

Cambridge  
International  
**A Level**

**Cambridge International Examinations**  
Cambridge International Advanced Level

CANDIDATE  
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**MATHEMATICS**

**9709/31**

Paper 3 Pure Mathematics 3 (P3)

**May/June 2017**

**1 hour 45 minutes**

Candidates answer on the Question Paper.

Additional Materials: List of Formulae (MF9)

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

**DO NOT WRITE IN ANY BARCODES.**

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 75.

This document consists of **19** printed pages and **1** blank page.



















**(ii)** Verify by calculation that  $x$  lies between 1 and 1.5. [2]

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**(iii)** Use an iterative formula based on the equation in part **(i)** to determine  $x$  correct to 3 decimal places. Give the result of each iteration to 5 decimal places. [3]

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6 The plane with equation  $2x + 2y - z = 5$  is denoted by  $m$ . Relative to the origin  $O$ , the points  $A$  and  $B$  have coordinates  $(3, 4, 0)$  and  $(-1, 0, 2)$  respectively.

(i) Show that the plane  $m$  bisects  $AB$  at right angles. [5]

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A second plane  $p$  is parallel to  $m$  and nearer to  $O$ . The perpendicular distance between the planes is 1.

(ii) Find the equation of  $p$ , giving your answer in the form  $ax + by + cz = d$ . [3]

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**7 Throughout this question the use of a calculator is not permitted.**

The complex numbers  $u$  and  $w$  are defined by  $u = -1 + 7i$  and  $w = 3 + 4i$ .

- (i) Showing all your working, find in the form  $x + iy$ , where  $x$  and  $y$  are real, the complex numbers  $u - 2w$  and  $\frac{u}{w}$ . [4]

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In an Argand diagram with origin  $O$ , the points  $A$ ,  $B$  and  $C$  represent the complex numbers  $u$ ,  $w$  and  $u - 2w$  respectively.

- (ii) Prove that angle  $AOB = \frac{1}{4}\pi$ . [2]

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(iii) State fully the geometrical relation between the line segments  $OB$  and  $CA$ . [2]

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- 8 (i) By first expanding  $2 \sin(x - 30^\circ)$ , express  $2 \sin(x - 30^\circ) - \cos x$  in the form  $R \sin(x - \alpha)$ , where  $R > 0$  and  $0^\circ < \alpha < 90^\circ$ . Give the exact value of  $R$  and the value of  $\alpha$  correct to 2 decimal places. [5]

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(ii) Hence solve the equation

$$2 \sin(x - 30^\circ) - \cos x = 1,$$

for  $0^\circ < x < 180^\circ$ .

[3]

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- 9 (i) Express  $\frac{1}{x(2x+3)}$  in partial fractions. [2]

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- (ii) The variables  $x$  and  $y$  satisfy the differential equation

$$x(2x+3)\frac{dy}{dx} = y,$$

and it is given that  $y = 1$  when  $x = 1$ . Solve the differential equation and calculate the value of  $y$  when  $x = 9$ , giving your answer correct to 3 significant figures. [7]

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