Write your name here		
Surname	Othe	r names
Pearson Edexcel Level 3 GCE	Centre Number	Candidate Number
Further M Advanced Paper 2: Core Pure M		
Sample Assessment Material for first t	eaching September 2017	Paper Reference
Time: 1 hour 30 minutes		9FM0/02

#### Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for algebraic manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 7 questions in this question paper. The total mark for this paper is 75.
- The marks for each question are shown in brackets
   use this as a guide as to how much time to spend on each question.

# Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.



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## Answer ALL questions. Write your answers in the spaces provided.

1. The roots of the equation

 $x^3 - 8x^2 + 28x - 32 = 0$ 

are  $\alpha$ ,  $\beta$  and  $\gamma$ 

Without solving the equation, find the value of

(i) 
$$\frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma}$$
  
(ii)  $(\alpha + 2)(\beta + 2)(\gamma + 2)$   
(iii)  $\alpha^2 + \beta^2 + \gamma^2$ 

(8)

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	(Total for Question 1 is 8 marks)

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**2.** The plane  $\Pi_1$  has vector equation

$$\mathbf{r}.(3\mathbf{i}-4\mathbf{j}+2\mathbf{k})=5$$

(a) Find the perpendicular distance from the point (6, 2, 12) to the plane  $\Pi_1$ 

The plane  $\Pi_2$  has vector equation

$$\mathbf{r} = \lambda(2\mathbf{i} + \mathbf{j} + 5\mathbf{k}) + \mu(\mathbf{i} - \mathbf{j} - 2\mathbf{k})$$

where  $\lambda$  and  $\mu$  are scalar parameters.

- (b) Show that the vector  $-\mathbf{i} 3\mathbf{j} + \mathbf{k}$  is perpendicular to  $\Pi_2$
- (c) Show that the acute angle between  $\Pi_1$  and  $\Pi_2$  is 52° to the nearest degree.

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**3.** (i)

<b>M</b> =	( 2	а	4)
<b>M</b> =	1	-1	-1
	(-1	2	-1)

where a is a constant.

(a) For which values of a does the matrix **M** have an inverse?

Given that **M** is non-singular,

(b) find  $\mathbf{M}^{-1}$  in terms of a

(ii) Prove by induction that for all positive integers n,

$$\begin{pmatrix} 3 & 0 \\ 6 & 1 \end{pmatrix}^n = \begin{pmatrix} 3^n & 0 \\ 3(3^n - 1) & 1 \end{pmatrix}$$
 (6)

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Question 3 continued	

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- 4. A complex number z has modulus 1 and argument  $\theta$ .
  - (a) Show that

$$z^{n} + \frac{1}{z^{n}} = 2\cos n\theta, \qquad n \in \mathbb{Z}^{+}$$
(2)

(b) Hence, show that
$$cos^{4}\theta = \frac{1}{8}(cos 4\theta + 4cos 2\theta + 3)$$
(5)

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Question 4 con	tinued	
		(Total for Question 4 is 7 marks)
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Show that $\frac{d^4y}{dx^4} = -4y$	
Show that $\frac{dx^4}{dx^4} = -4y$	
	(4)
Hence find the first three non-zero terms of the Maclaurin series for $y$ , giving eac	ch
coefficient in its simplest form.	(4)
Find an expression for the <i>n</i> th non-zero term of the Maclaurin series for <i>y</i> .	(2)
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Question 5 continued	
	(Total for Question 5 is 10 marks)

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6. (a) (i) Show on an Argand diagram the locus of points given by the values of z satisfying

$$|z-4-3\mathbf{i}|=5$$

Taking the initial line as the positive real axis with the pole at the origin and given that  $\theta \in [\alpha, \alpha + \pi]$ , where  $\alpha = -\arctan\left(\frac{4}{3}\right)$ ,

(ii) show that this locus of points can be represented by the polar curve with equation

$$r = 8\cos\theta + 6\sin\theta$$

The set of points A is defined by

$$A = \left\{ z : 0 \leqslant \arg z \leqslant \frac{\pi}{3} \right\} \cap \left\{ z : \left| z - 4 - 3\mathbf{i} \right| \leqslant 5 \right\}$$

(b) (i) Show, by shading on your Argand diagram, the set of points A.

(ii) Find the exact area of the region defined by A, giving your answer in simplest form.

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Question 6 continued	
	(Total for Question 6 is 13 marks)

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7. At the start of the year 2000, a survey began of the number of foxes and rabbits on an island.

At time t years after the survey began, the number of foxes, f, and the number of rabbits, r, on the island are modelled by the differential equations

$$\frac{\mathrm{d}f}{\mathrm{d}t} = 0.2 f + 0.1 r$$
$$\frac{\mathrm{d}r}{\mathrm{d}t} = -0.2 f + 0.4 r$$

(a) Show that  $\frac{d^2 f}{dt^2} - 0.6 \frac{df}{dt} + 0.1 f = 0$ 

- (b) Find a general solution for the number of foxes on the island at time *t* years.
- (c) Hence find a general solution for the number of rabbits on the island at time *t* years.

(3)

(3)

(4)

At the start of the year 2000 there were 6 foxes and 20 rabbits on the island.

- (d) (i) According to this model, in which year are the rabbits predicted to die out?
  - (ii) According to this model, how many foxes will be on the island when the rabbits die out?
  - (iii) Use your answers to parts (i) and (ii) to comment on the model.

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	(Total for Question 7 is 17 marks)
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ă I	TOTAL FOR PAPER IS 75 MARKS
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