Please check the examination deta	ils below b	efore entering yo	our candidate information
Candidate surname		Othe	er names
Pearson Edexcel International Advanced Level	Centre I	Number	Candidate Number
Wednesday 1	00	ctobe	er 2018
Morning (Time: 2 hours 30 minut	es)	Paper Refere	nce WMA01/01
Core Mathemat Advanced Subsidiary	tics (C12	
You must have: Mathematical Formulae and Star	tistical Ta	bles (Blue)	Total Marks

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 125.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶







1. (i) Given that $125\sqrt{5} = 5^a$, find the value of a.

(2)

(ii) Show that $\frac{16}{4 - \sqrt{8}} = 8 + 4\sqrt{2}$

You must show all stages of your working.

		?		
i)	5	-	175	<u> </u>
-			100	

(3)

:. 53 x 51/2 = 5 7/2

$$64 + 16\sqrt{8} = 64 + 16\sqrt{8}$$
 $16 - 8 = 8$



2. Use algebra to solve the simultaneous equations

$$x + y = 5$$
$$x^2 + x + y^2 = 51$$

You must show all stages of your working.

(7)

$$x^{2} + x + (5-x)^{2} = 51$$

$$= x^{2} + x + 25 - |0x + x^{2} = 5|$$

$$\chi = -2$$
 or $\frac{13}{2}$

$$y=7$$
 or -3

:. When
$$\chi = -2$$

when
$$x = \frac{13}{2}$$

$$y = -\frac{3}{2}$$

- 3. Given that $y = 2x^3 \frac{5}{3x^2} + 7$, $x \ne 0$, find in its simplest form
 - (a) $\frac{dy}{dx}$,

(3)

(b) $\int y \, dx$.

(4)

 $(9) \frac{dy}{dx} = 6x^2 + 10$

(b) fydr

$$= \int 2x^3 - 5 + 7$$

$$3x^2$$

$$=\frac{2x^{4}-5x^{-1}}{4}+7x+c$$

$$= \frac{1}{2} x^{4} + \frac{5}{3} x^{-1} + 7x + c.$$



4. A sequence of numbers $u_1, u_2, u_3,...$ satisfies

$$u_n = kn - 3^n$$

where k is a constant.

Given that $u_2 = u_4$

- (a) find the value of k
 - (3)
- (b) evaluate $\sum_{r=1}^{4} u_r$

(3)

(a)
$$4, = k - 3$$

 $= k - 3$.
 $= k - 3$.

$$U_2 = 2K - 3^2$$
 (4(36) - 81)

$$= 2K - 9 = 240$$

$$4K-81 = 2K-9$$



5. (a) Find the first 4 terms, in ascending powers of x, of the binomial expansion of

$$\left(1-\frac{1}{2}x\right)^{10}$$

giving each term in its simplest form.

(4)

(b) Hence find the coefficient of x^3 in the expansion of

$$(3+5x-2x^2)\left(1-\frac{1}{2}x\right)^{10}$$
 (2)

(a)
$$\binom{10}{0}\binom{1}{1}\binom{10}{2}\binom{-1}{2}\binom{1}{1}\binom{-1}{2}\binom{1}{2}\binom{-1}{2}\binom{1}{2}\binom{-1}{2}\binom{1}{2}\binom{1}{2}\binom{1}{2}\binom{1}{2}\binom{1}{2}$$

$$=1-5x+45x^2-15x^3$$
...

(b)
$$(3+5x-2x^2)$$
 $(1-5x+45x^2-15x^3)$

$$-2x^2 x - 5x = 10n^3$$

$$3x - 15x^3 = -45x^3$$

$$\frac{10 + 225 - 45 = 85}{4}$$

6. (a) Sketch the graph of
$$y = \left(\frac{1}{2}\right)^v$$
, $x \in \mathbb{R}$, showing the coordinates of the point at which the graph crosses the *y*-axis.

