^{Surname} aymanzayedman	NAN Other	names
Pearson Edexcel	Centre Number	Candidate Number
Mechanic	c M7	
Advanced/Advance		
	d Subsidiary	Paper Reference WME02/01

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use black ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
 Coloured pencils and highlighter pens must not be used.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Whenever a numerical value of g is required, take $g = 9.8 \text{ m s}^{-2}$, and give your answer to either two significant figures or three significant figures.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 75.
- The marks for each question are shown in brackets
 use this as a quide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

PEARSON

Turn over



1. A car of mass 900 kg is travelling up a straight road inclined at an angle θ to the horizontal,

where $\sin \theta = \frac{1}{25}$. The car is travelling at a constant speed of 14 m s⁻¹ and the resistance

to motion from non-gravitational forces has a constant magnitude of 800 N. The car takes 10 seconds to travel from A to B, where A and B are two points on the road.

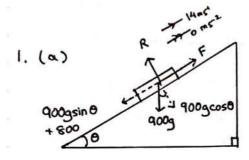
(a) Find the work done by the engine of the car as the car travels from A to B.

(4)

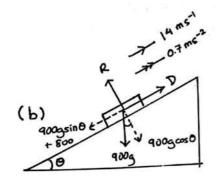
When the car is at B and travelling at a speed of $14\,\mathrm{m\,s^{-1}}$ the rate of working of the engine of the car is suddenly increased to P kW, resulting in an initial acceleration of the car of $0.7\,\mathrm{m\,s^{-2}}$. The resistance to motion from non-gravitational forces still has a constant magnitude of 800 N.

(b) Find the value of P.

(4)



$$R(A)$$
: F - 900gsin0 - 800 = 0
F = 900(9.8)($\frac{1}{25}$) +800
= 1152.8 N



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A particle *P* of mass 0.7 kg is moving in a straight line on a smooth horizontal surface.

2. A particle P of mass 0.7 kg is moving in a straight line on a smooth horizontal surface. The particle P collides with a particle Q of mass 1.2 kg which is at rest on the surface. Immediately before the collision the speed of P is 6 m s⁻¹. Immediately after the collision both particles are moving in the same direction. The coefficient of restitution between the particles is e.

(a) Show that
$$e < \frac{7}{12}$$
 (7)

Given that $e = \frac{1}{4}$

(b) find the magnitude of the impulse exerted on Q in the collision.

(3)

2. Before: $\xrightarrow{\text{G ms}^{-1}}$ 0 $\xrightarrow{\text{P}}$ 0,7kg $\xrightarrow{\text{I}_{2}\text{kg}}$ $\xrightarrow{\text{V}_{g}}$

$$(0.7) + 0(1.2) = 0.7 \text{ Vp} + 1.2 \text{ Vg}$$

$$4.2 = 0.7 \text{ Vp} + 1.2 \text{ Vg}$$

$$\frac{21}{5} = \frac{7 \text{ Vp}}{10} + \frac{6 \text{ Vg}}{5}$$

$$42 = 7 \text{ Vp} + 12 \text{ Vg} \qquad \qquad \text{ (2)}$$

NEL(→):

(i)
$$\times 12 \Rightarrow -12 \text{Vp} + 12 \text{Vg} = 72 \text{e}$$

(-) $19 \text{f} = 42 - 72 \text{e}$
 $\text{Vp} = \frac{1}{19} (42 - 72 \text{e})$

Both particles move in the same direction (>>> >>> 0

$$\frac{1}{19} (42-72e) > 0$$

$$42-72e > 0$$

$$-72e > -42$$

$$-e > \frac{-42}{72}$$



Question 2 continued

(b)
$$V_p = \frac{1}{19} (42 - 72(\frac{1}{4})) = \frac{24}{19} \text{ ms}^{-1}$$

$$I = mv - mu$$

= $m(v - u)$
= $0.7(\frac{29}{19} - 6)$
= $0.7(-\frac{90}{19})$
= $-\frac{63}{19}$
: $III = \frac{63}{19}$ Ns ≈ 3.32 Ns (3 SF)

(Total 10 marks)



3. At time t seconds $(t \ge 0)$ a particle P has velocity $\mathbf{v} \, \mathbf{m} \, \mathbf{s}^{-1}$, where

$$\mathbf{v} = (6t^2 + 6t)\mathbf{i} + (3t^2 + 24)\mathbf{j}$$

When t = 0 the particle P is at the origin O. At time T seconds, P is at the point A and $\mathbf{v} = \lambda(\mathbf{i} + \mathbf{j})$, where λ is a constant.

