



GCE

Further Mathematics B (MEI)

Y411/01: Mechanics A

Advanced Subsidiary GCE

Mark Scheme for Autumn 2021

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Text Instructions

1. Annotations and abbreviations

Annotation in scoris	Meaning
✓ and ✖	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
E	Explanation mark 1
SC	Special case
^	Omission sign
MR	Misread
BP	Blank page
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *. The * may be omitted if only previous M mark.
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This indicates that the instruction In this question you must show detailed reasoning appears in the question.

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2. Subject-specific Marking Instructions for AS/A Level Further Mathematics B (MEI)

- a a Annotations must be used during your marking. For a response awarded zero (or full) marks a single appropriate annotation (cross, tick, M0 or ^) is sufficient, but not required.

For responses that are not awarded either 0 or full marks, you must make it clear how you have arrived at the mark you have awarded and all responses must have enough annotation for a reviewer to decide if the mark awarded is correct without having to mark it independently.

It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

Award NR (No Response)

- if there is nothing written at all in the answer space and no attempt elsewhere in the script
- OR if there is a comment which does not in any way relate to the question (e.g. 'can't do', 'don't know')
- OR if there is a mark (e.g. a dash, a question mark, a picture) which isn't an attempt at the question.

Note: Award 0 marks only for an attempt that earns no credit (including copying out the question).

If a candidate uses the answer space for one question to answer another, for example using the space for 8(b) to answer 8(a), then give benefit of doubt unless it is ambiguous for which part it is intended.

- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not always be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner. If you are in any doubt whatsoever you should contact your Team Leader.

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- c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A method mark may usually be implied by a correct answer unless the question includes the DR statement, the command words “Determine” or “Show that”, or some other indication that the method must be given explicitly.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation *isw*. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation ‘dep*’ is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case, please escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
- Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be ‘follow through’. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

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- f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.)
We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so.
- When a value is **given** in the paper only accept an answer correct to at least as many significant figures as the given value.
 - When a value is **not given** in the paper accept any answer that agrees with the correct value to **2 s.f.** unless a different level of accuracy has been asked for in the question, or the mark scheme specifies an acceptable range.
NB for Specification A the rubric specifies 3 s.f. as standard, so this statement reads “3 s.f”
- Follow through should be used so that only one mark in any question is lost for each distinct accuracy error.
Candidates using a value of 9.80, 9.81 or 10 for g should usually be penalised for any final accuracy marks which do not agree to the value found with 9.8 which is given in the rubric.
- g Rules for replaced work and multiple attempts:
- If one attempt is clearly indicated as the one to mark, or only one is left uncrossed out, then mark that attempt and ignore the others.
 - If more than one attempt is left not crossed out, then mark the last attempt unless it only repeats part of the first attempt or is substantially less complete.
 - if a candidate crosses out all of their attempts, the assessor should attempt to mark the crossed out answer(s) as above and award marks appropriately.
- h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate’s data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A or B mark in the question. Marks designated as cao may be awarded as long as there are no other errors. If a candidate corrects the misread in a later part, do not continue to follow through. E marks are lost unless, by chance, the given results are established by equivalent working. Note that a miscopy of the candidate’s own working is not a misread but an accuracy error.
- i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers provided that there is nothing in the wording of the question specifying that analytical methods are required such as the bold “In this question you must show detailed reasoning”, or the command words “Show” and “Determine. Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
- j If in any case the scheme operates with considerable unfairness consult your Team Leader.

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Question		Answer	Marks	AOs	Guidance
1	(a)	$[\text{Energy}] = M(\text{LT}^{-1})^2$ or $M \cdot \text{LT}^{-2} \cdot \text{L}$ or ML^2T^{-2}	M1	1.2	Any form acceptable. This mark may be implied by the correct answer.
		$[\text{Specific energy}] = \text{ML}^2\text{T}^{-2} \cdot \text{M}^{-1} = \text{L}^2\text{T}^{-2}$	A1	1.1	
			[2]		
	(b)	$345 \div 4 \div 28.35 \times 40 \times 4184$	M1	1.1	All scale factors present. Allow one slip with \times/\div .
		$\approx 509,000 \text{ J}$	A1	2.2b	
			[2]		

