

CAMBRIDGE INTERNATIONAL EXAMINATIONS

November 2003

GCE A AND AS LEVEL

MARK SCHEME

MAXIMUM MARK: 75

SYLLABUS/COMPONENT: 9709/01

MATHEMATICS Pure Mathematics : Paper One



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	10	2.64	
1 x(11-2x)	= 12	Ml	Complete elimination of x, or of y.
$2x^2-11x+$	12=0	A1	Correct quadratic. (or $y^2-11y+24=0$)
Solution	of quadratic	DM1	Correct method of solution \rightarrow 2values
$\rightarrow (1\frac{1}{2}, 8)$	(4,3) and $(4,3)$	A1	All correct
	, , , , , , , , , , , , , , , , , , ,	[4]	(guesswork or TI B1 for one pair of
			values, full marks for both)
2 (i) $4c4\pm5c$	$-7(1 c^2) \rightarrow 4y^2 + 7y^2 - 0$	B1	Use of $s^2+c^2=1$ Answer given
2 (1) 48 + 5	$-7(1-5) \rightarrow 4x + 7x-2-0$	[1]	
		[1]	
(ii) 4s ⁴ +7	$s^{2}-2=0$	MI	Decompition of moduli in a?
\rightarrow s ² = ¹ /	4 or $s^2 = -2$	IVI I	Recognition of quadratic in s ²
$\rightarrow \sin \theta =$	$= +\frac{1}{2}$		
$\rightarrow \theta - 3$	0° and 150°	A1A1√	Co. For 180° - "his value"
$\rightarrow 0-3$	0° and 130°	A1√	For other 2 answers from "his value"
	210 and 350	[4]	providing no extra answers in the range or
		[,]	providing no extra answers in the range of answers from $s^2 - 1$
2 (a) a=(0	n-18 S -3726		
(a) a=00	$n - 40, S_n - 3/20$	M1	$C_{\text{ansat}} = (M_0)^{1/2} ($
S_n formul	la used	MI	Correct formula (MO if nth term used)
\rightarrow d = \$0	0.75	Al	Co
3 rd term =	= a+2d = \$61.50	Al√	Use of $a+2d$ with his d. 61.5 ok.
		[3]	
(b) a=6	ar =4 \therefore r= ² / ₃	M1	a, ar correct, and r evaluated
$S_{\infty} = a/($	1-r) = 18	M1A1	Correct formula used, but needs $r < 1$ for
		[3]	M mark
4 (i) $y = x^3$	$-2x^2 + x (+c)$	B2,1,0	Co - unsimplified ok.
(1,5) used	d to give $c=5$	B1√	Must have integrated + use of $x=1$ and $y=5$
		[3]	for c
(ii) 3x ² -4x	+1>0	M1	Set to 0 and attempt to solve.
\rightarrow end va	alues of 1 and $\frac{1}{2}$	A1	Co for end values – even if <,>,=,etc
	3	A1	Co (allow < and >). Allow $1 \le x \le \frac{1}{2}$
$\rightarrow X < \frac{2}{3} a$	x > 1	[3]	
5	(i) m of BC = $\frac{1}{2}$	B1	Со
A 91	Eqn BC $y-6=\frac{1}{2}(x-4)$	M1A1√	Correct form of eqn. $\sqrt{\text{ on m}}="1/2"$."
6.0	m of $CD = -2$	M1	Use of $m_1m_2=-1$
8 79	eqn CD v-5=-2(x-12)	A1√	$\sqrt{100}$ on his "1/2" but needs both M marks
I'r \		[5]	
	D	[2]	
(2.0) T (1)	(,5)		
0 40	-> ×		
-			
(ii) Sim e	ans $2y=x+8$ and $y+2x=29$	M1	Method for solving
\rightarrow C (1)	(0.9)	A1	Co
	,>)	Г <u>г</u> гол	Diagram only for (ii) allow R1 for (10.0)
		[4]	Diagram uny 101 (n), anow D1 101 (10,9)

