UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS
General Certificate of Education Advanced Subsidiary Level and Advanced Level
Advanced International Certificate of Education

MATHEMATICS **9709/06**

STATISTICS **0390/06**

Paper 6 Probability & Statistics 1 **(S1)**

October/November 2004

1 hour 15 minutes

Additional materials: Answer Booklet/Paper
Graph paper
List of Formulae (MF9)

READ THESE INSTRUCTIONS FIRST

If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet.
Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen on both sides of the paper.
You may use a soft pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** the questions.
Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles
in degrees, unless a different level of accuracy is specified in the question.
At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.
The total number of marks for this paper is 50.
Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger
numbers of marks later in the paper.
The use of an electronic calculator is expected, where appropriate.
You are reminded of the need for clear presentation in your answers.

This document consists of **3** printed pages and **1** blank page.

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International Examinations

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2

1 The word ARGENTINA includes the four consonants R, G, N, T and the three vowels A, E, I.

   (i) Find the number of different arrangements using all nine letters. [2]

   (ii) How many of these arrangements have a consonant at the beginning, then a vowel, then another consonant, and so on alternately? [3]

2 The lengths of cars travelling on a car ferry are noted. The data are summarised in the following table.

Length of car (x metres)	Frequency	Frequency density
$2.80 \leqslant x < 3.00$	17	85
$3.00 \leqslant x < 3.10$	24	240
$3.10 \leqslant x < 3.20$	19	190
$3.20 \leqslant x < 3.40$	8	a

   (i) Find the value of a. [1]

   (ii) Draw a histogram on graph paper to represent the data. [3]

   (iii) Find the probability that a randomly chosen car on the ferry is less than 3.20 m in length. [2]

3 When Andrea needs a taxi, she rings one of three taxi companies, A, B or C. 50% of her calls are to taxi company A, 30% to B and 20% to C. A taxi from company A arrives late 4% of the time, a taxi from company B arrives late 6% of the time and a taxi from company C arrives late 17% of the time.

   (i) Find the probability that, when Andrea rings for a taxi, it arrives late. [3]

   (ii) Given that Andrea's taxi arrives late, find the conditional probability that she rang company B. [3]

4 The ages, x years, of 18 people attending an evening class are summarised by the following totals: $\Sigma x = 745, \Sigma x^2 = 33\,951$.

   (i) Calculate the mean and standard deviation of the ages of this group of people. [3]

   (ii) One person leaves the group and the mean age of the remaining 17 people is exactly 41 years. Find the age of the person who left and the standard deviation of the ages of the remaining 17 people. [4]

5 The length of Paulo's lunch break follows a normal distribution with mean μ minutes and standard deviation 5 minutes. On one day in four, on average, his lunch break lasts for more than 52 minutes.

   (i) Find the value of μ. [3]

   (ii) Find the probability that Paulo's lunch break lasts for between 40 and 46 minutes on every one of the next four days. [4]

3

6 A box contains five balls numbered 1, 2, 3, 4, 5. Three balls are drawn randomly at the same time from the box.

   (i) By listing all possible outcomes (123, 124, etc.), find the probability that the sum of the three numbers drawn is an odd number.   [2]

   The random variable L denotes the largest of the three numbers drawn.

   (ii) Find the probability that L is 4.   [1]

   (iii) Draw up a table to show the probability distribution of L.   [3]

   (iv) Calculate the expectation and variance of L.   [3]

7   **(i)** State two conditions which must be satisfied for a situation to be modelled by a binomial distribution.   [2]

   In a certain village 28% of all cars are made by Ford.

   (ii) 14 cars are chosen randomly in this village. Find the probability that fewer than 4 of these cars are made by Ford.   [4]

   (iii) A random sample of 50 cars in the village is taken. Estimate, using a normal approximation, the probability that more than 18 cars are made by Ford.   [4]

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