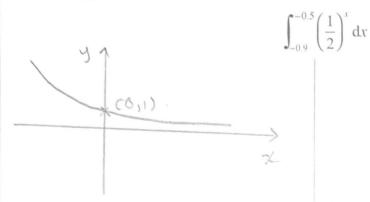
(2)

The table below gives corresponding values of x and y, for $y = \left(\frac{1}{2}\right)^x$

The values of y are rounded to 3 decimal places.

х	-0.9	-0.8	-0.7	-0.6	-0.5
У	1.866	1.741	1.625	1.516	1,414

(b) Use the trapezium rule with all the values of y from the table to find an approximate value for



(3)

(b)
$$h \Rightarrow -0.8 - -0.9 = 0.1$$

 $1 \times 0.1 \times [1.866 + 1.414 + 2(1.741 + 1.625 + 1.516)]$
 $= 0.652 (35f)$



14



7. The point A has coordinates (-1, 5) and the point B has coordinates (4, 1).

The line l passes through the points A and B.

(a) Find the gradient of l.

(2)

(b) Find an equation for l, giving your answer in the form ax + by + c = 0 where a, b and c are integers.

(2)

The point M is the midpoint of AB.

The point C has coordinates (5, k) where k is a constant.

Given that the distance from M to C is $\sqrt{13}$

(c) find the exact possible values of the constant k.

(a) (-1,5) (4,1)	(c) Finding M
$\frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 5}{4 + 1} = \frac{-4}{5}$	-1+4 = 3 5+1 = 3. 2 2
(b) y=mx+c.	i. M=> (1.5,3).
y=-4x+c at (-1,5)	(5,16) (1-5,3)
5=4+6	$\sqrt{(5-1.5)^2+(k-3)^2} = \sqrt{(3)^2}$
C = 21	$\frac{49}{4} + (k-3)^2 = 13$
$y = -\frac{4}{5}x + \frac{21}{5}$	$(K-3)^2 = \frac{3}{4}$
5y + 4x-21 =0.	L-3 = 1 <u>\(\frac{1}{3} \)</u>
	$k = 3 + \frac{\sqrt{3}}{2}$

where p and q are constants.

When f(x) is divided by (x - 1), the remainder is -6

(a) Use the remainder theorem to show that
$$p + q = -5$$

(2)

Given also that (x + 2) is a factor of f(x),

(b) find the value of p and the value of q.

(3)

(c) Factorise f(x) completely.

8.f(1)=-6.	(c) (a+2) (ax2+bx+c)
2(1)3-3(1)2+p(1)+9=-6.	$= 2x^3 - 3x^2 - 11x + 6$.
2-3+p+9=-6	2 C = 6 C = 3
p+q=-5 as req.	$9x^{3}=2x^{3}$ $q=2$
(b) $f(-2) = 0$	29x2+bx2=-3.
$2(-2)^{3} - 3(-2)^{2} + p(-2) + q = 0$ $-16 - 12 - 2p + q = 0$	4+b=-3 b=-7.
-2p+q=28.	: another factor = 2x2-7x+3-
p+9=-5	Factorising 2x2-7x+3
-3p = 33	$\Rightarrow (2x-1)(x-3)$
£=-11	f(x) = (x+2)(2x-1)(x-3)
9 = -5 + 11	

9. A car manufacturer currently makes 1000 cars each week.

The manufacturer plans to increase the number of cars it makes each week.

The number of cars made will be increased by 20 each week from 1000 in week 1, to 1020 in week 2, to 1040 in week 3 and so on, until 1500 cars are made in week N.

(a) Find the value of N.

(2)

The car manufacturer then plans to continue to make 1500 cars each week.

(b) Find the total number of cars that will be made in the first 50 weeks starting from and including week 1.

