n*, a fully factorised expression for  $\sum_{r=n+1}^{2n} r^2$ . [4]
- 7 The plane  $\Pi$  has equation 3x 5y + z = 9.
  - (i) Show that  $\Pi$  contains
    - the point (4,1,2)

and

• the vector 
$$\begin{pmatrix} 1\\1\\2 \end{pmatrix}$$
. [4]

(ii) Determine the equation of a plane which is perpendicular to  $\Pi$  and which passes through (4,1,2). [3]

### 8 In this question you must show detailed reasoning.

- (i) Explain why all cubic equations with real coefficients have at least one real root. [2]
- (ii) Points representing the three roots of the equation  $z^3 + 9z^2 + 27z + 35 = 0$  are plotted on an Argand diagram.

Find the exact area of the triangle which has these three points as its vertices. [7]

9 You are given that matrix  $\mathbf{M} = \begin{pmatrix} -3 & 8 \\ -2 & 5 \end{pmatrix}$ .

(i) Prove that, for all positive integers n,  $\mathbf{M}^n = \begin{pmatrix} 1-4n & 8n \\ -2n & 1+4n \end{pmatrix}$ . [6]

(ii) Determine the equation of the line of invariant points of the transformation represented by the matrix M.

It is claimed that the answer to part (ii) is also a line of invariant points of the transformation represented by the matrix  $\mathbf{M}^n$ , for any positive integer *n*.

- (iii) Explain *geometrically* why this claim is true.
- (iv) Verify *algebraically* that this claim is true.

#### **END OF QUESTION PAPER**

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