



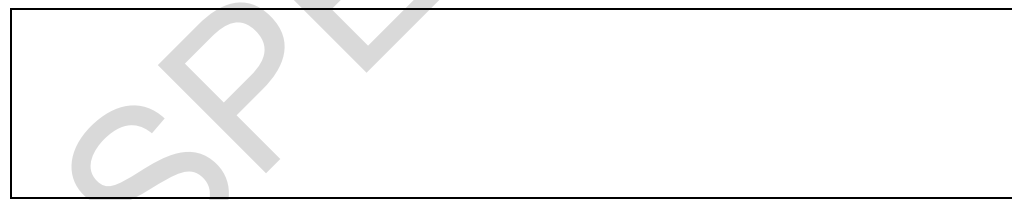
...day June 20XX – Morning/Afternoon

**A Level Further Mathematics B (MEI)
Y433 Modelling with Algorithms**

SAMPLE MARK SCHEME

Duration: 1 hour 15 minutes

MAXIMUM MARK 60



This document consists of 16 pages

Y433

Mark Scheme

June 20XX

Text Instructions

1. Annotations and abbreviations

| Annotation in scoris | Meaning |
|------------------------------------|---|
| ✓ and ✕ | |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0, 1 |
| B0, B1 | Independent mark awarded 0, 1 |
| SC | Special case |
| ^ | Omission sign |
| MR | Misread |
| Highlighting | |
| | |
| Other abbreviations in mark scheme | Meaning |
| E1 | Mark for explaining a result or establishing a given result |
| dep* | Mark dependent on a previous mark, indicated by * |
| cao | Correct answer only |
| oe | Or equivalent |
| rot | Rounded or truncated |
| soi | Seen or implied |
| www | Without wrong working |
| AG | Answer given |
| awrt | Anything which rounds to |
| BC | By Calculator |
| DR | This indicates that the instruction In this question you must show detailed reasoning appears in the question. |

2. Subject-specific Marking Instructions for Level Further Mathematics B (MEI)

- a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.
- c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

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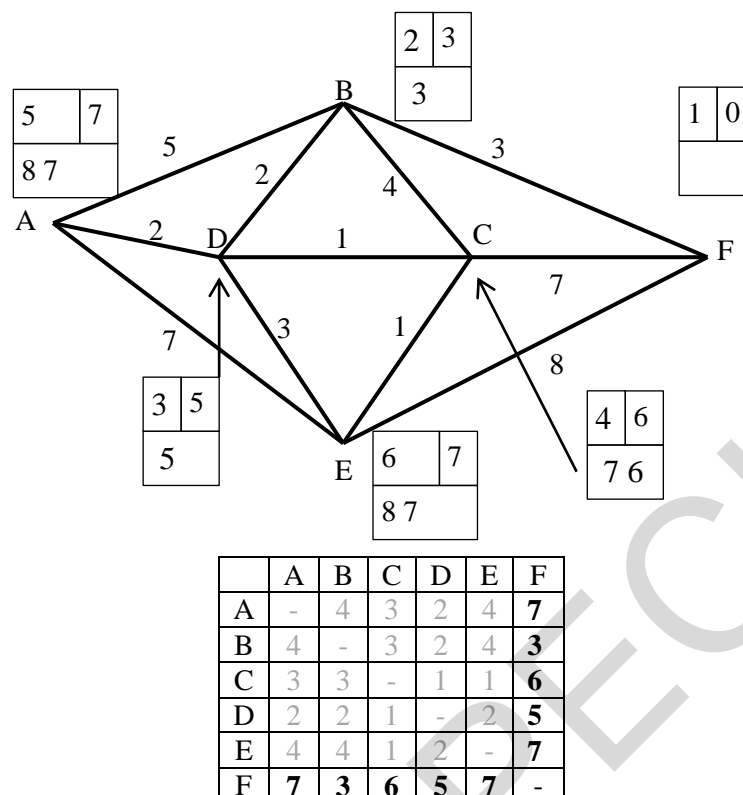
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.
- g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate’s data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some papers. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. ‘Fresh starts’ will not affect an earlier decision about a misread. Note that a miscopy of the candidate’s own working is not a misread but an accuracy error.
- i If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.
- k Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned on this occasion, but shows what a complete solution might look like