(5)

$$a = 1006$$

(b) Week 1-> 26.

$$\frac{26}{2} \left[2 (1000) + 20 (26-1) \right]$$
= 32500

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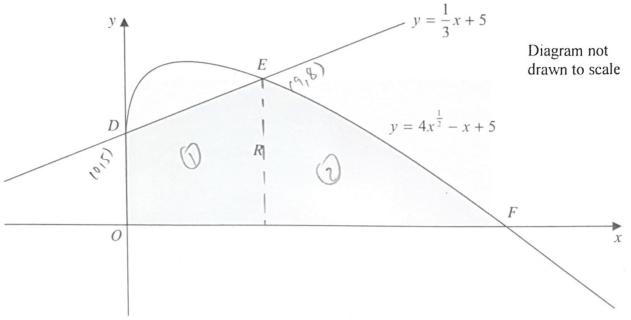


Figure 1

The finite region R, which is shown shaded in Figure 1, is bounded by the coordinate axes, the straight line l with equation $y = \frac{1}{3}x + 5$ and the curve C with equation $y = 4x^{\frac{1}{2}} - x + 5$, $x \ge 0$

The line l meets the curve C at the point D on the y-axis and at the point E, as shown in Figure 1.

(a) Use algebra to find the coordinates of the points D and E. (4)

The curve C crosses the x-axis at the point F.

(b) Verify that the x coordinate of F is 25 (1)

(c) Use algebraic integration to find the exact area of the shaded region R.

 $4x^{1/2} - x + 8 = 1x + 5.$ $4x^{1/2} = 4x.$ x(x-9) = 0 x = 0 x = 0 x = 0 y = 5 when x = 0 y = 8 when x = 9. $x = 1x^{2}.$

Question of continued	
(b) X int y=0.	208 + 117 3 Z
$4x^{1/2} - x + 5 = 0$ when $x = 25$	= 767 6:
4(25) -(25) +5	6
= 0	
X co-ordinate of F=25	
(c) <u>D</u>	
1 × 9 × (8+5)	
= 117	
25	
$\int_{Q} 4x^{1/2} - x + 5 dx$	
$\begin{bmatrix} 4\chi^{3/2} & -\chi^2 + 5\chi \end{bmatrix}$	
875 - 153	
= <u>208</u>	



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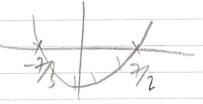
- 11. The equation $7x^2 + 2kx + k^2 = k + 7$, where k is a constant, has two distinct real roots.
 - (a) Show that k satisfies the inequality

$$6k^2 - 7k - 49 < 0 (4)$$

(b) Find the range of possible values for k.

7x2 +2kx +k2-k-7=0.	
	· -7(KC7/2
b2-49c>0.	/3

$$k = \frac{7}{3} \quad k = \frac{7}{2}$$



12. (a) Show that the equation

$$6\cos x - 5\tan x = 0$$

may be expressed in the form

$$6\sin^2 x + 5\sin x - 6 = 0$$

(3)

(b) Hence solve for $0 \le \theta < 360^{\circ}$

$$6\cos(2\theta - 10^{\circ}) - 5\tan(2\theta - 10^{\circ}) = 0$$

giving your answers to one decimal place.

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(5)

605x - 5510x =0.	:. Sin(20-10)=2/3.
6052x -55/10x=0	20-10 = 41.8, 138.2, 40 498.2
6(1-8in2x)-58inx=0.	20=51.8,148.2,411.8
$6-6\sin^2 x-5\sin x=0$	0=25.9,74.1,205.9
651/x+581/x-6=0. 95 req.	254.1
(b) let x=20-10°.	
-5+ \52-4(6)(-6) 2+6.	
$\sin n = -3/2$ $\sin n = 2/3$. of in range	

13. (i) Find the value of x for which

$$4^{3x+2} = 3^{600}$$

giving your answer to 4 significant figures.

(3)

(ii) Given that

$$\log_a (3b-2) - 2\log_a 5 = 4,$$
 $a > 0, a \ne 1, b > \frac{2}{3}$

find an expression for b in terms of a.

