

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel**  
International  
Advanced Level

Centre Number

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Candidate Number

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**Thursday 14 January 2021**

Morning (Time: 1 hour 30 minutes)

Paper Reference **WMA13/01**

**Mathematics**  
International Advanced Level  
Pure Mathematics P3

**You must have:**

Mathematical Formulae and Statistical Tables (Lilac), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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1. Find

$$\int \frac{x^2 - 5}{2x^3} dx \quad x > 0$$

giving your answer in simplest form.

(3)

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2.

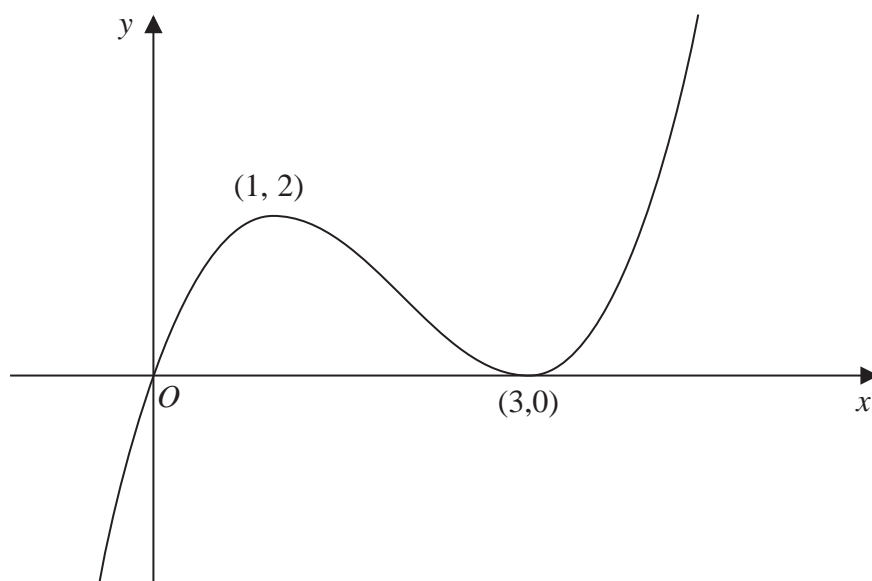
**Figure 1**

Figure 1 shows a sketch of the curve with equation  $y = f(x)$ , where  $x \in \mathbb{R}$  and  $f(x)$  is a polynomial.

The curve passes through the origin and touches the  $x$ -axis at the point  $(3, 0)$

There is a maximum turning point at  $(1, 2)$  and a minimum turning point at  $(3, 0)$

On separate diagrams, sketch the curve with equation

(i)  $y = 3f(2x)$  **(3)**

(ii)  $y = f(-x) - 1$  **(3)**

On each sketch, show clearly the coordinates of

- the point where the curve crosses the  $y$ -axis
- any maximum or minimum turning points



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**Question 2 continued**

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Q2

(Total 6 marks)













4.

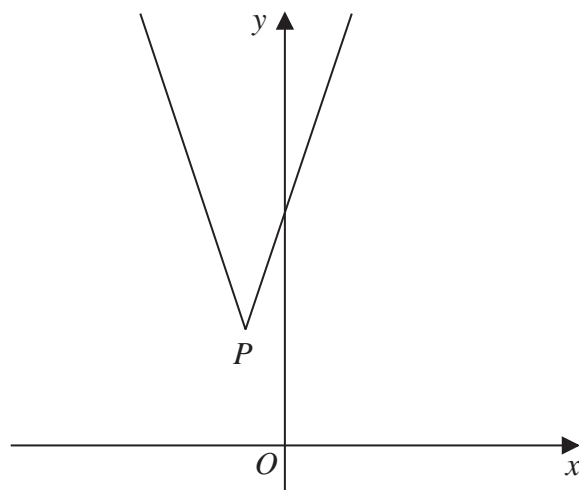


Figure 2

Figure 2 shows a sketch of the graph with equation  $y = f(x)$ , where

$$f(x) = |3x + a| + a$$

and where  $a$  is a positive constant.

The graph has a vertex at the point  $P$ , as shown in Figure 2.

(a) Find, in terms of  $a$ , the coordinates of  $P$ . (2)

(b) Sketch the graph with equation  $y = g(x)$ , where

$$g(x) = |x + 5a|$$

On your sketch, show the coordinates, in terms of  $a$ , of each point where the graph cuts or meets the coordinate axes. (2)

The graph with equation  $y = g(x)$  intersects the graph with equation  $y = f(x)$  at two points.

(c) Find, in terms of  $a$ , the coordinates of the two points. (5)

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### Question 4 continued

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Q4

(Total 9 marks)



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5. The temperature,  $\theta^\circ\text{C}$ , inside an oven,  $t$  minutes after the oven is switched on, is given by

$$\theta = A - 180e^{-kt}$$

where  $A$  and  $k$  are positive constants.

Given that the temperature inside the oven is initially  $18^\circ\text{C}$ ,

- (a) find the value of  $A$ .

(2)

The temperature inside the oven, 5 minutes after the oven is switched on, is  $90^\circ\text{C}$ .

- (b) Show that  $k = p \ln q$  where  $p$  and  $q$  are rational numbers to be found.

(4)

Hence find

- (c) the temperature inside the oven 9 minutes after the oven is switched on, giving your answer to 3 significant figures,

(2)

- (d) the rate of increase of the temperature inside the oven 9 minutes after the oven is switched on. Give your answer in  $^\circ\text{C min}^{-1}$  to 3 significant figures.

(3)

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**Question 7 continued**

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Q7

**(Total 9 marks)**



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8. The percentage,  $P$ , of the population of a small country who have access to the internet, is modelled by the equation

$$P = ab^t$$

where  $a$  and  $b$  are constants and  $t$  is the number of years after the start of 2005

Using the data for the years between the start of 2005 and the start of 2010, a graph is plotted of  $\log_{10} P$  against  $t$ .

The points are found to lie approximately on a straight line with gradient 0.09 and intercept 0.68 on the  $\log_{10} P$  axis.

- (a) Find, according to the model, the value of  $a$  and the value of  $b$ , giving your answers to 2 decimal places. (4)
  
- (b) In the context of the model, give a practical interpretation of the constant  $a$ . (1)
  
- (c) Use the model to estimate the percentage of the population who had access to the internet at the start of 2015 (2)

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**Question 8 continued**

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**(Total 7 marks)**

**Q8**



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9. Find

$$(i) \int \frac{3x - 2}{3x^2 - 4x + 5} dx \quad (2)$$

$$(ii) \int \frac{e^{2x}}{(e^{2x} - 1)^3} dx \quad x \neq 0 \quad (2)$$

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10. The curve  $C$  has equation

$$x = 3\sec^2 2y \quad x > 3 \quad 0 < y < \frac{\pi}{4}$$

(a) Find  $\frac{dx}{dy}$  in terms of  $y$ .

(2)

(b) Hence show that

$$\frac{dy}{dx} = \frac{p}{qx\sqrt{x-3}}$$

where  $p$  is irrational and  $q$  is an integer, stating the values of  $p$  and  $q$ .

(3)

(c) Find the equation of the normal to  $C$  at the point where  $y = \frac{\pi}{12}$ , giving your answer in the form  $y = mx + c$ , giving  $m$  and  $c$  as exact irrational numbers.

(5)

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