M2 Specimen (IAL) MA
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1. A particle
$$P$$
 moves on the x -axis. The acceleration of P at time t seconds, $t \ge 0$, is $(3t + 5)$ m s⁻² in the positive x -direction. When $t = 0$, the velocity of P is 2 m s⁻¹ in the positive x -direction. When $t = T$, the velocity of P is 6 m s⁻¹ in the positive x -direction. Find the value of T .

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(6)

$$\Rightarrow Vel = \int 3t + 5 dt = 3t^2 + 5t + C$$

$$\Rightarrow \text{ Vel} = \int 3t + 5 dt = \frac{3t^2 + 5t + C}{2}$$

 $V=2,t=0 \Rightarrow C=2 \Rightarrow \text{ Vel} = \frac{3t^2 + 5t + 2}{2}$

$$\Rightarrow Vel = \int 3t + 5 dt = \frac{3t^2}{2} + 5t + C$$

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$$V=2,t=0$$
 =) $C=2$ \Rightarrow $Vel = 3t^2 + 5t + 2$

When V=6 => 6=3+2+St+2 => 3t2+10t-8=0

(3t-2)(t+4)=0 => t=== sec

- A particle P of mass 0.6 kg is released from rest and slides down a line of greatest slope of a rough plane. The plane is inclined at 30 to the horizontal. When P has moved 12 m, its speed is 4 m s⁻¹. Given that friction is the only non-gravitational resistive force acting on P, find
- (a) the work done against friction as the speed of P increases from 0 m s^{-1} to 4 m s^{-1} ,
 - (b) the coefficient of friction between the particle and the plane. (4) N=0 V=4 S=12 $V^2=U^2+2aS$
 - 16 = 2a(12) a=2
- Rf 0.3g-fmax = 0.6x= =) fmax = 0.3g-0.4 (ud against fraction = $(0.3g-0.4)\times12 = 30.55$ (3sf)
- 0.39-0.4=M(0.359) max = unr

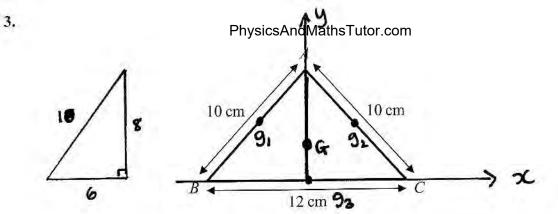


Figure 1

A triangular frame is formed by cutting a uniform rod into 3 pieces which are then joined to form a triangle ABC, where AB = AC = 10 cm and BC = 12 cm, as shown in Figure 1.

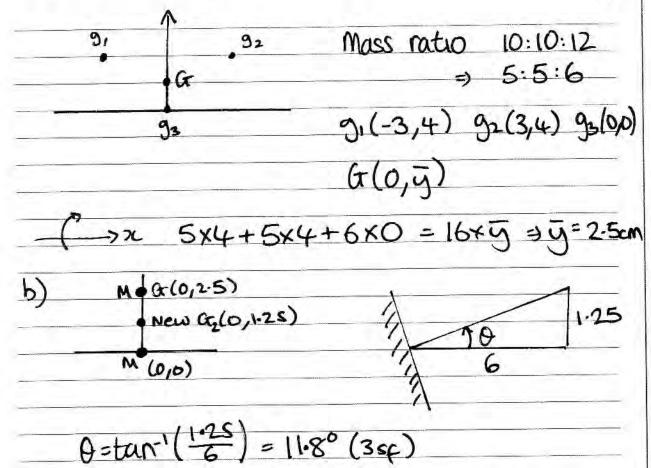
(a) Find the distance of the centre of mass of the frame from BC.

The frame has total mass M. A particle of mass M is attached to the frame at the mid-point of BC. The frame is then freely suspended from B and hangs in equilibrium.

(5)

(4)

(b) Find the size of the angle between BC and the vertical.



- A car of mass 750 kg is moving up a straight road inclined at an angle θ to the horizontal, PhysicsAndMathsTutor.com where $\sin \theta = \frac{1}{15}$. The resistance to motion of the car from non-gravitational forces has constant magnitude R newtons. The power developed by the car's engine is 15 kW and the car is moving at a constant speed of 20 m s⁻¹.
- (a) Show that R = 260.

The power developed by the car's engine is now increased to 18 kW. The magnitude of the resistance to motion from non-gravitational forces remains at 260 N. At the instant when the car is moving up the road at 20 m s⁻¹ the car's acceleration is a m s⁻².