(ii)
$$\log \left(\frac{3b-2}{5^2}\right) = 4.$$

$$9^{4} = 3b-2$$
 25

$$\frac{2594+2}{3} = 6$$

14. The circle *C* has equation

$$x^2 + y^2 + 16y + k = 0$$

where k is a constant.

(a) Find the coordinates of the centre of C.

(2)

Given that the radius of C is 10

(b) find the value of k.

(2)

The point A(a, -16), where a > 0, lies on the circle C. The tangent to C at the point A crosses the x-axis at the point D and crosses the y-axis at the point E.

(c) Find the exact area of triangle ODE.

(7)

(2+0) 2 + (y+8) -82+K=	s Grad of line (6,-16) (6,-8)
$(x+0)^{2} + (y+8)^{2} = 64-k$	$\frac{-8+16}{0-6} = \frac{8}{-6} = \frac{-4}{3}$
centre = (o, -8)	: Grad of + line = 3.
(b) Radius => 10.	
$\sqrt{64-16} = 10$	$y-y_0=m(n-x_0).$
64-k=100 $k=-36$	$y+16=\frac{3}{4}(x-6)$

 $(C)_{q^2 + (-16)^2 + 16(-16) - 36 = 0} = 2 = 8\frac{2}{3} \qquad (8\frac{2}{3}, 0)$

a2 = 36. Yint

 $\gamma = 6$ (0, -4/2)

1 × 4) × 82 - 168

15.

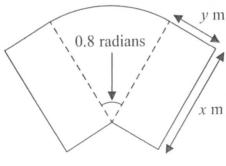


Figure 2

Figure 2 shows a plan for a garden.

The garden consists of two identical rectangles of width y m and length x m, joined to a sector of a circle with radius x m and angle 0.8 radians, as shown in Figure 2.

The area of the garden is 60 m².

(a) Show that the perimeter, P m, of the garden is given by

$$P = 2x + \frac{120}{x}$$
 (5)

(b) Use calculus to find the exact minimum value for P, giving your answer in the form $a\sqrt{b}$, where a and b are integers.

(4)

(c) Justify that the value of P found in part (b) is the minimum.

(2)

(a) Area yx +yx + [1 x n2 x 0.6]	Perimeter
yx +yx + [1 x * 400]	2(x+y+y)+ x(0.8)
2yx+0.4x2 =60.	2x+4/30 -0.2x)+0.8x.
24x = 60 - 0.4x2	1 x + 120 - 0 - 8 x + 0 . 8 x
y=1(60-0.4x2)	2x+120 - 0-8x+0;8x
y = 30 - 0.2x.	P=2x+128 as reg.
<i>γ</i> .	*

Question 15 continued

(b)	dP	 2 -	-120
	dx		K 2

$$2 = 120$$

$$(c) \frac{d^2p}{dx^2} = \frac{240}{x^3}$$

$$\frac{d^2\rho}{dn^2} > 0$$
 : min value of x found.



- 16. The first three terms of a geometric series are (k + 5), k and (2k 24) respectively, where k is a constant.
 - (a) Show that $k^2 14k 120 = 0$

(3)

(b) Hence find the possible values of k.

(2)

- (c) Given that the series is convergent, find
 - (i) the common ratio.
 - (ii) the sum to infinity.

	(4)
a= k+3.	(c) since series is convergent
$qr = k$ $qr^2 - (2k - 24)$	¥=20.
$\frac{(2k-24)}{k} = \frac{(c)}{k+s}$	20+5= a=25
	$r = \frac{20}{25} = \frac{4}{5}$
(K+5) (2K-24) = K2.	
2 (Kts) (K-12) = k2.	SD = 9 = 25 = 1-V 1-06
2[K2-12Kf5K-60]=K	= 125
$2[\kappa^2 - 7k - 60] = k^2$	
$2k^2 - 14k - 120 - k^2 = 0$	
$\kappa^2 - 14\kappa - 120 = 0$ as,	req.
(b) 14 + \(\sigma 14^2 - 4(-120)\)	
2 * 1	
x = -6 or 20.	