Please check the examination details below before entering your candidate information				
Candidate surname		Oth	er names	
Pearson Edexcel International Advanced Level	Centre N	lumber	Candida	ate Number
Tuesday 22 Ja	anua	ary 2	019	
Morning (Time: 1 hour 30 minute	es) F	Paper Refere	nce WME0 2	2/01
Mechanics M2 Advanced/Advanced Subsidiary				
Advanced/Advanced 3	ubsidia	ary		

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Whenever a numerical value of g is required, take $g = 9.8 \text{ m s}^{-2}$, and give your answer to either two significant figures or three significant figures.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
- use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶



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Three particles of masses 3m, m and 2m are positioned at the points with coordinates (a, 8), (-4, 0) and (5, -2) respectively.

Given that the centre of mass of the three particles is at the point with coordinates (k, 2k), where k is a constant, find the value of a.

(5)

$$3\eta \left(\frac{9}{8}\right) + \eta \left(\frac{-4}{0}\right) + 2\eta \left(\frac{5}{-2}\right) = 6\eta \left(\frac{1}{2}\right)$$

$$\begin{pmatrix} 3q - 4 + 10 \\ 24 - 4 \end{pmatrix} = 6 \begin{pmatrix} k \\ 2k \end{pmatrix}$$

2. A particle of mass $0.75 \,\text{kg}$ is moving with velocity $(4\mathbf{i} + \mathbf{j}) \,\text{m s}^{-1}$ when it receives an impulse $(-6\mathbf{i} + 4\mathbf{j}) \,\text{N s}$.

Find

(a) the velocity of the particle immediately after receiving the impulse,

(3)

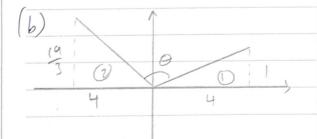
(b) the size of the angle through which the path of the particle is deflected as a result of the impulse.

(3)

0.75 (V- (4) = (-6)	0 = 180 - (4.03 +57.72)
((1)) (4)	

$$v - (4) = (-8)$$

$$... \ V = -4i + 19j$$



3. A car of mass 900 kg is moving on a straight road that is inclined at an angle θ to the horizontal, where $\sin \theta = \frac{1}{49}$. When the car is moving up the road, with the engine of the car working at a constant rate of 10.8 kW, the car has a constant speed of vms^{-1} . The resistance to the motion of the car from non-gravitational forces is modelled as a constant force of magnitude R newtons.

When the car is moving down the road, with the engine of the car working at a constant rate of $10.8 \,\mathrm{kW}$, the car has a constant speed of $2 \,\mathrm{vm\,s^{-1}}$. The resistance to the motion of the car is still modelled as a constant force of magnitude R newtons.

Find

(i) the value of R,

(ii) the value of v.

(8)
scenario 2
0'19
50
V
9009
Power = 10800W.
10800 = 2V X D'
,
D'+900gx1-R=0. R(V)
D' = R - 9009
49.
10800 = 2V × (12 - 900g)
10800=2V× (R-180) 0.
From egn O
V=10800
180+R.

Question 3 continued



blank

4.

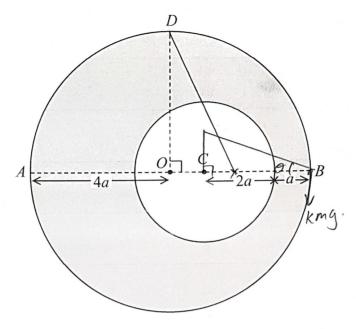


Figure 1

The uniform lamina L, shown shaded in Figure 1, is formed by removing a circular disc of radius 2a from a uniform circular disc of radius 4a. The larger disc has centre O and diameter AB. The radius OD is perpendicular to AB. The smaller disc has centre C, where C is on AB and BC = 3a

(a) Show that the centre of mass of L is
$$\frac{13}{3}a$$
 from B.

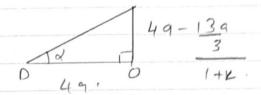
The mass of L is M and a particle of mass kM is attached to L at B. When L, with the particle attached, is freely suspended from point D, it hangs in equilibrium with A higher than B and AB at an angle θ to the horizontal, where $\tan \theta = \frac{3}{4}$

(b) Find the value of k.