| Question | | Answer | Marks | AOs | Guidance |
|----------|-------|---|-------------------------------------|--------------------------------|---|
| 1 | (i) | 1,2,4,5,7 | B1 [1] | 1.1 | |
| 1 | (ii) | E.g. Step 60 If $n < 6$ then go to Step 30 Step 70 Stop | M1 A1 [2] | 1.1 1.2 | Stopping condition... ...in the right place and gives 5 terms |
| 1 | (iii) | 3,6,10,13,17 | B1 [1] | 1.1 | |
| 1 | (iv) | $u(71) = 100$ $v(29) = 99, v(30) = 102$ 100 is in $u(n)$ but not $v(n)$, so true for $m = 100$. | B1 B1 E1 [3] | 3.2a 1.1 2.1 | |
| 2 | | | M1 A1 M1 A1 [4] | 1.1a 1.1 1.1a 1.1 | Forward pass Backward pass |

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| Question | Answer | Marks | AOs | Guidance | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------------|---|-----------------------------|--------------------|----------|----------|----------|---|---|---|---|---|---|---|---|----------|---|---|---|---|---|---|----------|---|---|---|---|---|---|----------|---|---|---|---|---|---|----------|---|---|---|---|---|---|----------|---|----------|----------|----------|----------|----------|---|---|--|--|
| <p>3 (i)</p> |  <table border="1" data-bbox="593 805 940 1061"> <thead> <tr> <th></th> <th>A</th> <th>B</th> <th>C</th> <th>D</th> <th>E</th> <th>F</th> </tr> </thead> <tbody> <tr> <th>A</th> <td>-</td> <td>4</td> <td>3</td> <td>2</td> <td>4</td> <td>7</td> </tr> <tr> <th>B</th> <td>4</td> <td>-</td> <td>3</td> <td>2</td> <td>4</td> <td>3</td> </tr> <tr> <th>C</th> <td>3</td> <td>3</td> <td>-</td> <td>1</td> <td>1</td> <td>6</td> </tr> <tr> <th>D</th> <td>2</td> <td>2</td> <td>1</td> <td>-</td> <td>2</td> <td>5</td> </tr> <tr> <th>E</th> <td>4</td> <td>4</td> <td>1</td> <td>2</td> <td>-</td> <td>7</td> </tr> <tr> <th>F</th> <td>7</td> <td>3</td> <td>6</td> <td>5</td> <td>7</td> <td>-</td> </tr> </tbody> </table> | | A | B | C | D | E | F | A | - | 4 | 3 | 2 | 4 | 7 | B | 4 | - | 3 | 2 | 4 | 3 | C | 3 | 3 | - | 1 | 1 | 6 | D | 2 | 2 | 1 | - | 2 | 5 | E | 4 | 4 | 1 | 2 | - | 7 | F | 7 | 3 | 6 | 5 | 7 | - | <p>M1 A1 B1</p> <p>[3]</p> | <p>1.1a 1.1 1.1</p> | <p>Dijkstra, starting from F All correct</p> <p>Order of labelling on A and E could be reversed</p> <p>All correct</p> |
| | A | B | C | D | E | F | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| A | - | 4 | 3 | 2 | 4 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B | 4 | - | 3 | 2 | 4 | 3 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| C | 3 | 3 | - | 1 | 1 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| D | 2 | 2 | 1 | - | 2 | 5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| E | 4 | 4 | 1 | 2 | - | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| F | 7 | 3 | 6 | 5 | 7 | - | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| <p>3 (ii)</p> | <p>Repeatedly applying Dijkstra will be $O(n^3)$</p> $\left(\frac{q}{p}\right)^t$ | <p>E1 B1</p> <p>[2]</p> | <p>2.4 3.3</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| <p>3 (iii)</p> | <p>$O(n^3)$ does not mean proportional to n^3, which is the assumption behind answer to (ii).</p> | <p>E1</p> <p>[1]</p> | <p>3.5b</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