Find

(a) the value of T,

(3)

(b) the acceleration of P as it passes through the point A,

(3)

(c) the distance OA.

(5)

Comparing ±:

Comparing 7: 3+2+24=1

(t-2)(t+4)=0

when t=2,



Question 3 continued

c)
$$\chi = \int \chi dt$$

= $\int \left[(6e^2 + 6e) \dot{\chi} + (3e^2 + 24) \dot{\chi} \right] dt$
= $\left(\frac{6t^3}{3} + \frac{6e^2}{2} \right) \dot{\chi} + \left(\frac{3t^3}{3} + \frac{24t}{1} \right) \dot{\chi} + C$
= $\left(2t^3 + 3t^2 \right) \dot{\chi} + \left(t^3 + 24t \right) \dot{\chi} + C$

when t=0,

$$\chi = (2t^3+3t^2) + (t^3+24t) = m$$

when
$$t=2$$
,
 $\chi = (2(2)^3 + 3(2)^2) = (2^3 + 24(2)) = (2(2)^3 + 3(2)^2) = (2^3 + 24(2)) = (2^$

(Total 11 marks)





4.

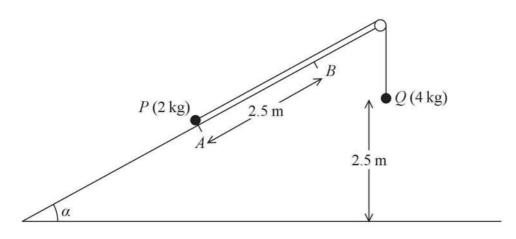


Figure 1

Two particles P and Q, of mass 2 kg and 4 kg respectively, are connected by a light inextensible string. Initially P is held at rest at the point A on a rough fixed plane inclined

at α to the horizontal ground, where $\sin \alpha = \frac{3}{5}$. The string passes over a small smooth

pulley fixed at the top of the plane. The particle Q hangs freely below the pulley and 2.5 m above the ground, as shown in Figure 1. The part of the string from P to the pulley lies along a line of greatest slope of the plane. The system is released from rest with the string taut. At the instant when Q hits the ground, P is at the point B on the plane. The coefficient of friction between P and the plane is $\frac{1}{A}$.

- (a) Find the work done against friction as P moves from A to B. (4)
- (b) Find the total potential energy lost by the system as P moves from A to B. (3)
- (c) Find, using the work-energy principle, the speed of P as it passes through B. (4)

(a)
$$R(x)$$
: $R = 2g\cos x$

$$= 2g \left(\frac{4}{5}\right)$$

$$R = \frac{59}{5} \text{ IV}$$

$$F = \mu R$$

$$= \frac{1}{4} \times \frac{89}{5}$$

$$F = \frac{29}{5} \text{ N}$$

Work done against friction =
$$\frac{29}{5} \times 2.5$$



= 9.8 J

Question 4 continued

At the point when
$$Q$$
 hits the ground, P and Q travel at the same speed $KE_p = \frac{1}{2}(2)v^2$

$$= v^2$$
 $KE_Q = \frac{1}{2}(4)v^2$

$$= 2v^2$$

KE gained by the system = 2v2+v2= 3v2

PE 1.54 by the system = Work alone against Richion + KE gained by the system
$$7g = g + 3v^2$$

$$6g = 3v^2$$

$$2g = v^2$$

$$v = \sqrt{(2g)} = 4.42718... \approx 4.43 \text{ ms}^4 (3SF)$$

(Total 11 marks)

Q4

5.

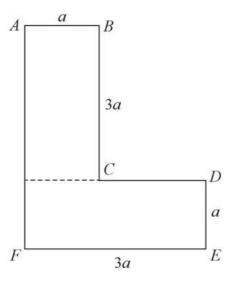


Figure 2

The uniform lamina ABCDEF, shown in Figure 2, consists of two identical rectangles with sides of length a and 3a. The mass of the lamina is M. A particle of mass kM is attached to the lamina at E. The lamina, with the attached particle, is freely suspended from A and hangs in equilibrium with AF at an angle θ to the downward vertical.

Given that $\tan \theta = \frac{4}{7}$, find the value of k.