(5)

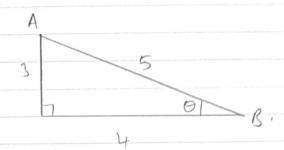
(a) Bigger arcular disc.	Smaller aralar disc.
Areq = 11 (49)2	Area = 11(29)2 = 41192
=161192	COM
(0)	(9)

Question 4 continued



Leave blank

$$\begin{pmatrix} 0 - 49 \\ 0 + 0 \end{pmatrix} = 12 \begin{pmatrix} \bar{\chi} \\ \bar{g} \end{pmatrix}$$



$$49 - 13/39$$
 $-1+k = 3$

$$4 - 13 = 3$$
.

$$\begin{array}{c}
(139) = (1+16)(\tilde{n}) \\
0
\end{array}$$

$$\bar{x} = \frac{13/3}{1+k}$$



5. A particle moves along the *x*-axis. At time *t* seconds, $t \ge 0$, the velocity of the particle is $v \, \text{m} \, \text{s}^{-1}$ in the direction of *x* increasing, where $v = 2t^{\frac{3}{2}} - 6t + 2$

At time t = 0 the particle passes through the origin O. At the instant when the acceleration of the particle is zero, the particle is at the point A.

Find the distance *OA*.

$$a = \frac{dv}{dt} = \frac{3}{2}(2)t^{\frac{1}{2}} - 6$$

$$= 3t^{\frac{1}{2}} - 6$$
(8)

when a=0 $3t^{\frac{1}{2}}-6=0$ $t^{\frac{1}{2}}=\frac{6}{3}$ = 2 t=4

$$S = \int v dt$$

$$= \int 2t^{\frac{3}{2}} - 6t + 2 dt$$

$$= \frac{2t^{\frac{5}{2}}}{\frac{5}{2}} - \frac{6t^{2}}{2} + 2t + c$$

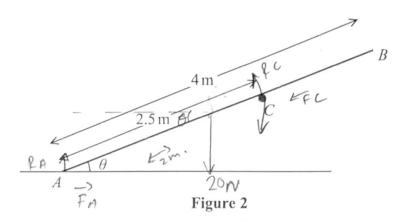
$$= \frac{4}{5}t^{\frac{5}{2}} - 3t^{2} + 2t + c$$

when t=0, S=0 $\frac{4}{5}t^{\frac{5}{2}}-3t^2+2t+C=0$ $\therefore C=0$

when
$$t=4$$
, $S=\frac{4}{5}(4)^{\frac{5}{2}}-3(4)^{2}+2(4)$
= -14.4

distance = 14.4 m

6.



A plank AB rests in equilibrium against a fixed horizontal pole. The plank has length 4 m and weight 20 N and rests on the pole at C, where AC = 2.5 m. The end A of the plank rests on rough horizontal ground and AB makes an angle θ with the ground, as shown in

Figure 2. The coefficient of friction between the plank and the ground is $\frac{1}{4}$.

The plank is modelled as a uniform rod and the pole as a rough horizontal peg that is perpendicular to the vertical plane containing AB.

Given that $\cos \theta = \frac{4}{5}$ and that the friction is limiting at both A and C,

(a) find the magnitude of the normal reaction on the plank at C,

(3)

(b) find the coefficient of friction between the plank and the pole.

(8)

\$ 13 4	(b) Balancing forces
a)M(A)	Pc. (050+ PA=20+. Fc. sino
Pc x2.5 = 200050x2	
	Given &c=12.8 and Fc=4c. RC
PC = 20 X0.8 X2	Sind = 3/5.
2.5	SIND = 3/5.
RC=12.8N	PA = 9.76N + 7-68. PC 0
	1 x PA = 7.68 + 10-24 MC.
	,
	$\frac{1}{4} (9.76 + 7.68, P_C) = 7.68 + 10.24,$

Question 6 continued	Leave blank
2.44 +1.97 1 = 7.68+10.24.1.	
8.32.Pc = 5.24.	
Pc=0.63	
	-
	-
	-
	-
	-
	-

- 7. A particle P of mass 3m is moving in a straight line with speed u on a smooth horizontal table. A second particle Q of mass 2m is moving with speed 2u in the opposite direction to P along the same straight line. Particle P collides directly with Q. The coefficient of restitution between P and Q is e.
 - (a) Show that the direction of motion of P is reversed as a result of the collision with Q.
 - (b) Find the range of values of e for which the direction of motion of Q is also reversed as a result of the collision.

(5)

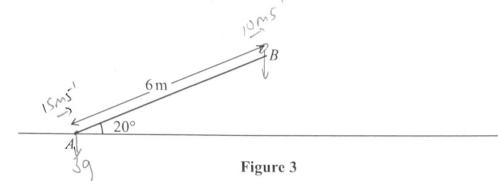
Given that $e = \frac{1}{2}$

(c) find, in terms of m and u, the kinetic energy lost in the collision between P and Q.