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Question			Answer	Marks	AOs	Guidance
2	(a)	(i)	$\angle OAB = \alpha$ and $\sin(\angle OAB) = \frac{3}{5} = 0.6$	B1	3.1a	AG Need not justify why $\angle OAB = \alpha$. Allow finding angles 53.1° , 36.9°
				[1]		
		(ii)	$\cos \alpha = 0.8$	B1	1.1	
				[1]		
	(b)		Moments about O: $3 \cdot 10 \sin \alpha = 4T_2$	M1	3.3	Taking moments about some point.
			$\Rightarrow T_2 = 4.5$	A1	1.1	
				M1	3.3	Attempt at resolving: one equation sufficient (all terms present, but condone $\sin \leftrightarrow \cos$) Or Taking moments about a different point
			$T_1 \cos \theta = 10 \sin \alpha$ or $T_1 \cos \theta = 6$ or $3T_1 \cos \theta = 4T_2$ $T_1 \sin \theta = 10 \cos \alpha + T_2$ or $T_1 \sin \theta = 8 + T_2$ or $4T_1 \sin \theta = 10(5)$	A1 A1	1.1 1.1	Correct equation involving $T_1 \cos \theta$ Correct equation involving $T_1 \sin \theta$
				M1	1.1	Correct method for finding T_1 or θ (from values of $T_1 \cos \theta$ and $T_1 \sin \theta$) <i>Dependent on previous M1M1</i>
			$\tan \theta = \frac{12.5}{6} \Rightarrow \theta \approx 64.4^\circ$ $T_1 = \sqrt{12.5^2 + 6^2} \approx 13.9$	A1	1.1	cao Both correct
				[7]		

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Question		Answer	Marks	AOs	Guidance
3	(a)	Let the velocities of A and B after the first collision be v_1 and v_2 ms^{-1} to the right.			
		$2v_1 + 3v_2 = 7 \times 2 = 14$	M1	3.3	COLM
		$v_2 - v_1 = 7$	M1	3.3	NELR
		$v_1 = -1.4$	A1	1.1	<i>These two marks can be earned</i>
		$v_2 = 5.6$	A1	1.1	<i>in (b) or (c) or (d)</i>
		So magnitude of impulse of A on B = $3 \times (5.6 - 0) = 16.8$ (Ns)	A1	1.1	Condone -16.8 <i>Award all 5 marks if 16.8 is obtained by correct working, even when the unused velocity is missing (or wrong)</i>
			[5]		
	(b)	KE after – KE before $= \frac{1}{2}(2)(-1.4)^2 + \frac{1}{2}(3)(5.6)^2 - \frac{1}{2}(2)(7)^2 = 0$ as required.	B1	1.1	
			[1]		
	(c)	Let the velocities of B and C after the second collision be w_B and w_C ms^{-1} to the right.			
		$3w_B + 5w_C = 3 \times 5.6 - 5u = 16.8 - 5u$	M1	3.3	Condone using same variables that they might have used in part (a).
		$w_C - w_B = 0.25(5.6 + u)$	M1	3.3	
		$3w_B + 5(w_B + 1.4 + 0.25u) = 16.8 - 5u$	M1	1.1	<i>Dependent on previous M1M1</i>
		$\Rightarrow w_B = 1.225 - 0.78125u$	A1	1.1	AG Must be convincingly reached.
			[4]		
	(d)	For A and B to collide again, $1.225 - 0.78125u < -1.4$	M1	3.1b	Or ' $w_B < -1.4$ '
		$\Rightarrow u > 3.36$	A1cao	2.5	
			[2]		

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Question		Answer	Marks	AOs	Guidance
4	(a)	$\frac{1}{2} \cdot 2 \cdot 3^2 + 40T - 60R = \frac{1}{2} \cdot 2 \cdot 15^2$	M1	3.3	Attempt at WEP: all terms present; allow one slip in coefficients of T and R .
		$\Rightarrow 40T - 60R = 216 \Rightarrow 20T - 30R = 108$	A1	1.1	AG
			[2]		
	(b)	Either $\frac{1}{2} \cdot 2 \cdot 3^2 + 18T - 25R = \frac{1}{2} \cdot 2 \cdot 11^2 \Rightarrow 18T - 25R = 112$ or $\frac{1}{2} \cdot 2 \cdot 11^2 + 22T - 35R = \frac{1}{2} \cdot 2 \cdot 15^2 \Rightarrow 22T - 35R = 104$	M1	3.4	WEP: all terms present; allow one slip in coefficients of T and R .
		$T = 16.5$	A1	1.1	
		$R = 7.4$	A1	1.1	
			[3]		
	(c)	If the particle can move as described from O to C, then T and R must have the values found in part (b).	M1	2.1	Seen or implied.
		But then $\frac{1}{2} \cdot 2 \cdot 11^2 + 6(16.5) - 12(7.4) = 2(9.8) \cdot 10 + E$, where E joules is the kinetic energy of the particle at B.	M1	3.4	Attempt at WEP must take into account GPE to find KE at B. This calculation can be done using B and any of O, A and C; the calculation in the MS is based on A.
		$\Rightarrow E = -64.8$ which is not possible.	A1	2.2a	Explicit recognition of a contradiction required.
			[3]		