(10)



Question 5 continued

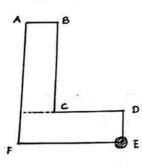
5.	٨	-	18
			3a
			<u> </u>
	F		3a E

 mass	/area	be	m

		E			. Com FE
F _	30			el Distance	of COM HOW
let	mass /ar	ea be m	Distance of COH	from AF	50/2
Shope	Mass	Hass rat	Distance of COH		2/2
[]_	3a²m	e	3%		/2
\Box_{ϵ}^{c}	3a2m				3
<u> </u>	6a ² m	2	泵	1	

$$M_{(F)}: 2\bar{z} = \frac{a}{2} + \frac{3a}{2}$$
 $H_{(F)}: 2\bar{5} = \frac{5a}{2} + \frac{a}{2}$
 $\bar{y} = \frac{3a}{2}$

COM of the lamina is $(a, \frac{3a}{2})$.



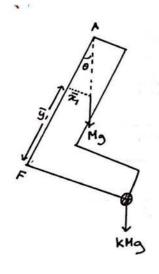
2	•		Distance of COM from	from to
Shape	Mass	Mass ratios	Distance of COM from	39/2
	м	L	3a	0
0	KM			-
r ₂	(1+k)M	K+1	元	1 2,
-	18	•		30

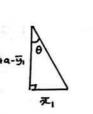
$$M_{(F)}: (k+1) \overline{Z}_1 = \alpha + 3 \alpha k$$
 $M_{(F)}: (k+1) \overline{Z}_1 = \frac{3\alpha}{2} + 0$

$$= \alpha (1+3k)$$

$$\overline{Z}_1 = \frac{\alpha (1+3k)}{k+1}$$

$$\overline{Z}_1 = \frac{3\alpha}{2(k+1)}$$





Question 5 continued

$$\frac{4}{7} = \frac{2+6k}{8k+5}$$

$$k = \frac{6}{10}$$

$$\therefore k = \frac{3}{5}$$

(Total 10 marks)

Q5



6.

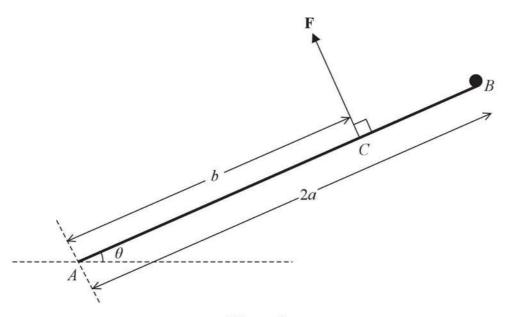


Figure 3

A uniform rod AB, of mass 3m and length 2a, is freely hinged at A to a fixed point on horizontal ground. A particle of mass m is attached to the rod at the end B. The system is held in equilibrium by a force \mathbf{F} acting at the point C, where AC = b. The rod makes an acute angle θ with the ground, as shown in Figure 3. The line of action of \mathbf{F} is perpendicular to the rod and in the same vertical plane as the rod.

(a) Show that the magnitude of **F** is
$$\frac{5mga}{b}\cos\theta$$
 (4)

The force exerted on the rod by the hinge at A is \mathbf{R} , which acts upwards at an angle ϕ above the horizontal, where $\phi > \theta$.

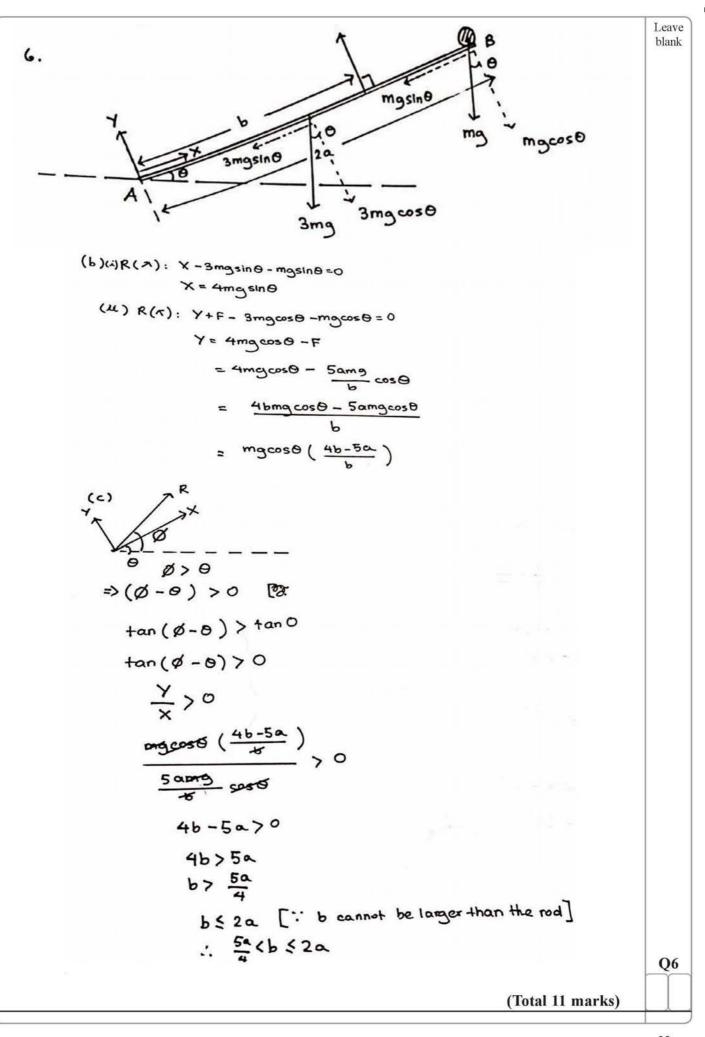
- (b) Find
 - (i) the component of **R** parallel to the rod, in terms of m, g and θ ,
 - (ii) the component of **R** perpendicular to the rod, in terms of a, b, m, g and θ . (5)
- (c) Hence, or otherwise, find the range of possible values of b, giving your answer in terms of a.