(a) P 6 (b) Using Impact Law; (3m) (2m) y+x = e 3u 3u	(a) P @	(b) Using Impact Law,
$\frac{3m}{2} \frac{(2m)}{2u} \frac{y+x}{3u} = e^{-\frac{x}{2}}$		
$\frac{y+x}{2} = e$	(3m) (2m)	
		4+x = e.
	20	30
	<i>→</i> > <i>→</i> >	
2 9' Y+X = Sve.	2 4'	y+x=3ve.
C _x .	Cz .	
Law of conservation of x=3ue-y.	Law of conservation of	x=3ue-y.
hapathhim.		
-u = -3 (3ue - y) + 2y.		-u=-3 (3ue-y)+2y.
SmU - 4mu = Smx +2mu	3mu - 4mu = 3mx +2my	
-U = - 9ve + Sy + 2y.		-v = - que + 3y + 2y.
$-mv = 3m\chi + 2m\mu$.	-mu = 3 mx + 2 my.	
5y= 4ve-u		5y = 9ve - v.
- some the rotal is neoghbor	-> Since the total is negative	
		4=0 (9e-1)
(i) either x 20 and y 20 because x 20, y 0 is not possible.	(i) either x Ld and	5
440	460	
because xco, yso U (9e-1) so.	because x 60, 450	U (9e-1) > 0,
is not possible.	is not possible.	
9 e-150	,	9 e-150
Has chia ha a l D'C	:. the direction of P's	
motion has definetly been e>/g but e <)	motion has definetly been	$e > V_q$ but $e \in I$
motion has definetly been $e > 1/q$ but $e \le 1$ reversed. $e > 1/q$ but $e \le 1$	reversed.	1gLe <1

Question 7 continued	Leave blank
(c) given e= 1/2	
ICE Before	
$\frac{1}{2} \times 3m \times v^2 = \frac{3}{2} m v^2$	
$\frac{1}{2} \times 2m \times (2u)^2 = 4mu^2$	
= 5.5mu²	
LE After	
y= v (4·5-1).	
= 7 v. 16	
·. x = 4 u	
$\frac{1}{2} \times 3m \times (40)^2 = 24mv^2$	
+ 1	
$\frac{1}{2} + \frac{1}{2} \times \frac{1}{16} \times \frac{1}{16} = \frac{49 \text{ mu}^2}{100}$ $\frac{1.45 \text{ mu}^2}{1.45 \text{ mu}^2}$	
5.5mv2-1.45mv2= 4.05mv2	
4.05mv	

8.



A rough ramp AB is fixed to horizontal ground at A. The ramp is inclined at 20° to the ground. The line AB is a line of greatest slope of the ramp and $AB = 6 \,\mathrm{m}$. The point B is at the top of the ramp, as shown in Figure 3. A particle P of mass $3 \,\mathrm{kg}$ is projected with speed $15 \,\mathrm{m \, s^{-1}}$ from A towards B. At the instant P reaches the point B the speed of P is $10 \,\mathrm{m \, s^{-1}}$. The force due to friction is modelled as a constant force of magnitude F newtons.

(a) Use the work-energy principle to find the value of F.

(6)

After leaving the ramp at B, the particle P moves freely under gravity until it hits the horizontal ground at the point C. The speed of P as it hits the ground at C is $w \, \text{m s}^{-1}$.

Find

(b) (i) the value of w,

(5)

(c) the greatest height of P above the ground as P moves from A to C.

(ii) the direction of motion of P as it hits the ground at C,

(4)

(a) Gain in GPE.	(b) 10 cos 20 -> Ux.
	10 gin 20 > Vy.
3g x 6 Sin 20 = 60.33 235328.	0
3	S = -68in20 1 + ve
Loss in KE.	S = -68in20 $V = 10 gin 20$ $V = 7$
$\frac{1}{2} \times 3 \times (15^2 - 10^2)$	9 = -9.8.
2	E=x.
= 1875.	
	v2=v2+2015
187.5-60.33 = FX6	
	V2=(108in20)2+2(-9.8)(-64in2
F=21.19460779.	
=21.2N	v=7.205508081.

Question 8 continued	
10(0520 7.205	
w= \(7.205)2 + (1000520)	
= (1.8ms-1	
tan (7.205.)	
the Horizontal.	
(c) $S = ?$ $V = 10 \% n 20$	
V = 0 9 = -9.8 t = X	
v ² =v ² +795'	
0 = (10 sin20) 2+2(-9.8)(s)	
S=0.596.	
0.596+68in20	
= 2.65m above the	



Leave blank