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Question		Answer	Marks	AOs	Guidance	
5	(a)	Let the caravan have mass m kg and the driving force on the car have magnitude D N.				
		No acceleration, so $D = (1600 + m)g \sin 4.7^\circ$.	M1	3.3		
		$120000 = (1600 + m)g \sin 4.7^\circ \times 32$	M1	3.4	Power = force \times velocity	
		$\Rightarrow m \approx 3070$	A1	1.1		
		[3]				
	(b)	Let the speed of the car at B be v ms ⁻¹ .				
		Total work done by engine = $80000 \times 3.54 (= 283200)$ J	B1	1.1	Need not be seen separately.	
		Gain in GPE = $1600 \times 9.8 \sin 4.7^\circ \times 80 (\approx 102784)$ J	B1	1.1	Need not be seen separately.	
		$\frac{1}{2} \cdot 1600 \cdot 20^2 + 283200 = \frac{1}{2} \cdot 1600 \cdot v^2 + 102784$	M1	3.3	WEP: all terms present; condone one sign error / term on wrong side.	
		$\Rightarrow v \approx 25.0$	A1	1.1	Accept 25	25.0104...
		[4]				
(c)	Resistance forces could be taken into account.	B1	3.5c			
		[1]				

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Question		Answer	Marks	AOs	Guidance
6	(a)	If the box and trolley were not to slide, both would have to have an acceleration of $\frac{50}{16} = 3.125 \text{ ms}^{-2}$.	M1	1.1	Enough to see 3.125 to award this mark.
		So the frictional force of the trolley on the block would have to be 15.625 N.	M1	1.1	Enough to see 15.625 to award this mark.
		But the maximum friction force on the block = $5g \times 0.3 = 14.7 \text{ N}$ which is not enough, so the block will slide.	A1	2.2a	AG Only award this mark if some sort of argument is conveyed as well as seeing 14.7 or 2.94
			[3]		
	(b)	Let the accelerations be a_B and $a_T \text{ ms}^{-2}$.			
	(i)	Box: $14.7 = 5a_B \Rightarrow a_B = 2.94$	B1	1.1	
			[1]		
	(ii)	Trolley: $50 - 14.7 = 11a_T \Rightarrow a_T \approx 3.21$	B1	1.1	
			[1]		
	(c)	At the point of sliding, assuming toppling has not yet occurred, let the force of the obstruction on the block have magnitude $S \text{ N}$.			
	$S = 14.7$	B1	3.4		
	At the point of toppling, assuming sliding has not yet occurred, let the force of the obstruction on the block have magnitude $T \text{ N}$.				
	Moments about bottom left corner: $91T = 28 \cdot 5g$	M1	1.1		
	$\Rightarrow T \approx 15.1$	A1	1.1		
	$S < T$ so the block will slide.	A1	2.4	Conclusion must be stated clearly in words.	
		[4]			

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Question		Answer	Marks	AOs	Guidance	
7	(a)	Centre of mass lies at $(\frac{1}{3}(0+20+100), \frac{1}{3}(0+60+0))$	M1	1.2	One coordinate sufficient. May be implied by one correct answer.	
		$= (40, 20)$	A1	1.1		
			[2]			
	(b)	Let the COM lie at $(\bar{x}, \bar{y}, \bar{z})$.				
		$5000\bar{x} = 3000 \times 40 + 1000 \times 70 + 1000 \times 28$	M1	3.1b	Might be seen embedded in a vector equation with \bar{y} and \bar{z} . Award if all terms present and at most one error in areas and at most one error in x -coordinates 40 (ft), 28, 70	
$\bar{x} = 43.6$		A1	1.1	AG		
$5000\bar{y} = 3000 \times 20 + 1000 \times 0 + 1000 \times 54$		M1	1.1	Allow one error in y -coordinates 20 (ft), 54, 0		
$5000\bar{z} = 3000 \times 0 + 1000 \times (-25) + 1000 \times (-25)$		M1	1.1	Allow one error in z -coordinates 0, -25 (but -50 is M0)		
	$\bar{y} = 22.8, \bar{z} = -10$	A1	1.1	cao		
		[5]				
(c)	Line joining $(20, 60)$ to $(60, 0)$ has equation $y = -\frac{3}{2}x + 90$.	M1	3.1b	Or Line joining $(36, 48)$ to $(80, 0)$ is $y = -(12/11)x + (960/11)$		
	$-\frac{3}{2}(43.6) + 90 = 24.6$	M1	1.1	Finding one critical value (24.6 or $2184/55 \approx 39.71$)		
	$\bar{y} = 22.8 < 24.6$, so COM lies outside the base region \Rightarrow it will topple.	A1ft	2.2a	Follow through their value of \bar{y} provided $0 < \bar{y} < 42.3$ $0 < \bar{y} < 24.6 \Rightarrow$ unstable $24.6 < \bar{y} < 39.71 \Rightarrow$ stable $39.71 < \bar{y} < 42.3 \Rightarrow$ unstable		
		[3]		\bar{y} must be compared with the correct relevant critical value(s)		

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