(4)

(b) Find the value of a.

(4)

$$RF = 0 \Rightarrow 7SO = 50g + R \Rightarrow R = 260N$$

o)
$$P = 18kW$$
 $\frac{18000}{20} - 260 - Sog = 750a$ $\alpha = \pm ms$

Find (a) the magnitude of the impulse of the bat on the ball,

a)

(3)

a) Mom before =
$$\frac{1}{2}(10i+24j) = 5i+12j$$

Mom after = $\frac{1}{2}(20i+0j) = 10i$
Impulse = change in momentum = $5i-12j$
Impulse = $\sqrt{5^2+12^2} = 13ns$

b)
$$\frac{5}{12}$$
 $\theta = \tan^{-1}(\frac{12}{5}) = 67.4^{\circ}$ below:
c) Vel before = $\sqrt{10^2 + 24^2} = 26$ mc⁻¹

c) Vel before =
$$\sqrt{10^2 + 24^2} = 26 \text{ ms}^{-1}$$

Vel after = 20 ms^{-1}
 $| \text{OSS in K.E.} = \frac{1}{2} \text{m}(v_2^2 - v_1^2) = \frac{1}{2} (\frac{1}{2})(26^2 - 20^2) = 69 \text{J}$

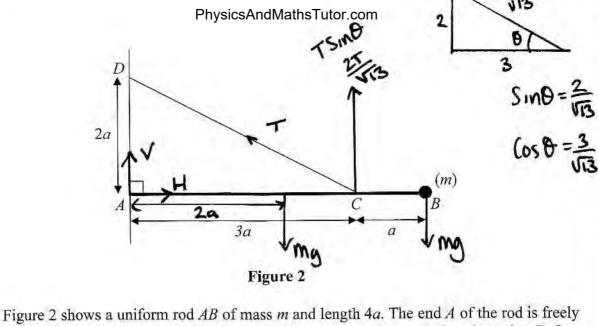


Figure 2 shows a uniform rod AB of mass m and length 4a. The end A of the rod is freely hinged to a point on a vertical wall. A particle of mass m is attached to the rod at B. One end of a light inextensible string is attached to the rod at C, where AC = 3a. The other end of the string is attached to the wall at D, where AD = 2a and D is vertically above A. The rod rests horizontally in equilibrium in a vertical plane perpendicular to the wall and the tension in the string is T.

(a) Show that
$$T = mg\sqrt{13}$$
.

6.

The particle of mass m at B is removed from the rod and replaced by a particle of mass M which is attached to the rod at B. The string breaks if the tension exceeds $2mg\sqrt{13}$. Given that the string does not break,

(5)

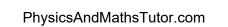
(3)

(b) show that
$$M \leqslant \frac{5}{2}m$$
.

a)
$$A = \frac{2T}{\sqrt{13}} \times 3\alpha$$

$$6mg = \frac{6T}{\sqrt{13}} \Rightarrow T = \sqrt{13} mg$$

A)
$$m_{g} \times 2\alpha + M_{g} \times 4\alpha \leq 2m_{g} \sqrt{r_{g}} \times \frac{2}{\sqrt{r_{g}}} \times 3\alpha = 2m_{g} + 4M_{g} \leq 12m_{g}$$