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| Question | | Answer | Marks | AOs | Guidance | |
|----------|-------|---|---------------------------------|-------------------------------|----------|--|
| 4 | (i) | Largest (30) in 10 th /last place Smallest (21) in 9 th /penultimate place | B1 B1 [2] | 1.1 1.1 | | |
| 4 | (ii) | Each pass moves the smallest number 1 to left, so need $n - 1$ passes to get smallest number to left One checking pass with no swaps, so n passes altogether $n - 1$ comparisons in one pass $n(n - 1)$ comparisons altogether | E1 E1 M1 A1 [4] | 2.1 2.4 1.1 2.2a | | |
| 4 | (iii) | $n - 1$ $n(n - 1)$ | B1 B1 [2] | 1.1 2.2a | | |

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| Question | | Answer | Marks | AOs | Guidance | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------|-------|--|----------------------------------|-----------------------------|------------|--|----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|--|---|---|--|--|--|--|--|--|---|--|--|--|---|----|--|--|--|---|--|---|---|--|--|--|--|--|----|--|--|--|---|---|--|---|--|--|--|--|---|--|---|---|--|----|--|--|--|---|--|--|---|--|---|--|--|--|--|---|--|--|--|---|--|---|--|--|----|--|--|--|--|---|--|---|---|--|--|--|---|--|--|---|--|--|---|---|--|---|--|--|---|---|--|--|--|--|---|--|--|--|---|--|--|---|---|--|--|---|---|--|
| 5 | (i) | <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td></td> <td>1</td> <td>3</td> <td>2</td> <td>5</td> <td>4</td> <td>6</td> </tr> <tr> <td></td> <td>A</td> <td>B</td> <td>C</td> <td>D</td> <td>E</td> <td>F</td> <td>G</td> <td>H</td> <td>I</td> <td>J</td> </tr> <tr> <td>A</td> <td></td> <td></td> <td>8</td> <td>4</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>B</td> <td></td> <td></td> <td></td> <td>6</td> <td>10</td> <td></td> <td></td> <td></td> <td>7</td> <td></td> </tr> <tr> <td>C</td> <td>8</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>12</td> <td></td> <td></td> <td></td> </tr> <tr> <td>D</td> <td>4</td> <td></td> <td>6</td> <td></td> <td></td> <td></td> <td></td> <td>6</td> <td></td> <td>7</td> </tr> <tr> <td>E</td> <td></td> <td>10</td> <td></td> <td></td> <td></td> <td>8</td> <td></td> <td></td> <td>9</td> <td></td> </tr> <tr> <td>F</td> <td></td> <td></td> <td></td> <td></td> <td>8</td> <td></td> <td></td> <td></td> <td>8</td> <td></td> </tr> <tr> <td>G</td> <td></td> <td></td> <td>12</td> <td></td> <td></td> <td></td> <td></td> <td>6</td> <td></td> <td>9</td> </tr> <tr> <td>H</td> <td></td> <td></td> <td></td> <td>6</td> <td></td> <td></td> <td>6</td> <td></td> <td></td> <td>7</td> </tr> <tr> <td>I</td> <td></td> <td>7</td> <td></td> <td></td> <td>9</td> <td>8</td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>J</td> <td></td> <td></td> <td></td> <td>7</td> <td></td> <td></td> <td>9</td> <td>7</td> <td></td> <td></td> </tr> </table> | | 1 | 3 | 2 | 5 | 4 | 6 | | A | B | C | D | E | F | G | H | I | J | A | | | 8 | 4 | | | | | | | B | | | | 6 | 10 | | | | 7 | | C | 8 | | | | | | 12 | | | | D | 4 | | 6 | | | | | 6 | | 7 | E | | 10 | | | | 8 | | | 9 | | F | | | | | 8 | | | | 8 | | G | | | 12 | | | | | 6 | | 9 | H | | | | 6 | | | 6 | | | 7 | I | | 7 | | | 9 | 8 | | | | | J | | | | 7 | | | 9 | 7 | | | <p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p> | <p>1.1</p> <p>1.1</p> <p>1.1</p> | <p>Choosing 4 in column A Selecting at least two entries in column D</p> <p>All correct</p> <p>Order could be ADHCGJ or ADHGCJ</p> <p>JD replacing JH is an alternative solution</p> |
| | 1 | 3 | 2 | 5 | 4 | 6 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | A | B | C | D | E | F | G | H | I | J | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| A | | | 8 | 4 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| B | | | | 6 | 10 | | | | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| C | 8 | | | | | | 12 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| D | 4 | | 6 | | | | | 6 | | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| E | | 10 | | | | 8 | | | 9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| F | | | | | 8 | | | | 8 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| G | | | 12 | | | | | 6 | | 9 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| H | | | | 6 | | | 6 | | | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| I | | 7 | | | 9 | 8 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| J | | | | 7 | | | 9 | 7 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5 | (ii) | Algorithm terminates as no remaining values in cols A C D G H J | <p>E1</p> <p>[1]</p> | 2.2a | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5 | (iii) | (A) | | <p>B1</p> <p>[1]</p> | 1.1 | <p>Connector</p> <p>JD replacing JH is an alternative solution</p> | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 5 | (iii) | (B) | Length of minimum connector = 29 | <p>B1</p> <p>[1]</p> | 1.1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