(2)

(a)
$$M(A) \bigcirc : bF = 3amgcos0 + 2a(mgcos0)$$

$$bF = 5amgcos0$$

$$\therefore F = \frac{5amg}{b} \cos0$$



7.

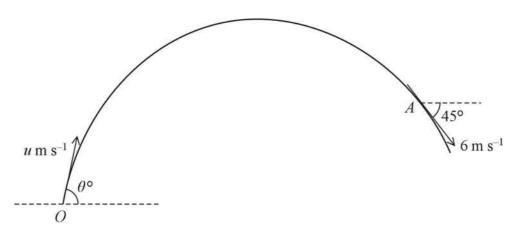


Figure 4

At time t = 0, a particle P of mass 0.7 kg is projected with speed u m s⁻¹ from a fixed point O at an angle θ ° to the horizontal. The particle moves freely under gravity. At time t = 2 seconds, P passes through the point A with speed 6 m s⁻¹ and is moving downwards at 45° to the horizontal, as shown in Figure 4.

Find

(a) the value of θ ,

(6)

(b) the kinetic energy of P as it reaches the highest point of its path.

(3)

For an interval of T seconds, the speed, $v \text{ m s}^{-1}$, of P is such that $v \leq 6$

(c) Find the value of T.

(5)

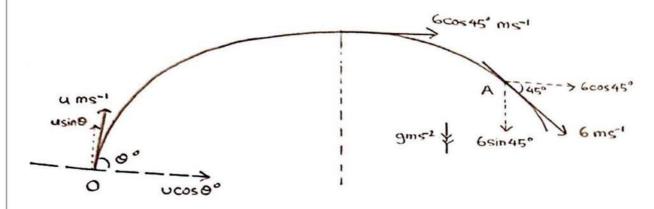
(a) Horizontal velocity is constant (=> ucos 0 = 6cos 45°

R(t):
$$S=$$
 $u = usin\theta$
 $V = -6sin45$
 $a = -9$
 $t = 2$
 $2g - 6sin45$ = $4sin\theta - g(2)$
 $-6sin45$ = $(\frac{6cos45}{cos\theta} \times sin\theta) - 2g$
 $-2g - 6sin45$ = $(\frac{6cos45}{cos\theta} \times sin\theta) - 2g$
 $-2g - 6sin45$ = $(\frac{2g - 6sin45}{6cos45})$
 $-6sin45$ = $(\frac{2g - 6sin45}{6cos45})$

∴ 0 ≈ 74.6° (3 SF)

Question 7 continued

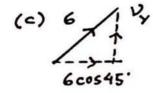
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(b) At the highest point, the only component of velocity acting is the horizontal component.

KE at highest point =
$$\frac{1}{2} \dot{m} v^2 = \frac{1}{2} (0.7) (6 \cos 45^{\circ})^2$$

= 0.35 (18)
= 6.3 J



$$6^2 = Vy^2 + (6cos45')^2$$

 $36 = Vy^2 + 18$
 $18 = Vy^2$
 $V_{y=} \pm \sqrt{18} = \pm 3\sqrt{2} \text{ ms}^{-1}$

When the ball moves at 6 mg-1 for the first time,

$$R(\tau)$$
: S=
 $u = u \sin \theta = 15.35735931...$
 $v = 3\sqrt{2}$
 $a = -9 \text{ ms}^{-2}$
 $t = ?$

Q7

Question 7 continued

When the ball moves at 6ms for the second time,

u= 15.357359...

(Total 14 marks)

TOTAL FOR PAPER: 75 MARKS

END