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6 (i) $20 = 2r + r\theta$ $\rightarrow \theta = (20 / r) - 2$	M1 A1 [2]	Eqn formed + use of $r\theta$ + at least one r Answer given.
$(ii) A = \frac{1}{2}r^{2}\theta$ $\rightarrow A = 10r - r^{2}$	M1 A1 [2]	Appropriate use of $\frac{1}{2}r^2\theta$ Co – but ok unsimplified –eg $\frac{1}{2}r^2(20/r)-2$)
(iii) Cos rule $PQ^2 = 8^2+8^2-2.8.8\cos 0.5$ Or trig $PQ = 2 \times 8\sin 0.25$	M1 A1	Recognition of "chord" +any attempt at trigonometry in triangle. Correct expression for PQ or PQ ² .
\rightarrow PQ = 3.96 (allow 3.95).	A1 [3]	Со
7 (i) Height = 4	B1 [1]	Pythagoras or guess – anywhere, 4k ok.
$\begin{array}{c} \textbf{B} \\ \textbf{5} \\ \textbf{5} \\ \textbf{5} \\ \textbf{6} \\ \textbf{0} \\ \textbf{1} \\ $	B2,1√ B1√ [3]	$\sqrt{10}$ for "4". Special case B1 for $-3i+6j+4k$ $\sqrt{10}$ on "4". Accept column vectors.
AGC D	[-]	(nb if (ii) incorrect, but answers are correct in (iii) allow feedback).
(iii) MC.MN = $-36+16 = -20$ MC.MN = $\sqrt{61}\sqrt{52}\cos\theta$ $\rightarrow \theta = 111^{\circ}$	M1A1√ M1 A1 [4]	Use of $x_1y_1+x_2y_2+x_3y_3$. $$ on MC and MN Product of two moduli and $\cos \theta$. Co.
		111° for full marks.
8 (i) $y = 72 \div (2x^2)$ or $36 \div x^2$ $A = 4x^2 + 6xy$ $\rightarrow A = 4x^2 + 216 \div x$	B1 M1 A1 [3]	Co from volume = lbh . Attempts most of the faces(4 or more) Co – answer was given.
(ii) $dA/dx = 8x - 216 \div x^2$ = 0 when $8x^3 = 216$ $\rightarrow x = 3$	M1 DM1 A1 [3]	Reasonable attempt at differentiation. Sets his differential to 0 and uses. Co. (answer = ± 3 loses last A mark)
(iii) Stationary value = 108 cm^2	A1√	For putting his x into his A. Allow in (ii).
$d^{2}A/dx^{2}=8+432 \div x^{3}$ \rightarrow Positive when x=3 Minimum.	M1 A1 [3]	Correct method – could be signs of dA/dx A mark needs d^2A/dx^2 correct algebraically, + x=3 + minimum. It does not need "24".

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9 (i) $dy/dx = -24/(3x+2)^2$	M1A1	Use of fn of fn. Needs $\times 3$ for M mark. Co.
Eqn of tangent y-1=- $\frac{3}{8}$ (x-2) Cuts y=0 when x= $\frac{42}{3}$	M1A1√	Use of line form with dy/dx. Must use calculus. $$ on his dy/dx. Normal M0.
Area of $Q = \frac{1}{2} \times \frac{2^2}{3} \times 1 = \frac{4}{3}$	M1A1 [6]	Needs y=0 and ½bh for M mark. (beware fortuitous answers)
(ii) Vol = $\pi \int y^2 dx = \pi \int 64(3x+2)^{-2} dx$ = $\pi [-64(3x+2)^{-1} \div 3]$ Limits from 0 to 2 $\rightarrow 8\pi$	M1 A1A1 DM1 A1 [5]	Uses $\int y^2 + \text{some integration} \rightarrow (3x+2)^k$. A1 without the $\div 3$. A1 for $\div 3$ and π Correct use of 0 and 2. DMO if 0 ignored. Co. Beware fortuitous answers.
10 (i) $fg(x) = g$ first, then f	M1	Correct order - g first, then into f.
= 8/(2-x) - 5 = 7	DM1	Correct method of solution of fg=7.
$\rightarrow x = 1\frac{1}{3}$	A1	Co. (nb gf gets $0/3$)
(or f(A)=7, A = 6, g(x) = 6, $\rightarrow x = 1\frac{1}{3}$)	[3]	(M1 for 6. M1 for g(x)=6. A1)
(ii) $f^1 = \frac{1}{2}(x+5)$ Makes y the subject $y = 4 \div (2-x)$ $\rightarrow g^{-1} = 2 - (4 \div x)$	B1 M1 A1 [3]	Anywhere in the question. For changing the subject. Co – any correct answer. (A0 if f(y).)
(iii) $2-4/x = \frac{1}{2} (x+5)$ $\rightarrow x^2+x+8=0$ Use of b ² -4ac \rightarrow Negative value \rightarrow No roots.	M1 M1 A1 [3]	Algebra leading to a quadratic. Quadratic=0 + use of b ² -4ac. Correct deduction from correct quadratic.
(iv)	B1 B1 B1 [3]	Sketch of f Sketch of f ⁻¹ Evidence of symmetry about y=x.