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| Question | | | Answer | Marks | AOs | Guidance | |
|----------|------|-----|--|-------|-----|-------------------|--|
| 5 | (iv) | (A) | | B1 | 1.1 | Network | |
| | | | | [1] | | | |
| 5 | (iv) | (B) | | B1 | 1.2 | Minimum connector | |
| | | | | [1] | | | |
| 5 | (iv) | (C) | Length of minimum connector = 23 | B1 | 1.1 | | |
| | | | | [1] | | | |
| 5 | (v) | | <p>Arc AB must be in minimum connector otherwise not connected, and AB cannot be part of a cycle.</p> <p>If a shorter spanning tree than the one suggested is possible then there will be a shorter minimum connector for one or both of ACGHJ, BEFI</p> | E1 | 2.1 | | |
| | | | | E1 | 2.3 | | |
| | | | | [2] | | | |

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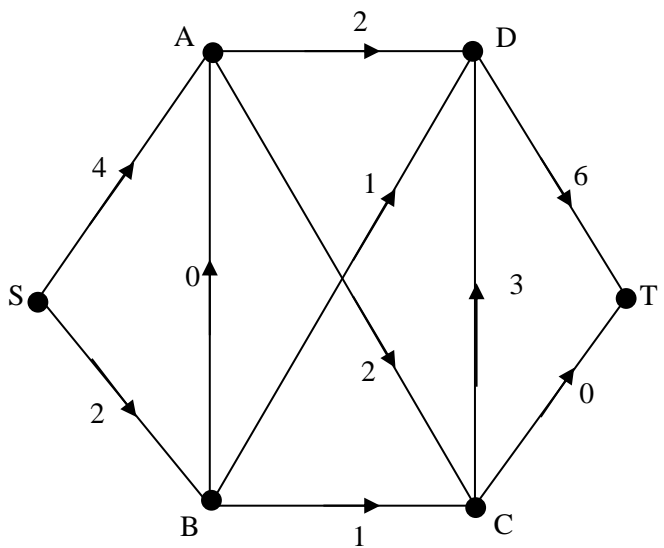
| Question | | Answer | Marks | AOs | Guidance | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------|------|--|---------------------|-------------------|---|----------------|----------------|----------------|----------------|----------------|-----|---|---|-------|---|------|---|---|-------|-------|---|---|------|---|-----|---|---|-------|-----|---|---|------|---|------|---|---|------|-----|---|---|------|---|------|---|---|-------|------|---|---|--------|---|-------|---|---|-------|------|---------------------|------------|----------------------|
| 5 | (vi) | E.g. If arc length AB = 1 and arc length CE = 100 [then applying Kruskal] will produce the suggested minimum connector. E.g. If arc length AB = arc length CE = 1 [then applying Kruskal] will produce a minimum connector with both of AB and CE in it. So sometimes true | E1 | 3.1a | Example of true | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | E1 | 2.4 | Example when false | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | E1 dep [3] | 2.2a | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | (i) | Maximise $5x + 2y + 3z$ subject to $2x + 5y + 3z \leq 20$ $2y + z \leq 10$ $2x + 4y + 2z \leq 70$ $4x + 3y + 2z \leq 30$ $x, y, z \geq 0$ | M1 