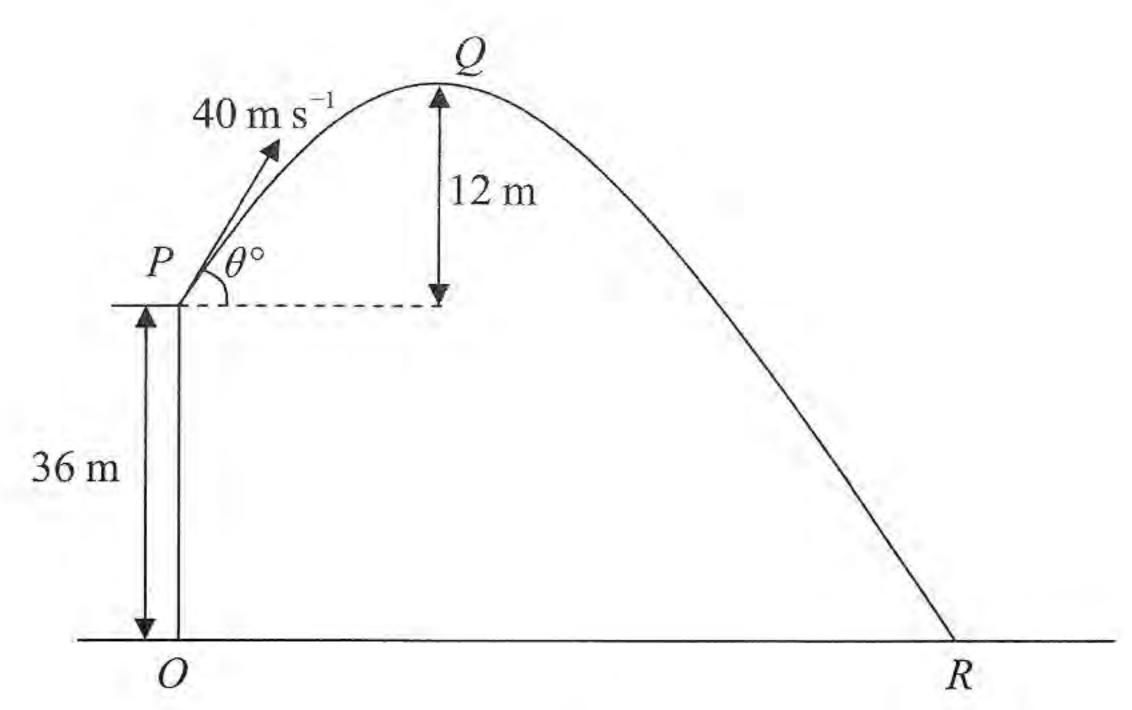


Figure 3

A ball is projected with speed 40 m s^{-1} from a point P on a cliff above horizontal ground. The point O on the ground is vertically below P and OP is 36 m. The ball is projected at an angle θ° to the horizontal. The point Q is the highest point of the path of the ball and is 12 m above the level of P. The ball moves freely under gravity and hits the ground at the point R, as shown in Figure 3. Find

(a) the value of θ ,

(3)

blank

(b) the distance OR,

(6)

(c) the speed of the ball as it hits the ground at R.

a) $u = 40 \sin \theta$ $v^2 = u^2 + 2as = 0 = (40 \sin \theta)^2 - 19.6 \times 12$ 0 = -9.8 0 = 12 $0 = 19.6 \times 12$ $0 = 22.5 \times 1480 \text{ S}$ $0 = 22.5 \times 1480 \text{ S}$

U = 15.336231 $S = ut + \frac{1}{2}at^2 -) -36 = 15.3.t - 496^2$ a = -9.8

S = -36 4.9t2-15.33...t-36=0 t= 4.694.

FP Ve1=40Cos0 = 36.943... dist=Velxtime 0R=173.4m

C) $V^2 = u^2 + 2as$ $V^2 = (40sin 22.54...)^2 - 19.6x-36 = <math>|V| = 30.672...$

V=36.943 Vel=36.943;-30.672; => Speed=48 ms1

- A small ball A of mass 3m is moving with speed u in a straight line on a smooth horizontal table. The ball collides direct Rhysigs And Matha Tultob com of mass m moving with speed u towards A along the same straight line. The coefficient of restitution between A and Bis $\frac{1}{2}$. The balls have the same radius and can be modelled as particles. (a) Find
 - (i) the speed of Λ immediately after the collision,
 - (ii) the speed of B immediately after the collision.
 - After the collision B hits a smooth vertical wall which is perpendicular to the direction of motion of B. The coefficient of restitution between B and the wall is $\frac{2}{5}$.

(7)

(6)

- (b) Find the speed of B immediately after hitting the wall. (2) The first collision between A and B occurred at a distance 4a from the wall. The balls collide again T seconds after the first collision.
- (c) Show that $T = \frac{112a}{15a}$.
- e = V2-V1 = 1 => V2=U+V1
- 3mu-mu = 3mVi +m(u+Vi) => 2mu=3mVi+mu+mVi Mu=49hV1 => V1=44 V2=44= 44
- e= \frac{1}{5} = \frac{2}{5} = \frac{1}{5} \frac{1}{5} \frac{2}{5} \frac{1}{5} \frac{1}{5}
- Vel= &u S=4a 4a= &uxt => t1= 16a
-) Vel= &u t= 169 S= &ux 169 = 49 4a-4a= 6a

So when B hits Aboutes Androduks Tu (Adopted B) are 16 a apant t= 16a speed of approach = 34 u