A2 [3] | 3.3 3.3 1.1 | objective constraints -1 each error | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | (ii) | (A) <table border="1" style="margin-left: 20px;"> <thead> <tr> <th>P</th> <th>x</th> <th>y</th> <th>z</th> <th>s₁</th> <th>s₂</th> <th>s₃</th> <th>s₄</th> <th>RHS</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>0</td> <td>2.625</td> <td>0</td> <td>0.25</td> <td>0</td> <td>0</td> <td>1.125</td> <td>38.75</td> </tr> <tr> <td>0</td> <td>0</td> <td>1.75</td> <td>1</td> <td>0.5</td> <td>0</td> <td>0</td> <td>-0.25</td> <td>2.5</td> </tr> <tr> <td>0</td> <td>0</td> <td>0.25</td> <td>0</td> <td>-0.5</td> <td>1</td> <td>0</td> <td>0.25</td> <td>7.5</td> </tr> <tr> <td>0</td> <td>0</td> <td>0.75</td> <td>0</td> <td>-0.5</td> <td>0</td> <td>1</td> <td>-0.25</td> <td>52.5</td> </tr> <tr> <td>0</td> <td>1</td> <td>-0.125</td> <td>0</td> <td>-0.25</td> <td>0</td> <td>0</td> <td>0.375</td> <td>6.25</td> </tr> </tbody> </table> | P | x | y | z | s ₁ | s ₂ | s ₃ | s ₄ | RHS | 1 | 0 | 2.625 | 0 | 0.25 | 0 | 0 | 1.125 | 38.75 | 0 | 0 | 1.75 | 1 | 0.5 | 0 | 0 | -0.25 | 2.5 | 0 | 0 | 0.25 | 0 | -0.5 | 1 | 0 | 0.25 | 7.5 | 0 | 0 | 0.75 | 0 | -0.5 | 0 | 1 | -0.25 | 52.5 | 0 | 1 | -0.125 | 0 | -0.25 | 0 | 0 | 0.375 | 6.25 | M1 A1 [2] | 3.4 1.1 | Pivot all correct |
| P | x | y | z | s ₁ | s ₂ | s ₃ | s ₄ | RHS | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 1 | 0 | 2.625 | 0 | 0.25 | 0 | 0 | 1.125 | 38.75 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | 1.75 | 1 | 0.5 | 0 | 0 | -0.25 | 2.5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | 0.25 | 0 | -0.5 | 1 | 0 | 0.25 | 7.5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 0 | 0.75 | 0 | -0.5 | 0 | 1 | -0.25 | 52.5 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 0 | 1 | -0.125 | 0 | -0.25 | 0 | 0 | 0.375 | 6.25 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| 6 | (ii) | (B) <p>Maximum profit of £38.75 manufacturing 6.25 litres of X, none of Y and 2.5 litres of Z.</p> | B1 [1] | 3.2a | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

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| Question | | Answer | | | | | | | | | | | Marks | AOs | Guidance | | | |
|----------|-------|--------|---|-----|-----|-----|-----|-------|-------|-------|-------|-------|-------|-----------------|----------------|-----|---------|--|
| 6 | (iii) | | Q | P | x | y | z | s_1 | s_2 | s_3 | s_4 | s_5 | a_5 | RHS | B1 B1 B1 | 3.3 | Surplus | |
| | | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | -1 | 0 | 5 | | | | |
| | | 0 | 1 | -5 | -2 | -3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | | | |
| | | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | -1 | 1 | 5 | | | | |
| | | 0 | 0 | 2 | 5 | 3 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 20 | | | | |
| | | 0 | 0 | 0 | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 10 | | | | |
| | | 0 | 0 | 2 | 4 | 2 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 70 | | | | |
| | | 0 | 0 | 4 | 3 | 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 30 | | | | |
| | | | | | | | | | | | | | | [3] | | | | |
| 7 | (i) | | Flow is in direction C to D. | | | | | | | | | | | E1 [1] | 3.3 | | | |
| 7 | (ii) | (A) | SA+ SB is the total flow leaving S This line maximises the total flow in the network, so finds the capacity. | | | | | | | | | | | E1 E1 [2] | 1.2 3.3 | | | |
| | | (B) | SA + BA is the flow into vertex A. AD + AC is the flow out of vertex A This line achieves: flow into A = flow out of A | | | | | | | | | | | E1 [2] | 1.1 3.3 | | | |
| | | (C) | This constrains the flow from C to T to be not greater than its capacity of 2. | | | | | | | | | | | E1 [1] | 2.5 | | | |

| Question | Answer | Marks | AOs | Guidance | |
|-----------------|---|-------|-----|----------|--|
| 7 (iii) (A) |  <p>Online LP Solver</p> | B1 | 3.4 | | |

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| | | | <p>Spreadsheet LP Solver</p> | <p>B1 [2]</p> | <p>3.4</p> | | |
| 7 | (iii) | (B) | The maximum capacity of the network is 6. | <p>B1 [1]</p> | <p>3.2a</p> | | |
| 7 | (iv) | | {S, A} {B, C, D, T} | <p>B1 [1]</p> | <p>3.4</p> | | |
| 7 | (v) | | AB and CT can be shut with flow as online solver Also BD can be shut – increase BC, CD, DT by 1 | <p>B1 B1 [2]</p> | <p>3.1b 3.2a</p> | <p>Any 2 shut All three shut</p> | |

| Question | AO1 | AO2 | AO3(PS) | AO3(M) | Totals |
|---------------|-----|-----|---------|--------|--------|
| 1i | 1 | 0 | 0 | 0 | 1 |
| 1ii | 2 | 0 | 0 | 0 | 2 |
| 1iii | 1 | 0 | 0 | 0 | 1 |
| 1iv | 1 | 1 | 1 | 0 | 3 |
| 2 | 4 | 0 | 0 | 0 | 4 |
| 3i | 3 | 0 | 0 | 0 | 3 |
| 3ii | 0 | 1 | 0 | 1 | 2 |
| 3iii | 0 | 0 | 0 | 1 | 1 |
| 4i | 2 | 0 | 0 | 0 | 2 |
| 4ii | 1 | 3 | 0 | 0 | 4 |
| 4iii | 1 | 1 | 0 | 0 | 2 |
| 5i | 3 | 0 | 0 | 0 | 3 |
| 5ii | 0 | 1 | 0 | 0 | 1 |
| 5iiiA | 1 | 0 | 0 | 0 | 1 |
| 5iiiB | 1 | 0 | 0 | 0 | 1 |
| 5ivA | 1 | 0 | 0 | 0 | 1 |
| 5ivB | 1 | 0 | 0 | 0 | 1 |
| 5ivC | 1 | 0 | 0 | 0 | 1 |
| 5v | 0 | 2 | 0 | 0 | 2 |
| 5vi | 0 | 2 | 1 | 0 | 3 |
| 6i | 1 | 0 | 0 | 2 | 3 |
| 6iiA | 1 | 0 | 0 | 1 | 2 |
| 6iiB | 0 | 0 | 1 | 0 | 1 |
| 6iii | 1 | 0 | 0 | 2 | 3 |
| 7i | 0 | 0 | 0 | 1 | 1 |
| 7ii | 2 | 1 | 0 | 2 | 5 |
| 7iiiA | 0 | 0 | 0 | 2 | 2 |
| 7iiiB | 0 | 0 | 1 | 0 | 1 |
| 7iv | 0 | 0 | 0 | 1 | 1 |
| 7v | 0 | 0 | 2 | 0 | 2 |
| Totals | 29 | 12 | 6 | 13 | 60 |

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